

# Lagrangian temperature and vertical velocity fluctuations due to gravity waves in the lower stratosphere



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# Introduction

- Sensitivity of chemistry and microphysics to temperature-vertical velocity fluctuations (Polar Stratospheric Clouds, cirrus, aerosols)

Example of the impact the gravity wave “fast” temperature fluctuations on the microphysics : homogeneously nucleated ice crystal number concentration in cirrus clouds

- to constrain the temperature fluctuations undergone by air parcels, need of Lagrangian observation of the fluctuations

# Superpressure Balloon campaigns provide a good and unbiased sampling over regions of interest

Superpressure balloon campaigns in 2010

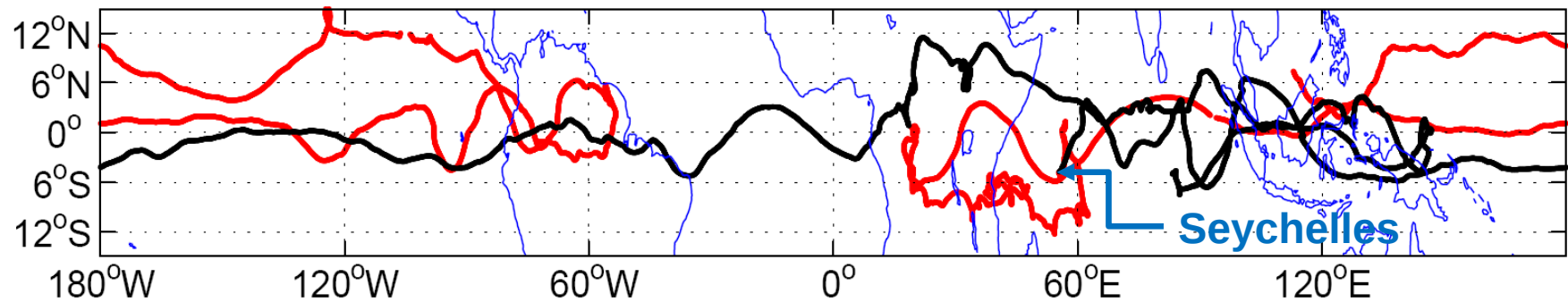
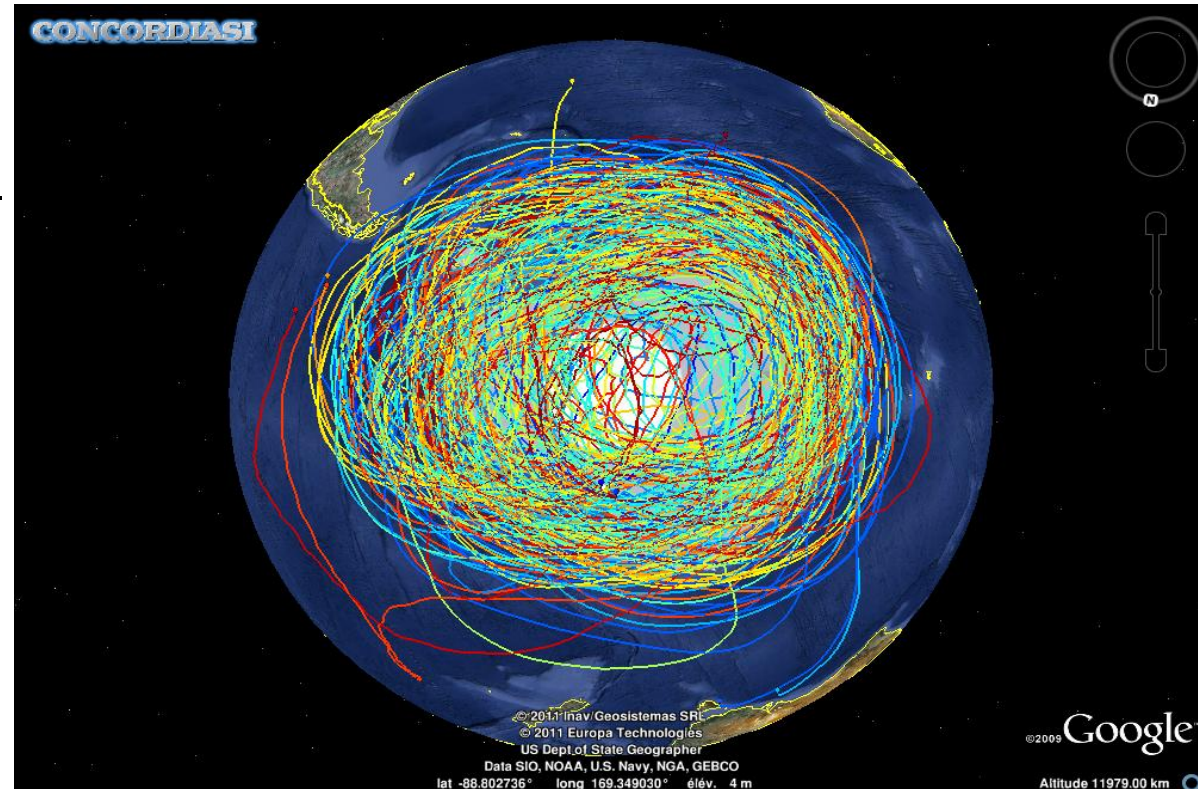
19 balloons over Antarctica (September-December, austral spring): **PSCs**

2 balloons in the tropics (March-May, boreal spring): **TTL cirrus**

~3 months flights

1 min sampling

Measurements of the balloon position, temperature, pressure



# Superpressure Balloon flights allow to quantify Lagrangian Temperature and vertical velocity fluctuations

On the horizontal, the balloon follows the wind field :

**quasi-Lagrangian measurements**

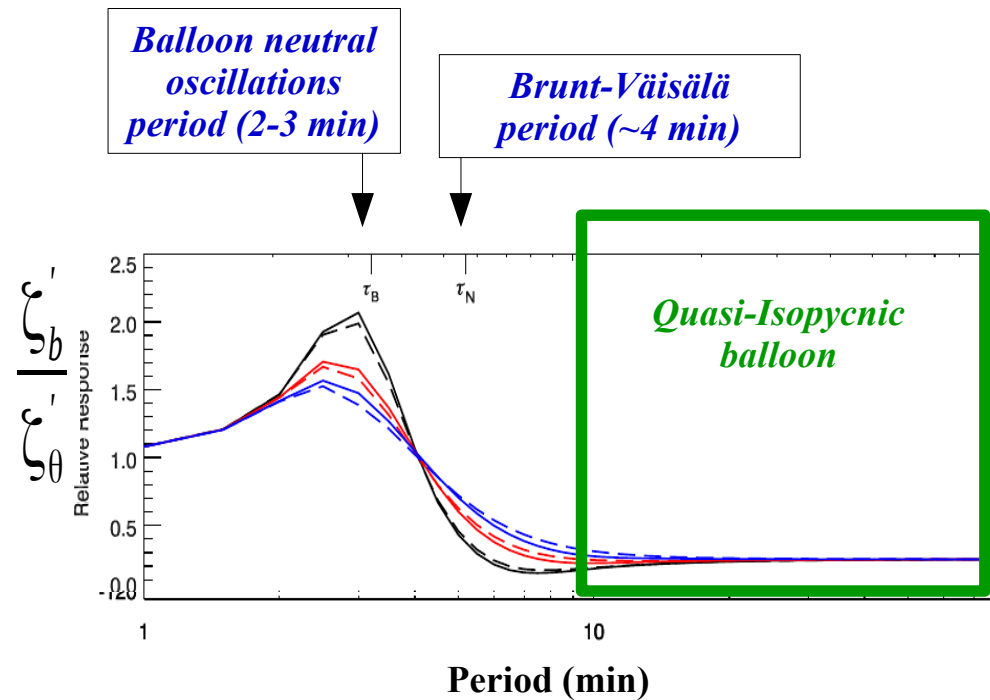
On the vertical, we consider that the balloon follows **isopycnic (constant density) surfaces** (questionable at GW high frequencies)

The vertical displacement of (isentropic) air parcels  $\zeta_\theta$  is deduced from that of the isopycnic balloon  $\zeta_\rho$  (deduced from pressure)

$\zeta_\rho = \alpha \zeta_\theta$  where  $\alpha \simeq 0.3$  in the lower stratosphere

**Lagrangian temperature fluctuations  $T_l'$  are deduced from the estimated vertical displacement (dry adiabatic):**

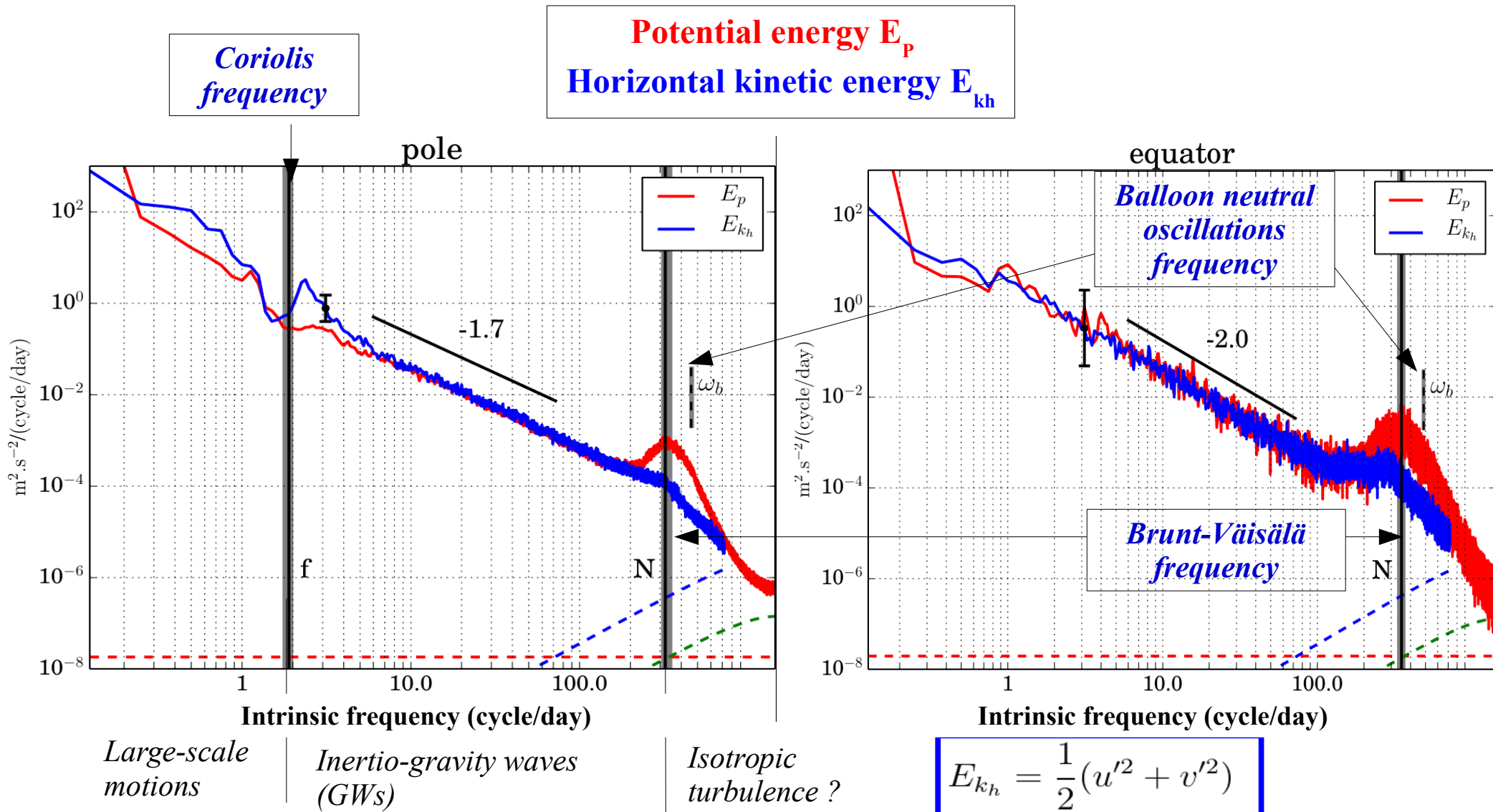
$$T_l' = -\frac{g}{C_p} \zeta_\theta'$$



*Vincent and Hertzog, 2014*



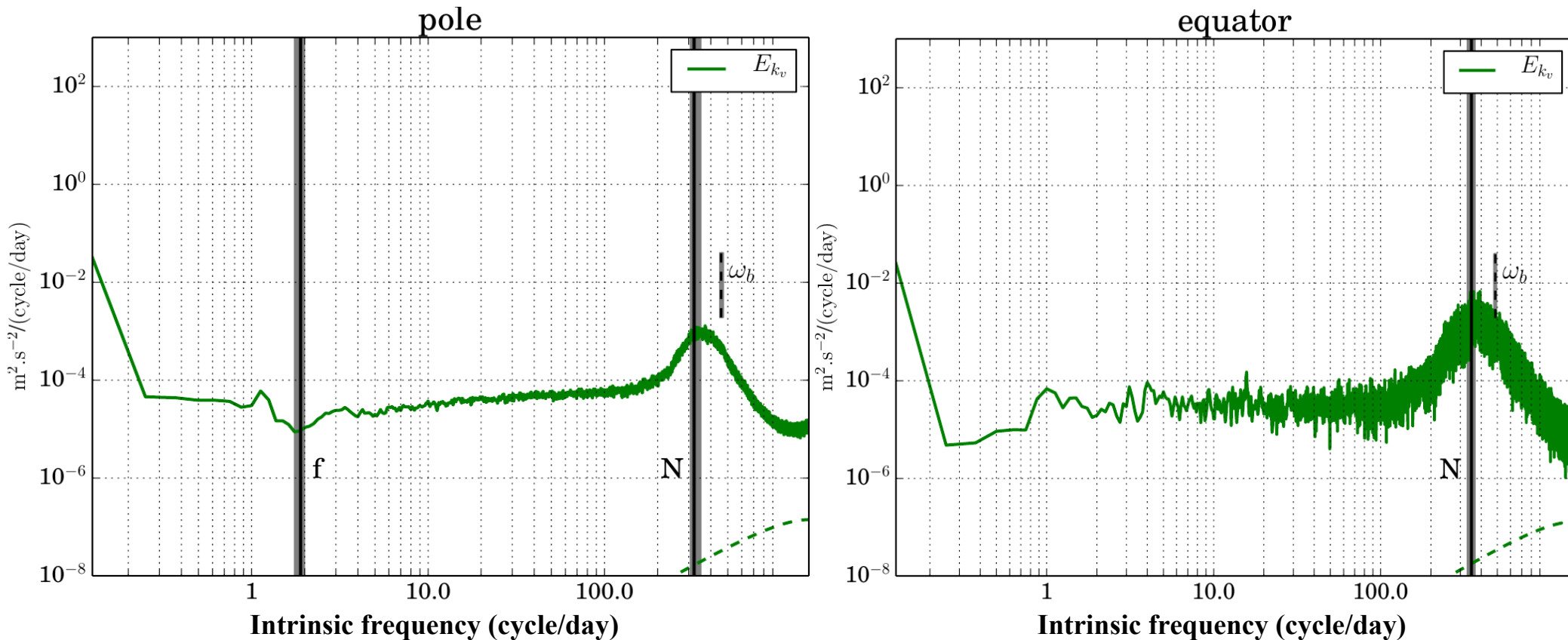
# Observed spectra of atmospheric motions show scaling behavior and exceptions in the GW range



Exceptions to scaling behavior : peaks at  $f$  in  $E_{kh}$  and at  $N$  in  $E_p$  (pollution by non isopycnic behavior ?)

# High frequency gravity waves dominate the vertical velocity

## Vertical kinetic energy



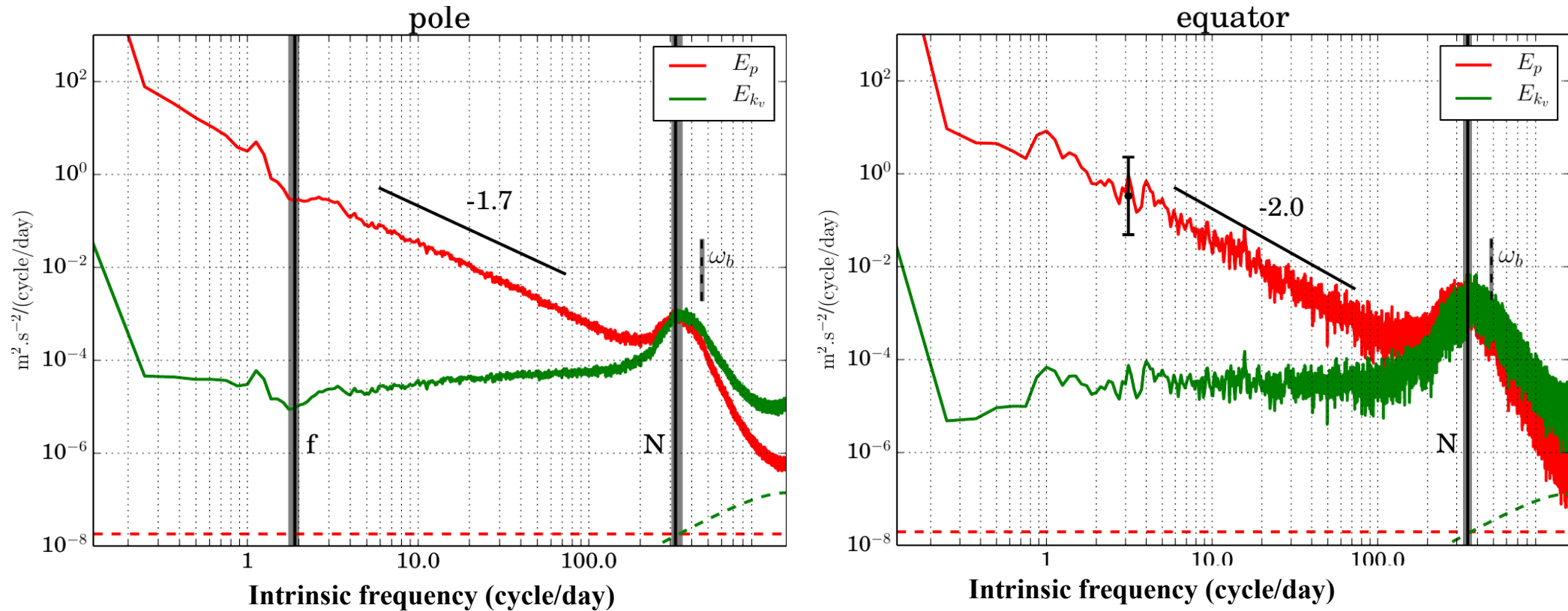
The spectrum of vertical velocity is approximately flat up to  $N/2$  both in the tropics and the pole, then increases towards  $N$ . Potential effect of the balloon response at these high frequencies.

In any case, the **variance of vertical velocity** is mainly contained in the **high frequencies**; strong maxima in vertical velocity variance at the Brunt-Väisälä frequency.



# How do microphysically relevant quantities relate to balloon observations ?

Lagrangian temperature fluctuation power spectrum  
Lagrangian cooling rates power spectrum



Lagrangian Temperature fluctuations (deduced from the vertical displacement) :

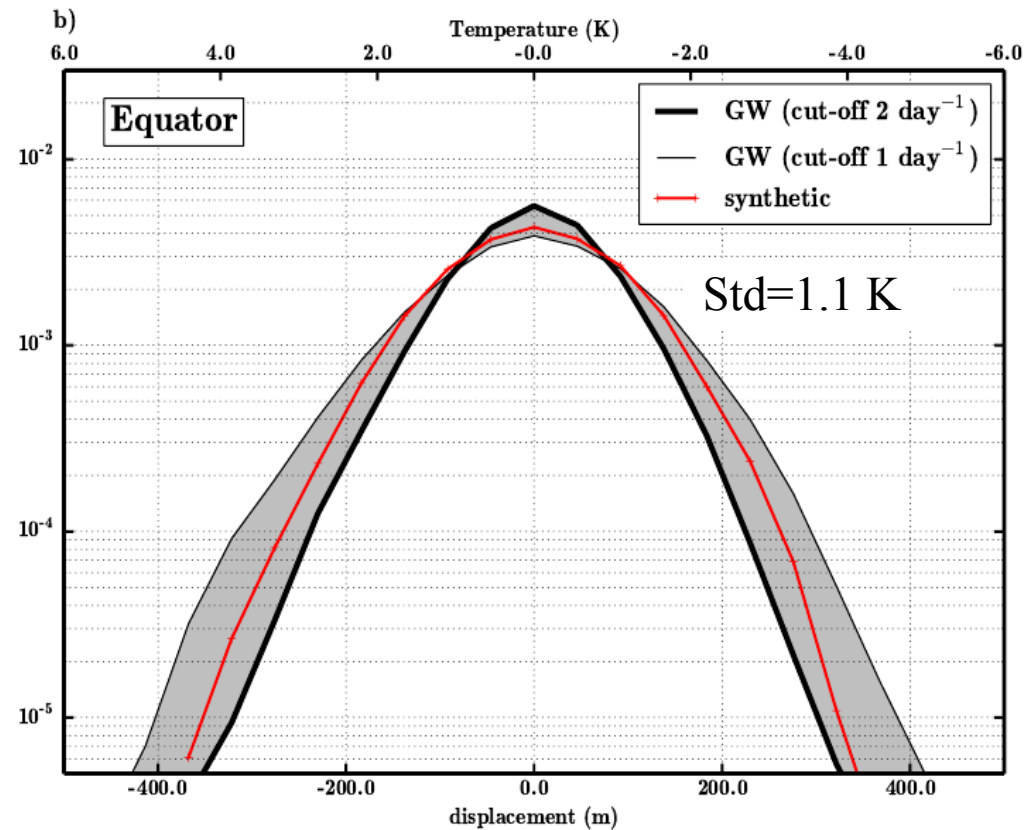
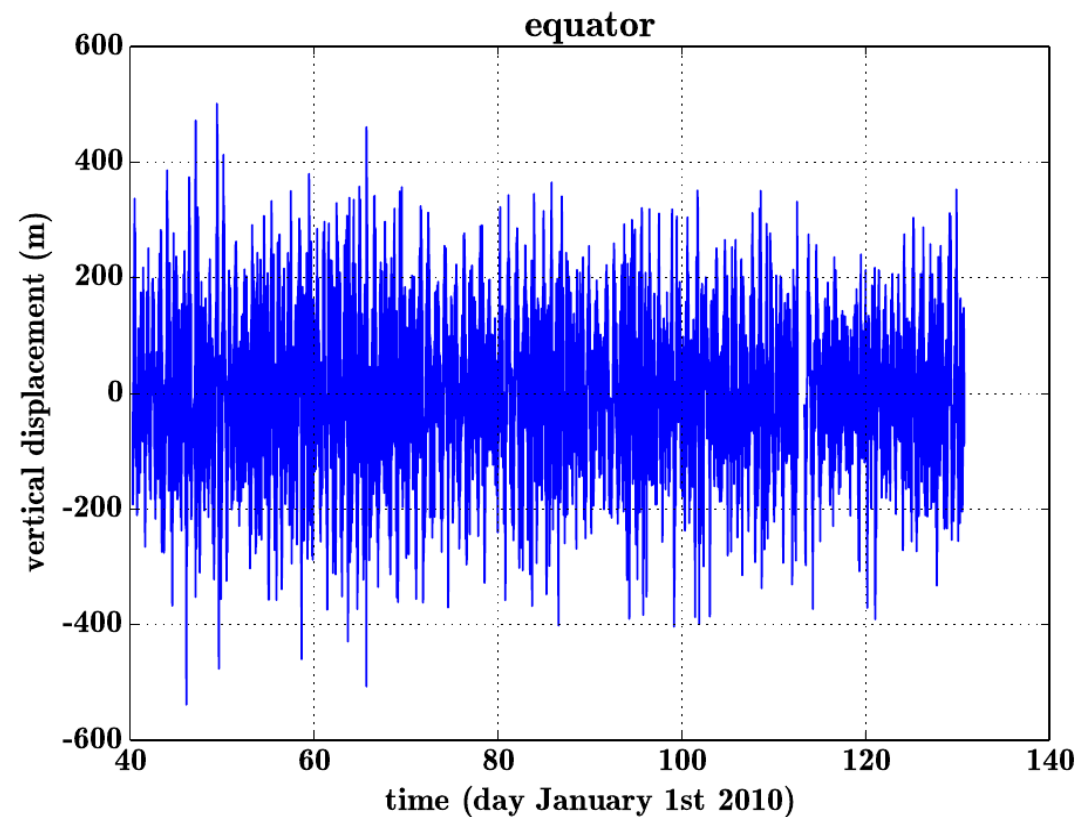
$$T'_l = -\frac{g}{C_p} \zeta'_\theta$$

$$T_l'^2 = 2 \left( \frac{g}{C_p N} \right)^2 E_p$$

Lagrangian cooling rates :  $\frac{DT'_l}{Dt} = -\frac{g}{C_p} w'$

# Temperature fluctuations in the equatorial LS are Gaussian, limited intermittency

## Temperature PDF

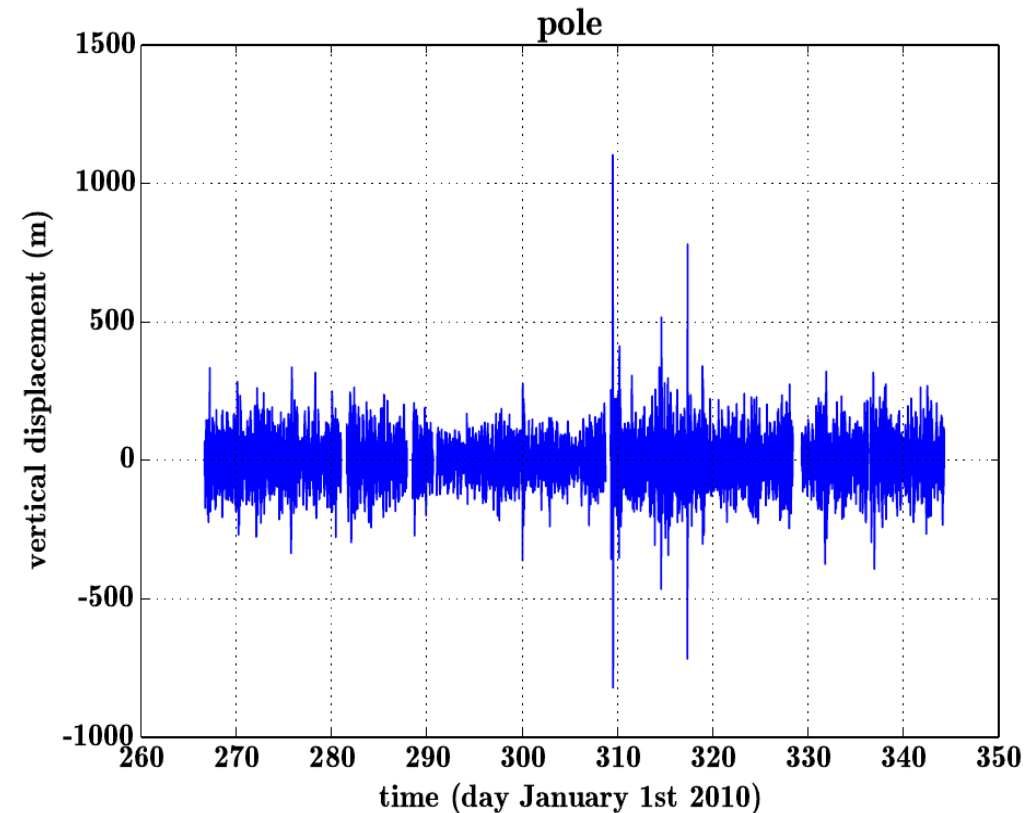
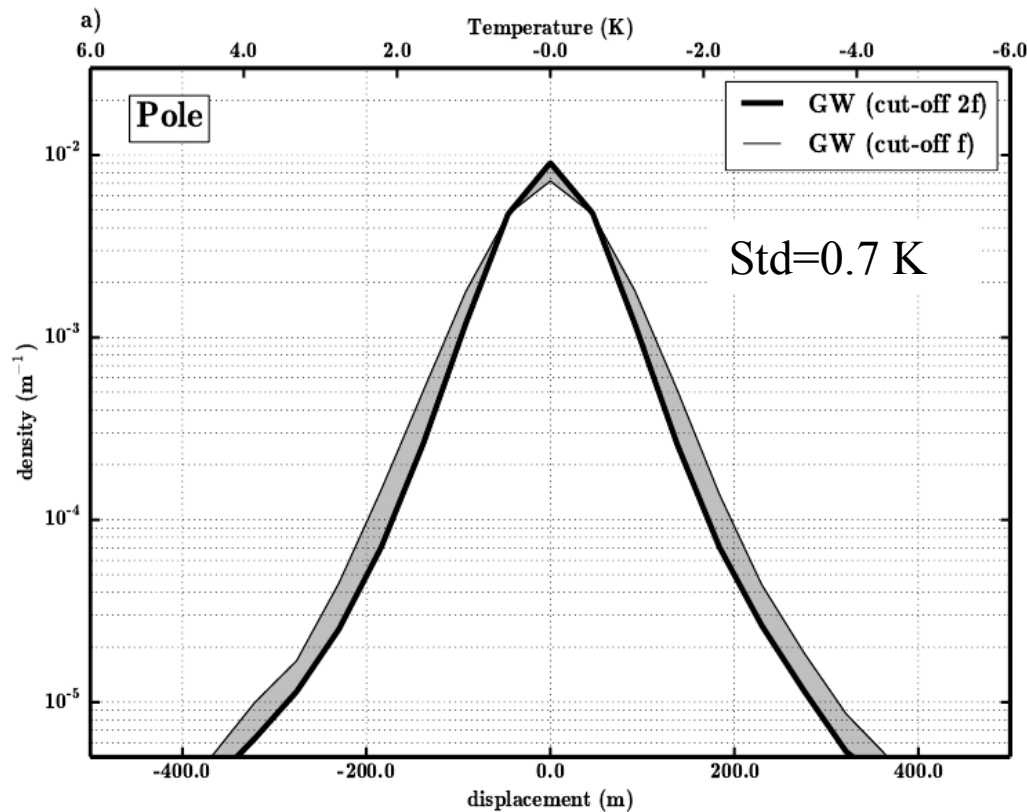


Important contribution of the gravity waves to the temperature variability  
**Gaussian PDF over the equator**



# Temperature fluctuations in the polar LS have large wings are more intermittent

## Temperature PDF



Important contribution of the gravity waves to the temperature variability

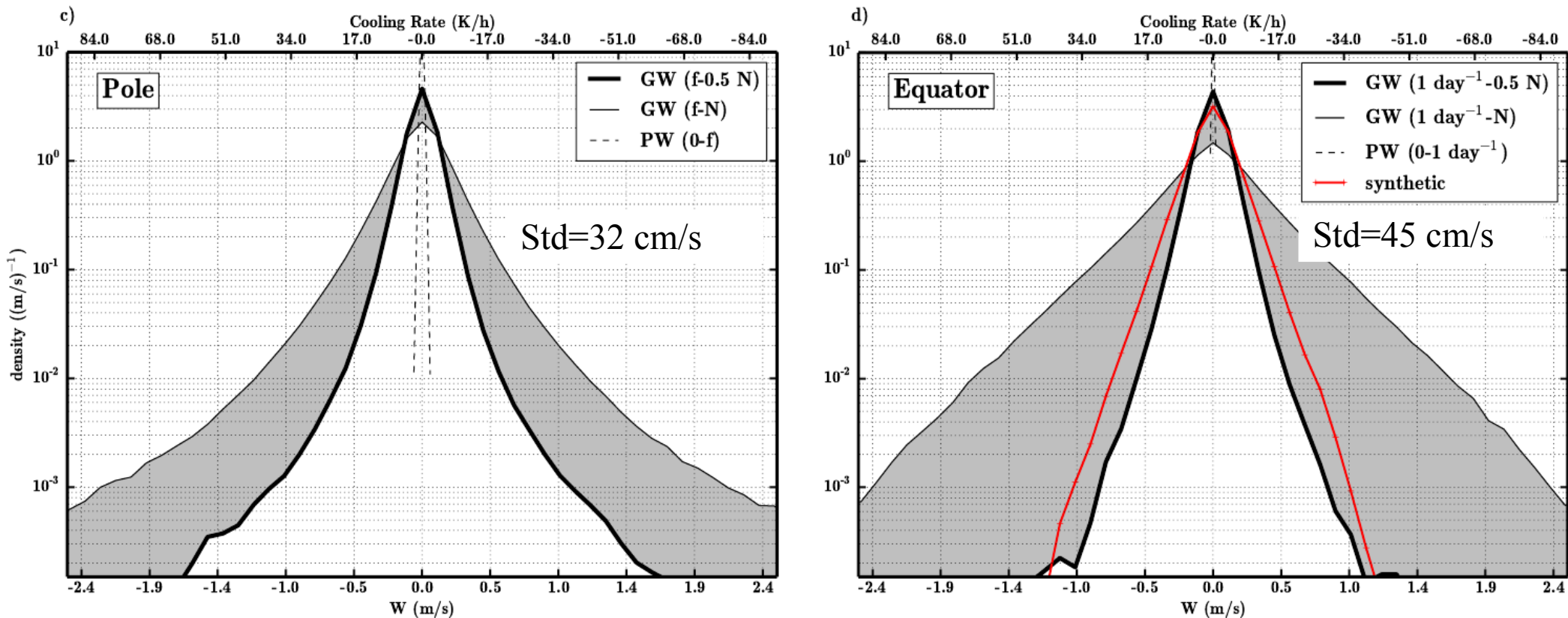
**Gaussian PDF over the equator, non Gaussian PDF over the pole**

Larger contribution of the wings to the variance in the polar flights.

Linked to intermittency in the GW field

# Vertical velocity/cooling rates are non Gaussian (intermittent)

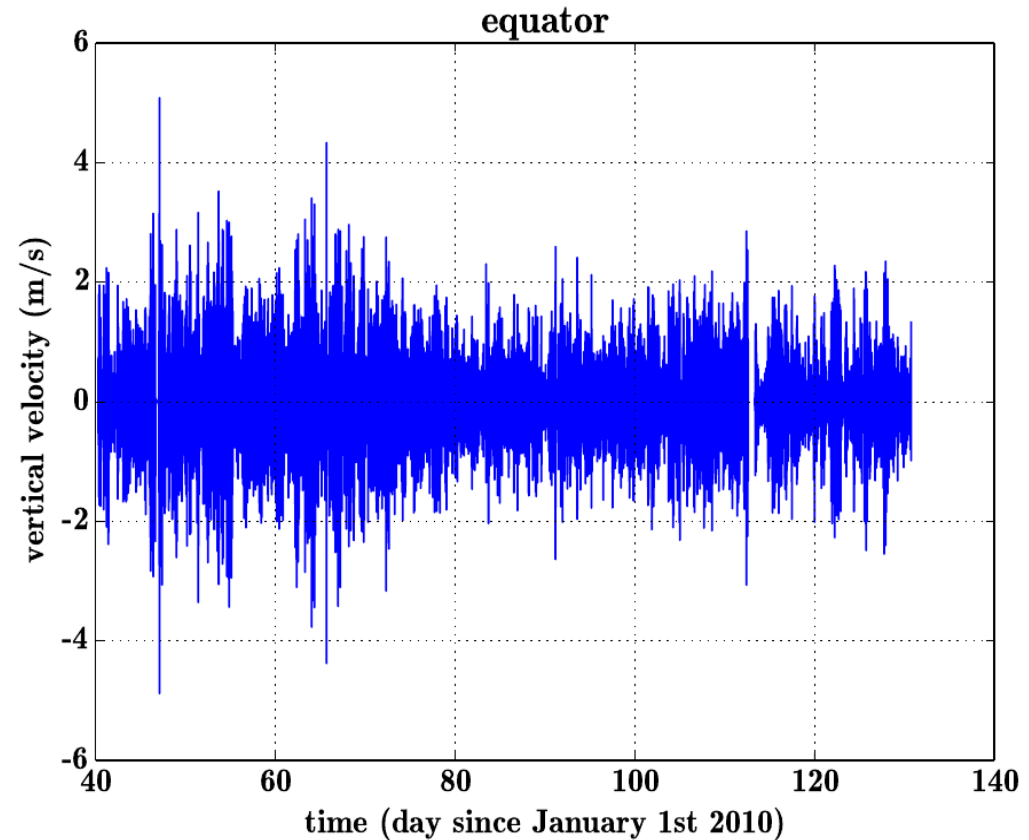
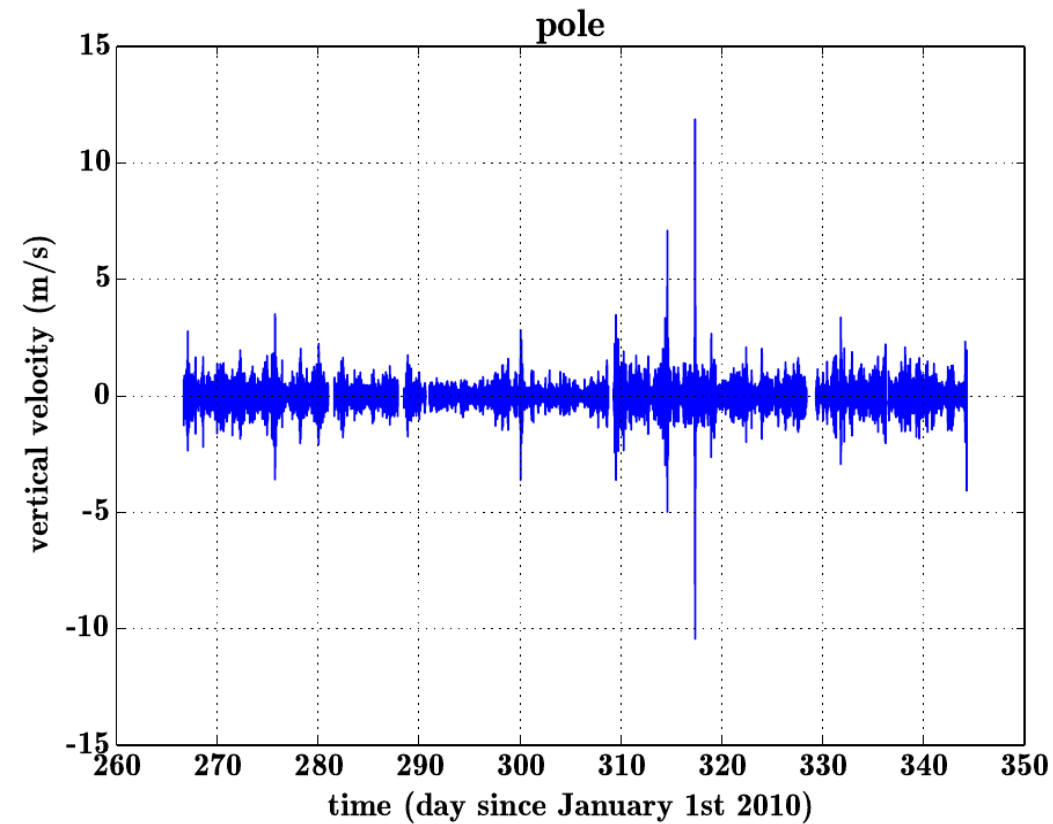
## Vertical velocity/cooling rates PDF



Variability largely dominated by the (very) high frequencies (gravity waves  $\gg$  planetary waves)  
**Non Gaussian PDFs** both over the equator and the pole : intermittent field.  
Larger contribution of the wings to the variance in the Southern Pole flights.



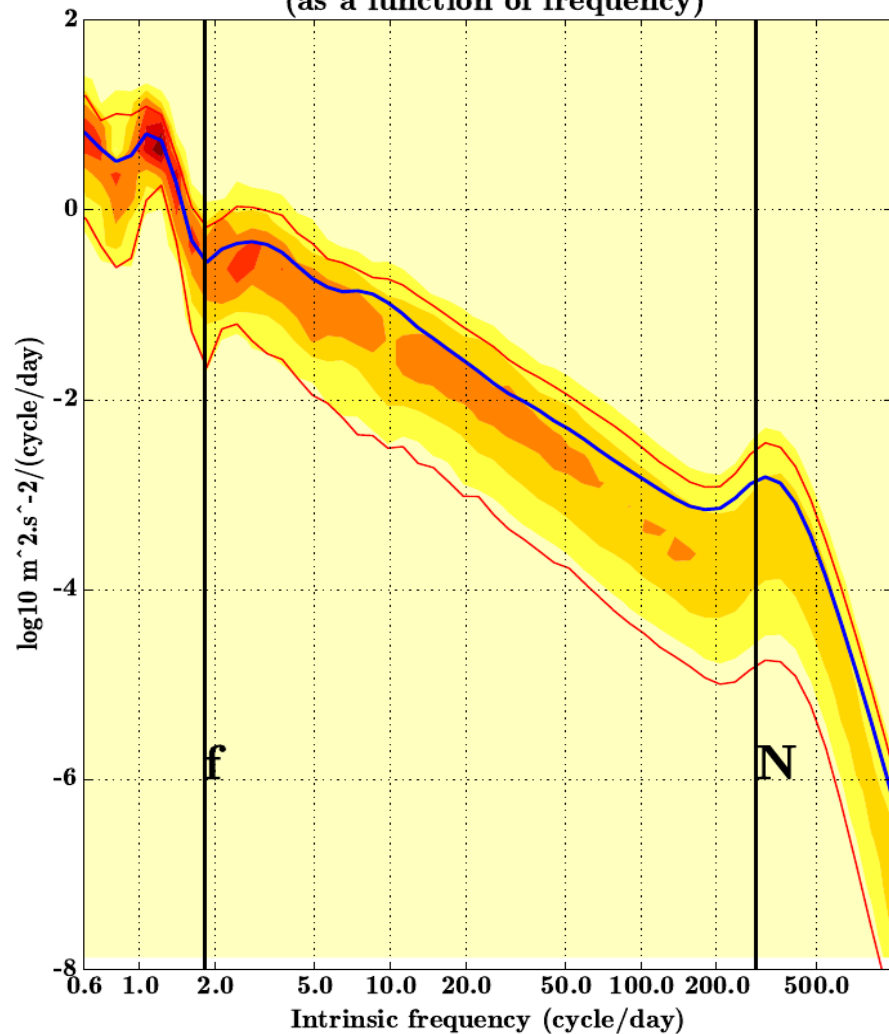
# Intermittency in vertical velocity is weaker in the tropics, stronger over the pole



# Intermittency of temperature fluctuations varies with frequency

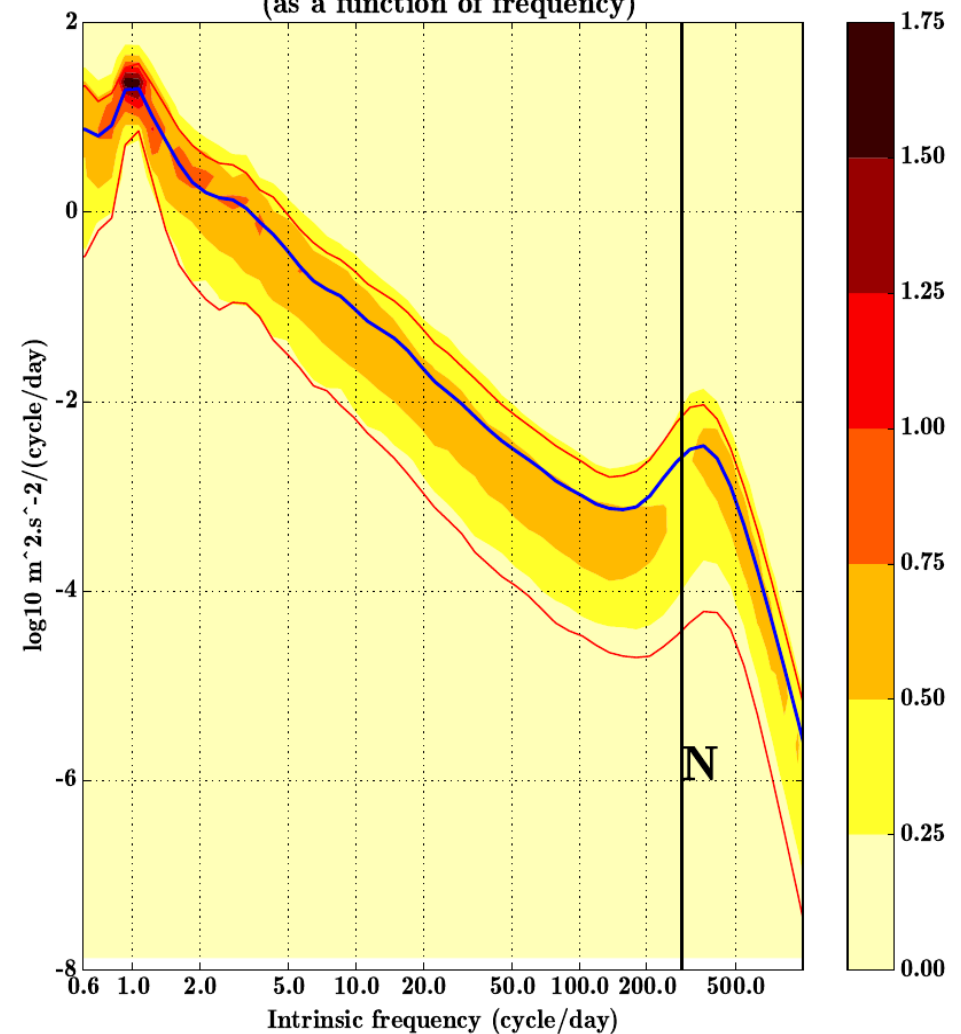
Pole

PDF of wavelet variance  
(as a function of frequency)



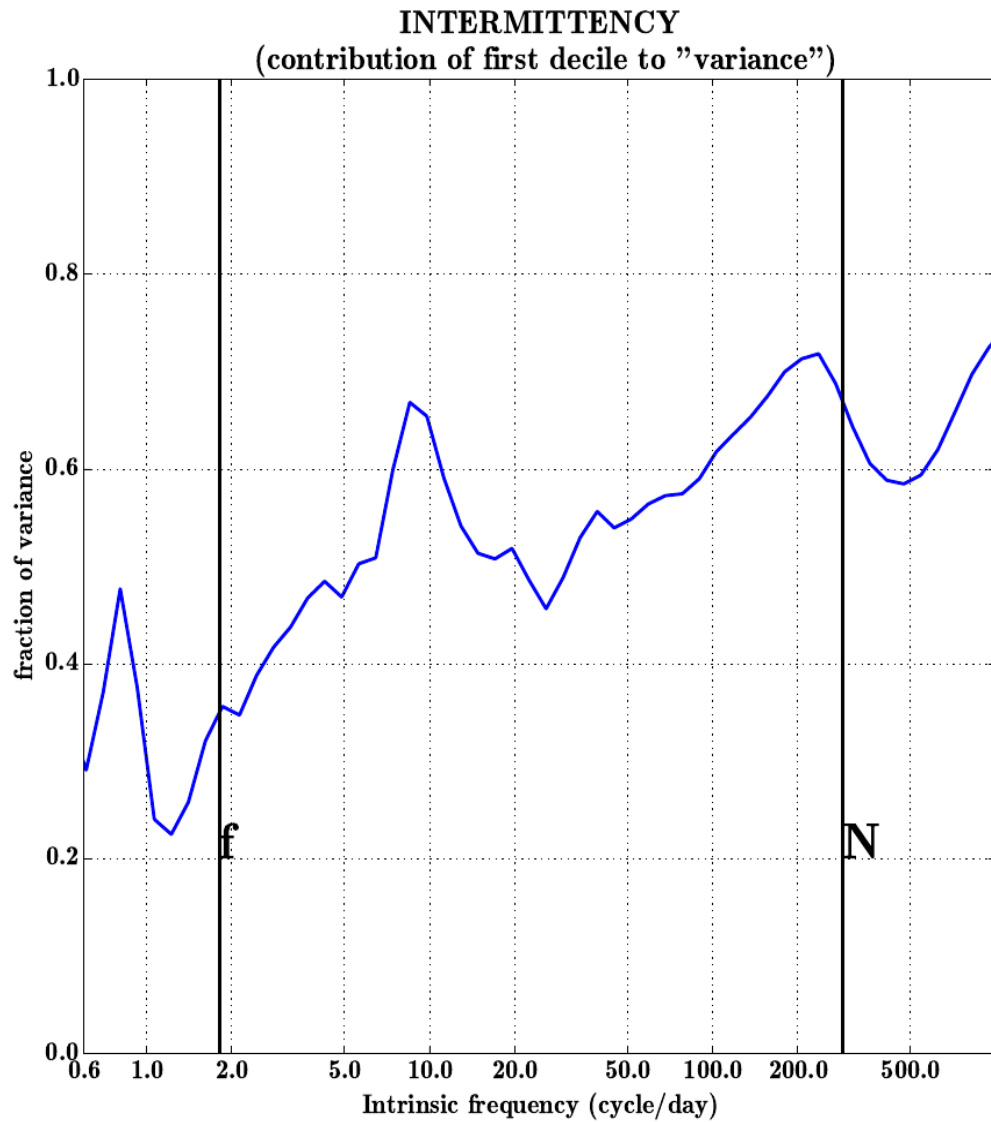
Equator

PDF of wavelet variance  
(as a function of frequency)

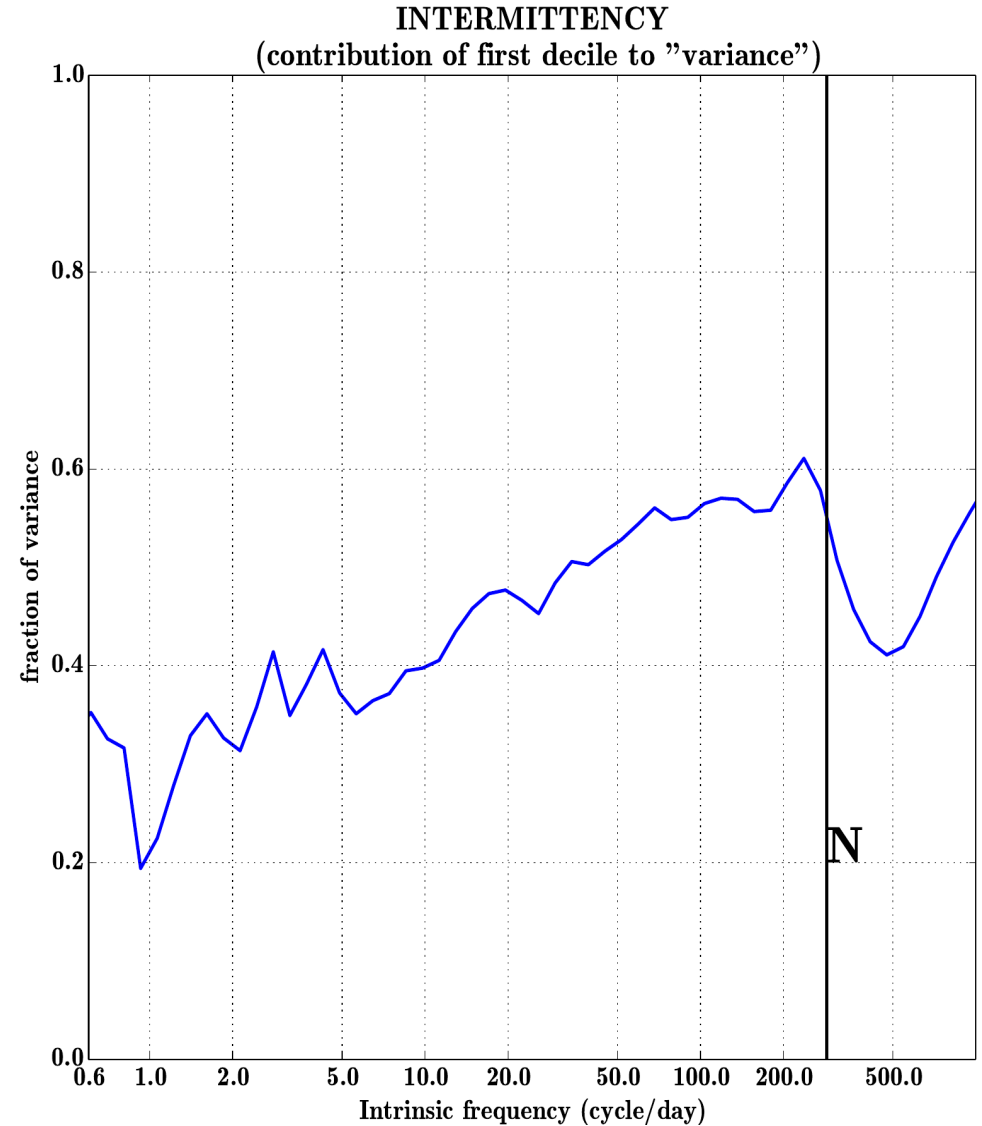


# Intermittency increases with frequency

**Pole**



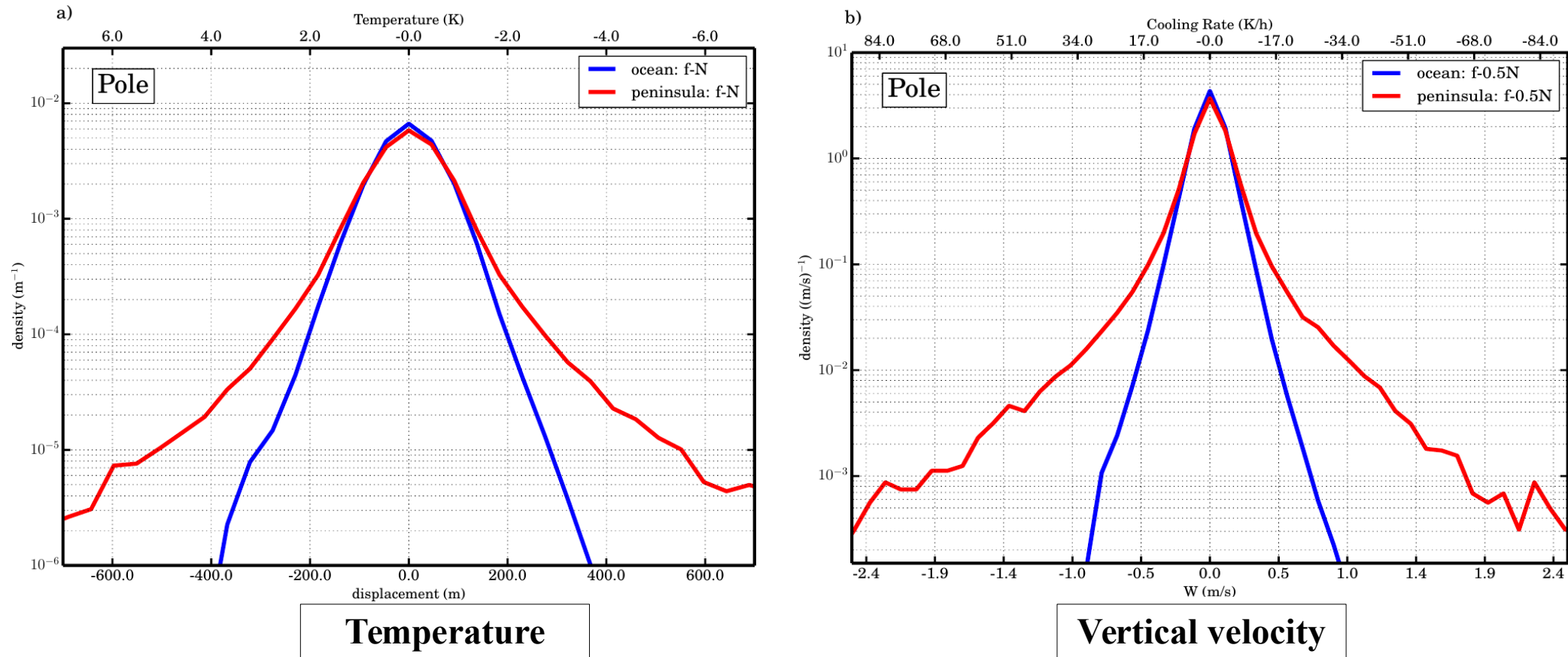
**Equator**





# Large-intermittent T-W excursions over the pole are mainly tied to orography

## Regional contributions over the pole



**Large wings** over the pole are associated with **mountain waves** (regions of high topographic gradients : Antarctic peninsula versus ocean and the flat Antarctic plateau), both for temperature and vertical velocity

# Summary

- Superpressure balloon observations quantify Lagrangian temperature fluctuations
- Those observations confirm the scaling behavior in the mid-frequency range (T perturbations are the strongest at low frequencies, W fluctuations are the strongest at high frequencies )
- They suggest a peak of vertical velocity variance near the buoyancy frequency
- GW induced temperature fluctuations are close to gaussian in the tropics but not over the pole : large tails due to intermittency
- GW vertical velocity fluctuations are non gaussian in both regions
- Intermittency of T fluctuations increases with intrinsic frequency
- AR-1 process reproduce realistic temperature fluctuations in the tropics (simple parameterization)



# Thank you for your attention



## Geophysical Research Letters

### RESEARCH LETTER

10.1002/2016GL068148

#### Key Points:

- Long-duration balloon observations are used to characterize Lagrangian temperature fluctuations
- Intrinsic frequency spectra and PDFs are derived for temperature and cooling rates

## Lagrangian temperature and vertical velocity fluctuations due to gravity waves in the lower stratosphere

**Aurélien Podglajen<sup>1</sup>, Albert Hertzog<sup>2</sup>, Riwal Plougonven<sup>1</sup>, and Bernard Legras<sup>1</sup>**

<sup>1</sup>Laboratoire de Météorologie Dynamique, CNRS-UMR8539, Institut Pierre Simon Laplace, École Normale Supérieure, École polytechnique, Université Pierre et Marie Curie, Paris, France, <sup>2</sup>Laboratoire de Météorologie Dynamique/IPSL, UPMC Univ Paris 06, CNRS, Palaiseau, France



**Backup slides**

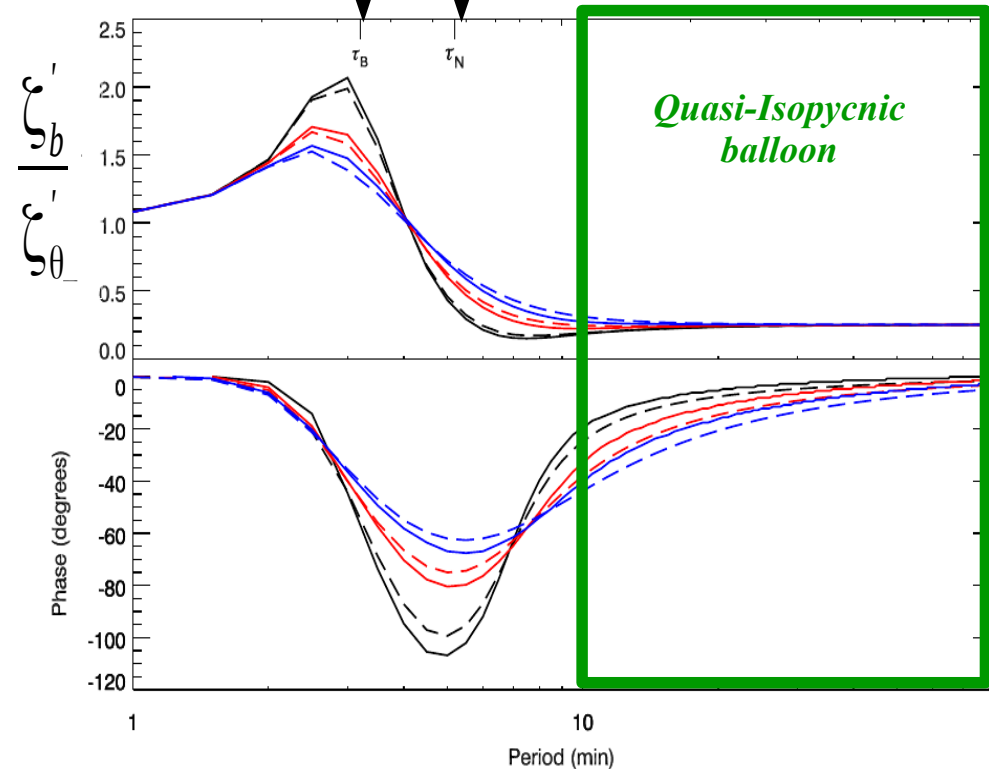
# Balloon response to air motions

However, the balloon is no longer isopycnic at high frequencies, its vertical position  $\zeta'_b$  evolves as :

$$\frac{\partial^2 \zeta'_b}{\partial t^2} = -\omega_B^2 \zeta'_b + \frac{2}{3} g R - A \left( \frac{\partial \zeta'_b}{\partial t} - w' \right) \left| \frac{\partial \zeta'_b}{\partial t} - w' \right| + \frac{\partial w'}{\partial t}$$

*Balloon neutral  
oscillations  
period*

*Brunt-Väisälä  
period*



Numerical simulations of the balloon response to harmonic “atmospheric” oscillations :

Amplitude and phase response

*Vincent and  
Hertzog, 2014*

# Balloon response to air motions

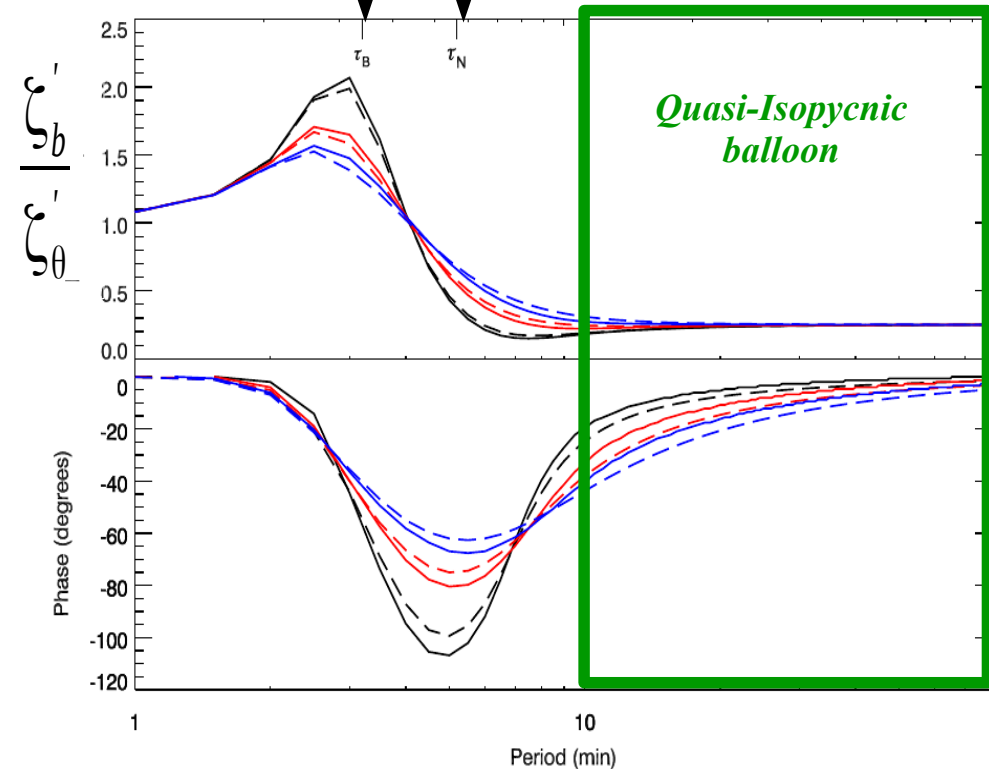
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*Balloon neutral  
oscillations  
period*

*Brunt-Väisälä  
period*

Isopycnic  
behavior:  $0 = -\omega_B^2 \zeta'_b + \frac{2}{3}gR$



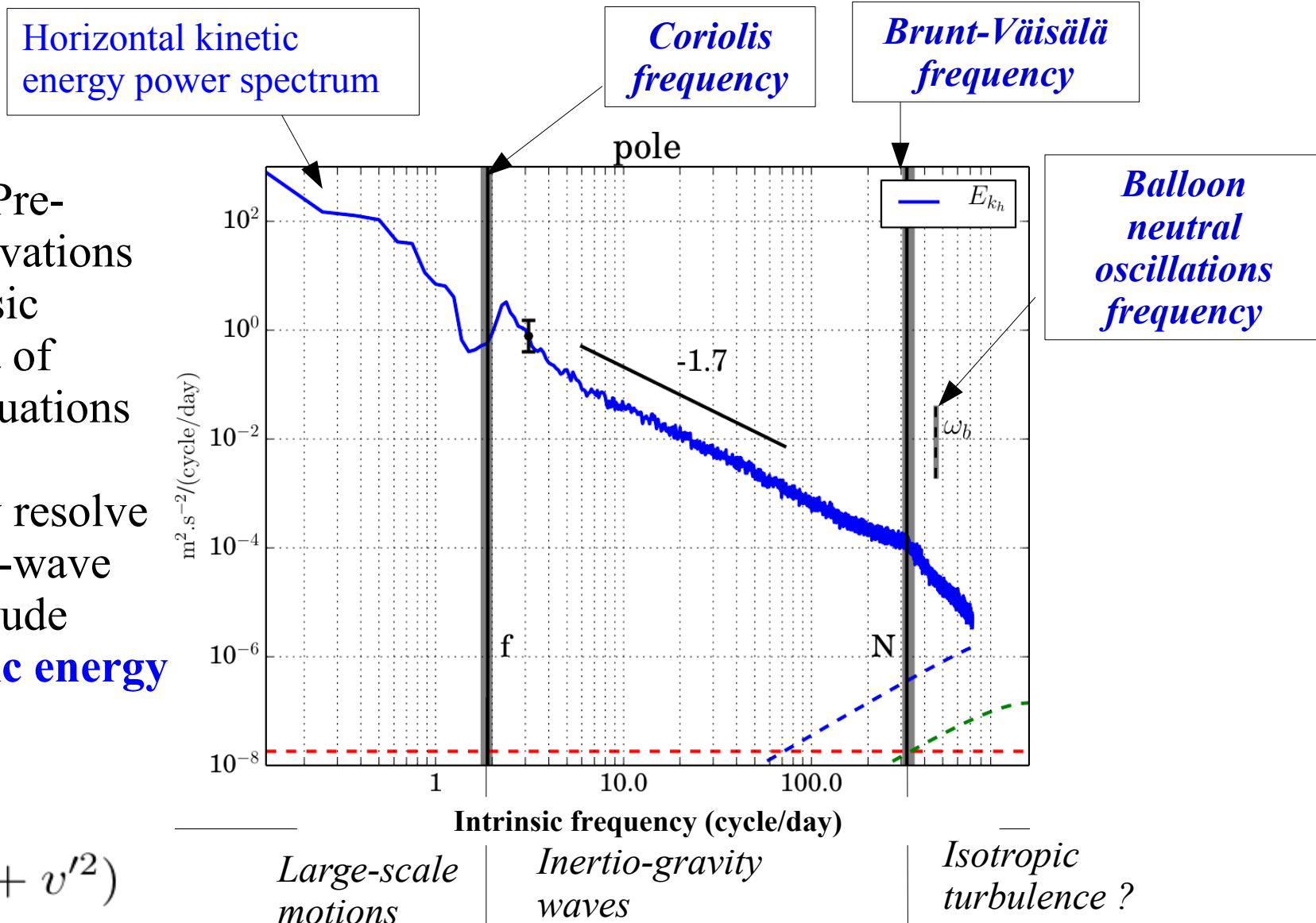


# Balloon observations resolve the whole GW spectrum

Concordiasi and Pre-concordiasi observations resolve the intrinsic frequency spectra of atmospheric fluctuations

In particular, they resolve the whole gravity-wave subrange and include **horizontal kinetic energy spectra**

$$E_{kh} = \frac{1}{2}(u'^2 + v'^2)$$



# Variance at the Brunt-Väisälä

Strong enhancement in potential and vertical kinetic energy power spectra at the Brunt-Vaisala frequency (trapped-near reflection waves)

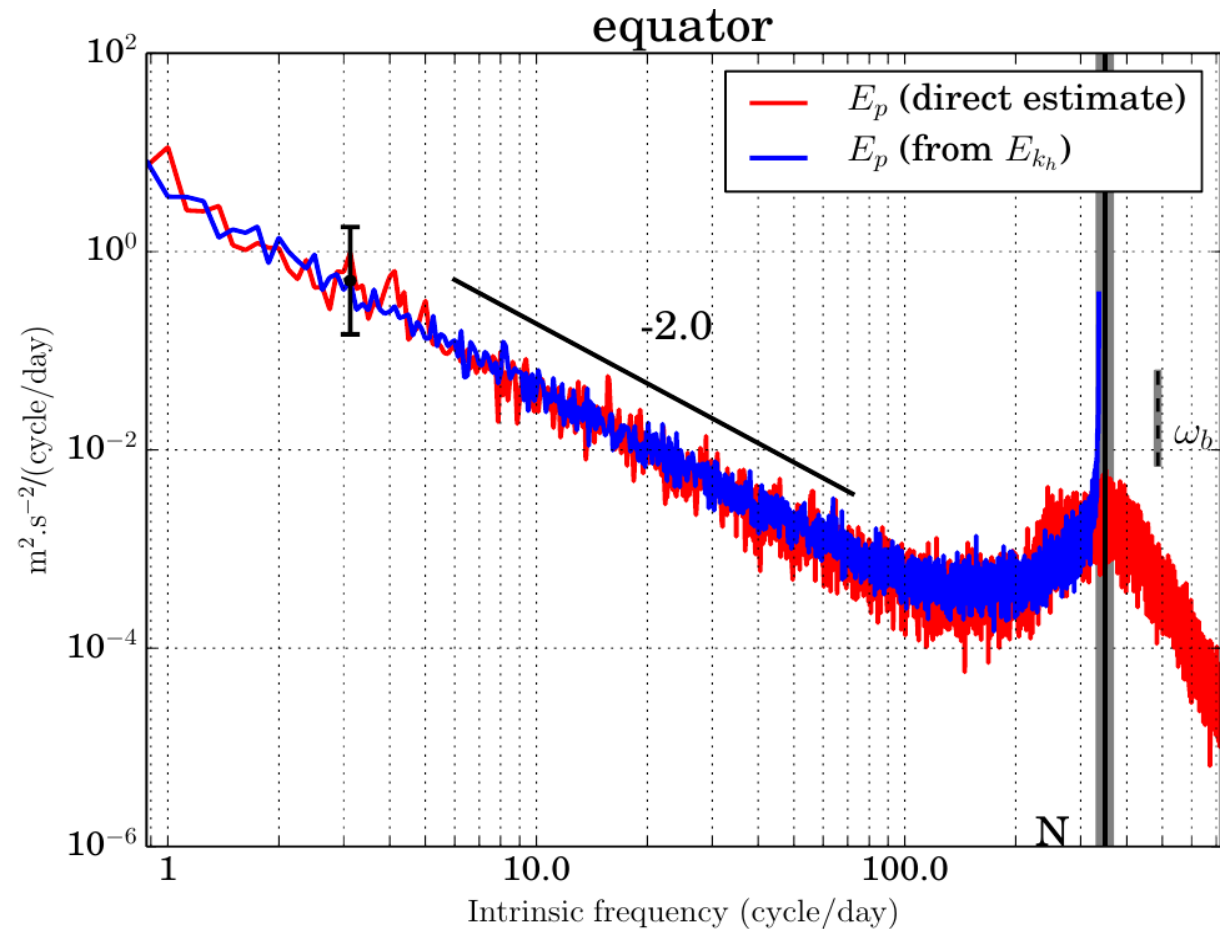
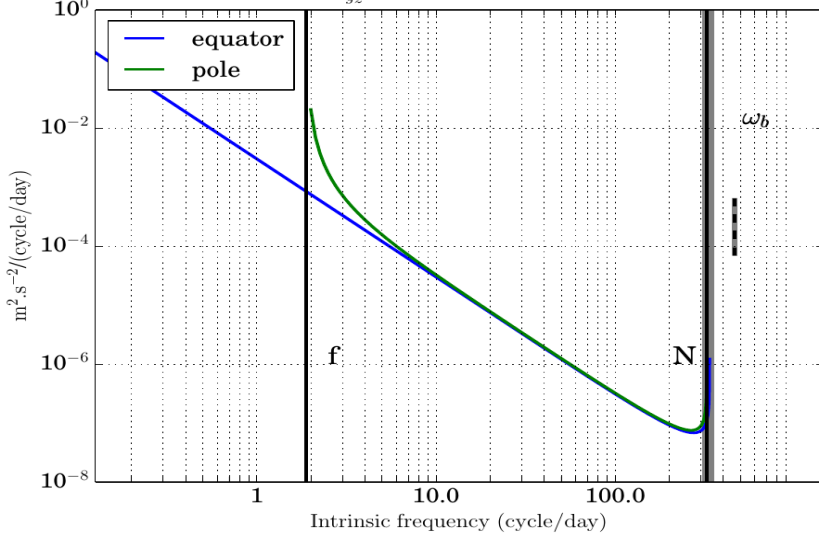
Artifact of balloon observations? (non isopycnic balloon response)? Maybe but

Potential energy

$$E_p = \left( \frac{N^2}{N^2 - \hat{\omega}^2} \right) \left( \frac{\hat{\omega}^2 - f^2}{\hat{\omega}^2 + f^2} \right) E_{kh}$$

Horizontal kinetic energy

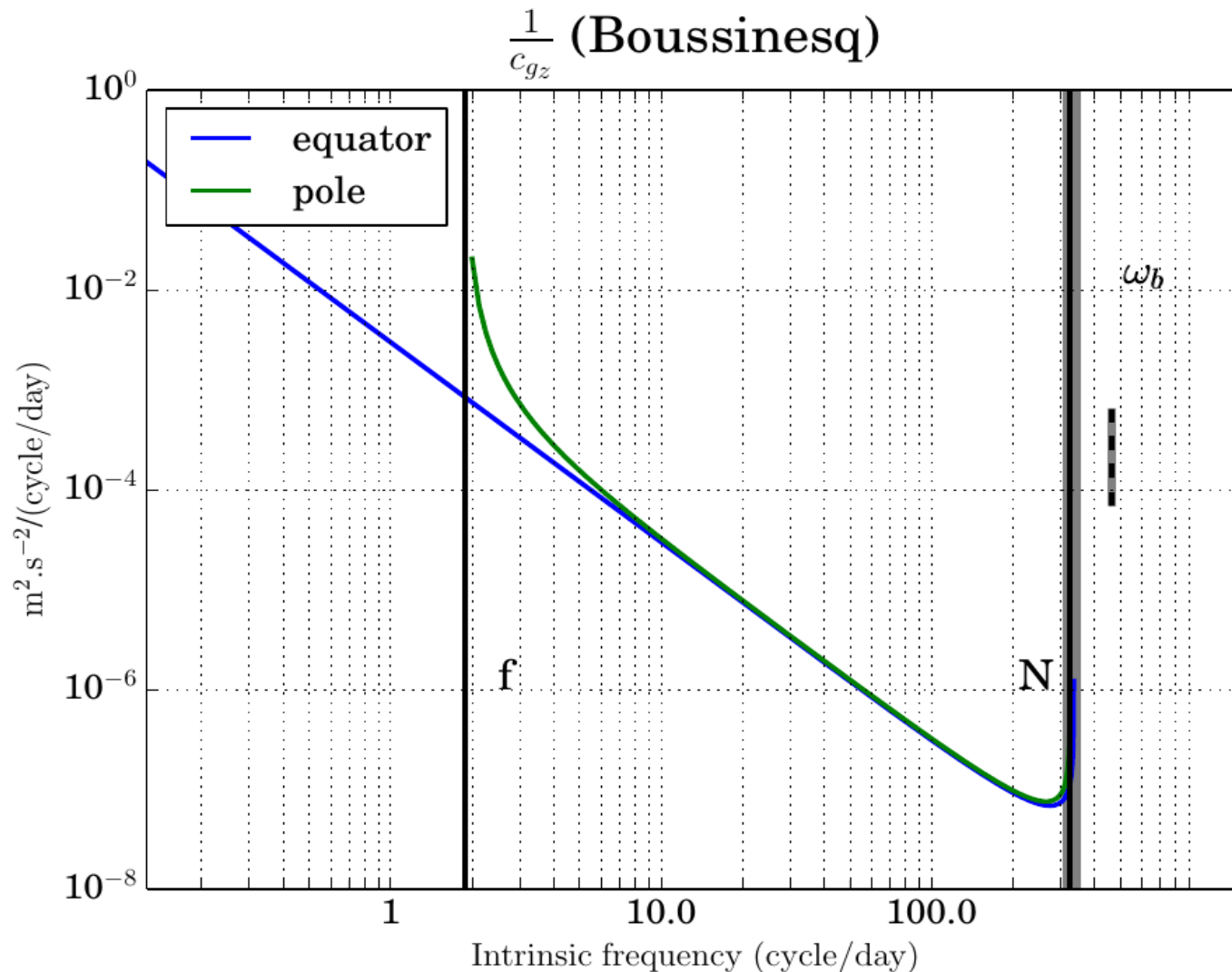
$\frac{1}{c_{gz}}$  (Boussinesq)



# Variance at the Brunt-Väisälä

Strong enhancement in potential and vertical kinetic energy power spectra at the Brunt-Vaisala frequency (trapped-near reflection waves)

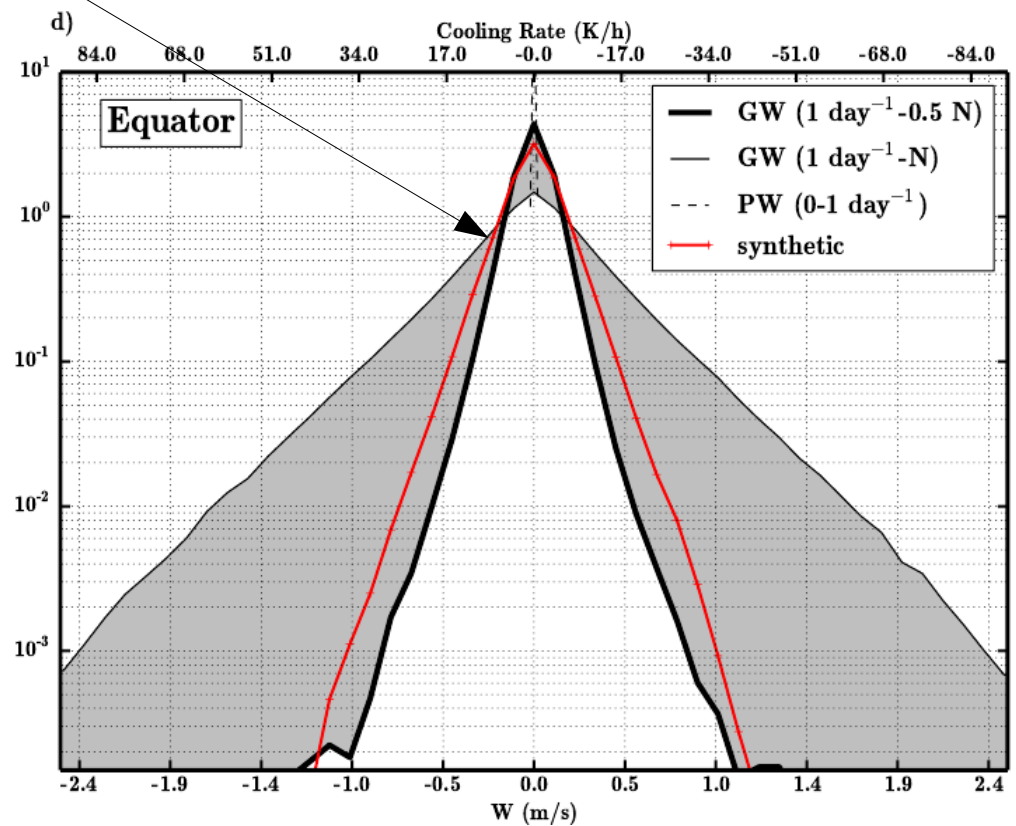
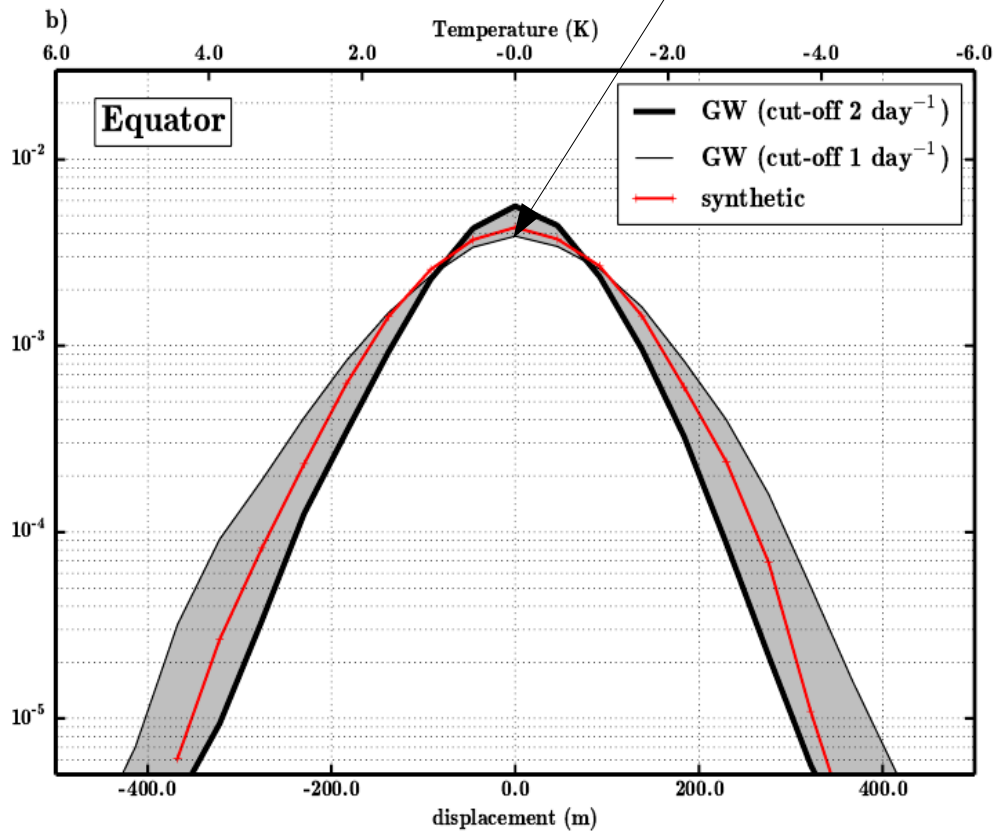
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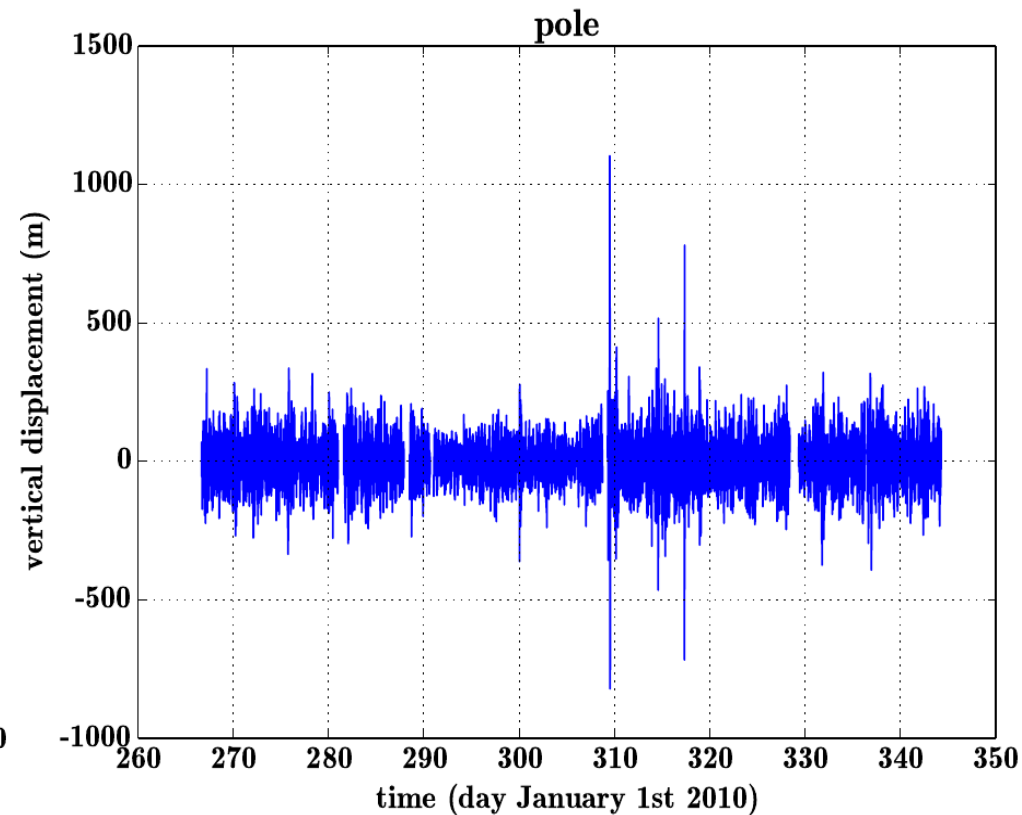
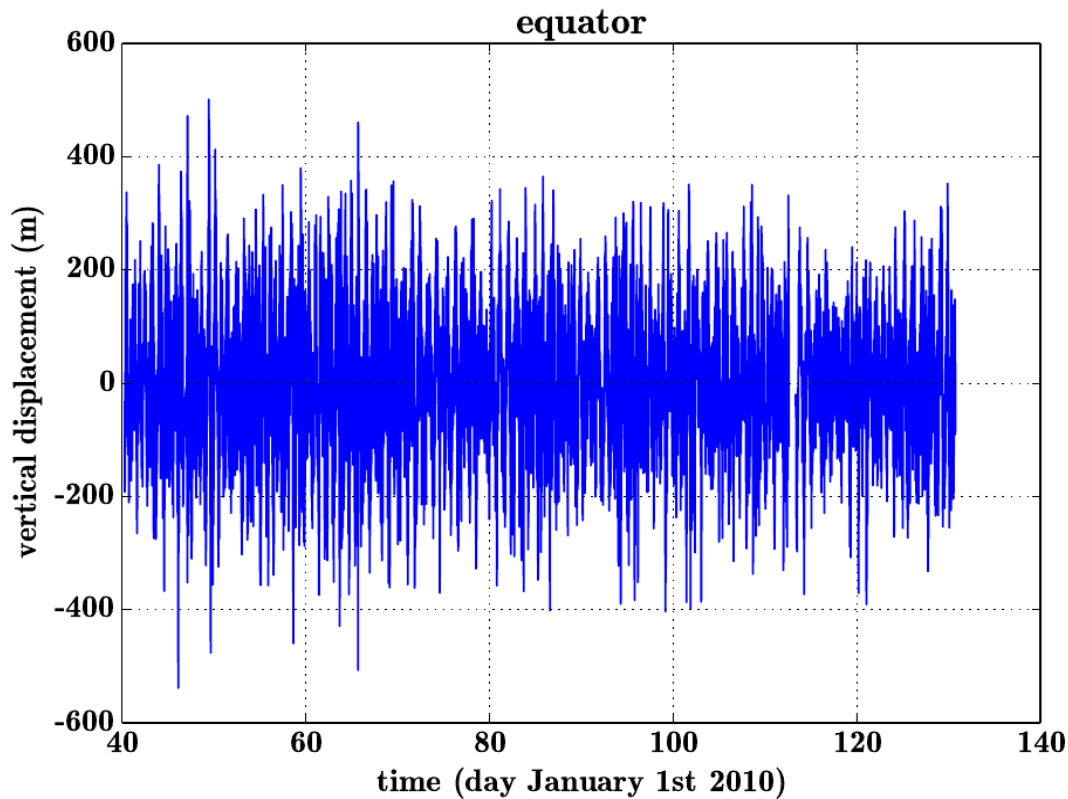
# Synthetic Lagrangian temperature time series

PDF of synthetic temperature and cooling rates time series



# Temperature fluctuations : Equator vs pole

Temperature  
PDF



Vertical displacement

Important contribution of the gravity waves to the temperature variability

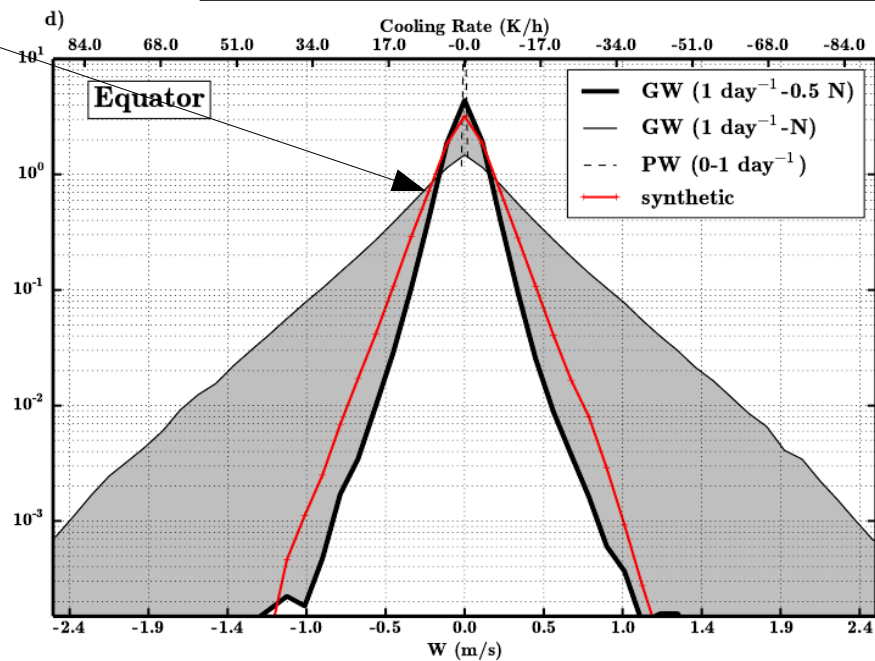
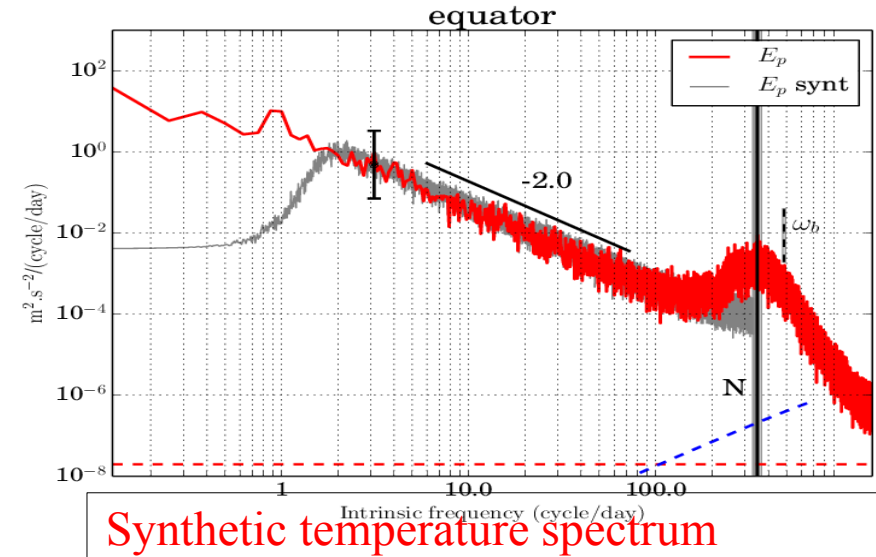
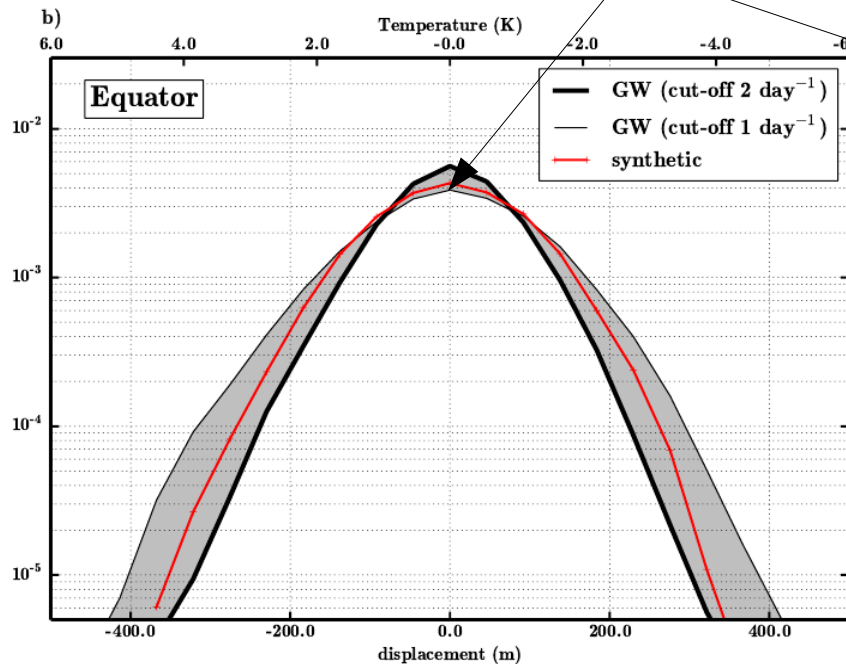
**Gaussian PDF over the equator, non Gaussian PDF over the pole**

Larger contribution of the wings to the variance in the polar flights.

# Synthetic AR-1 processes allow to reproduce realistic time series of Lagrangian T-fluctuations

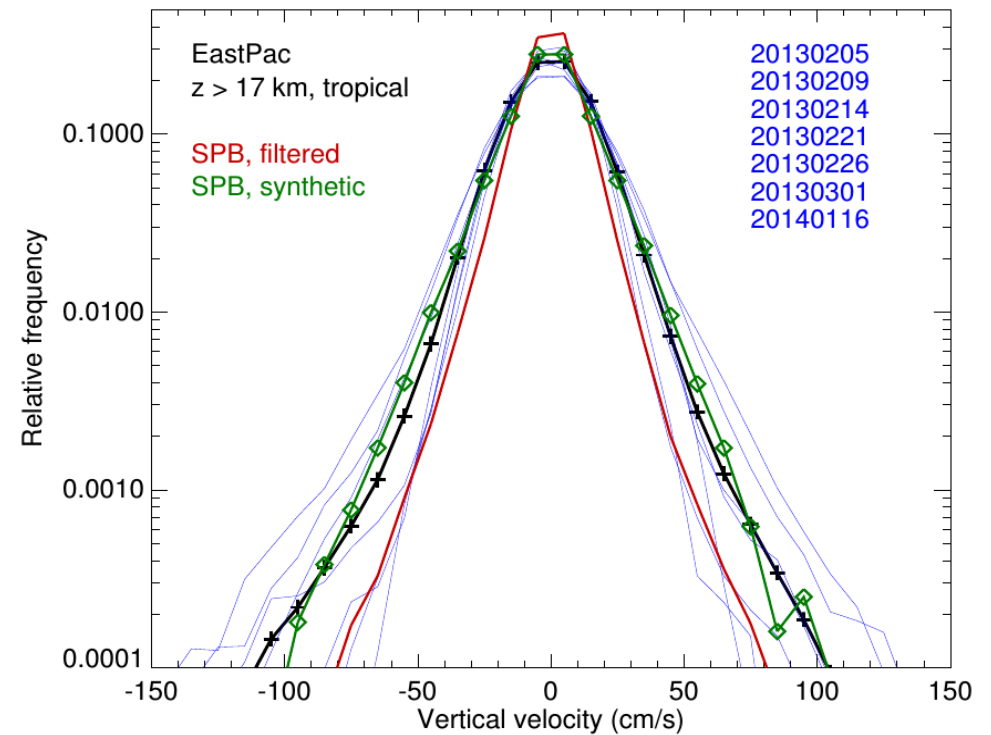
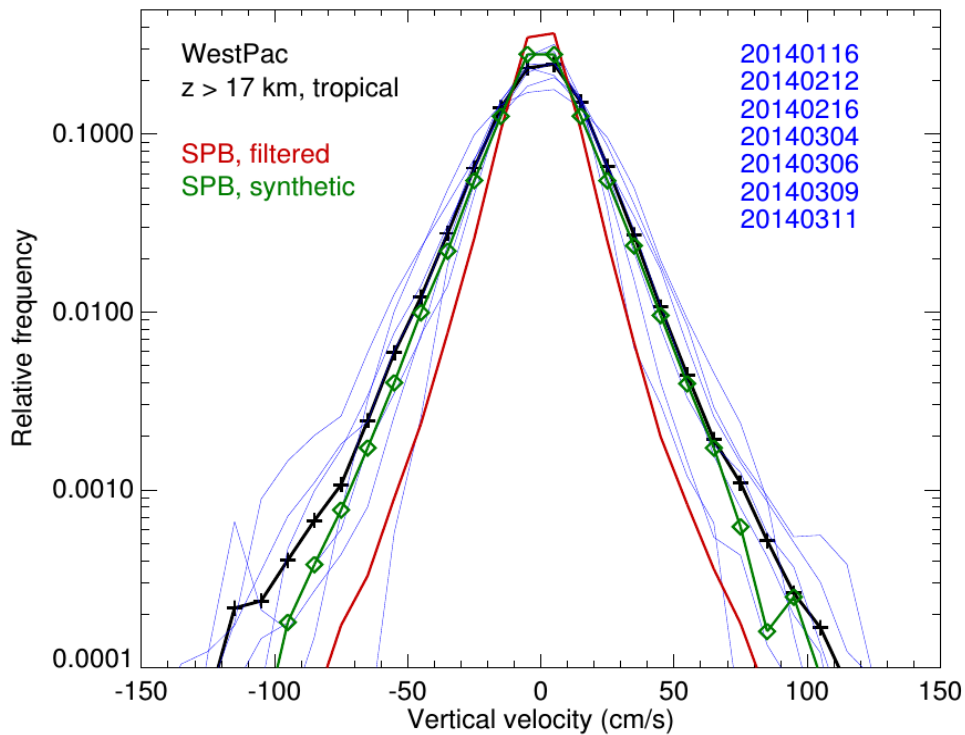
$$\zeta'_{t+dt} = \zeta'_t + W \cdot dt$$

PDF of synthetic temperature and cooling rates time series



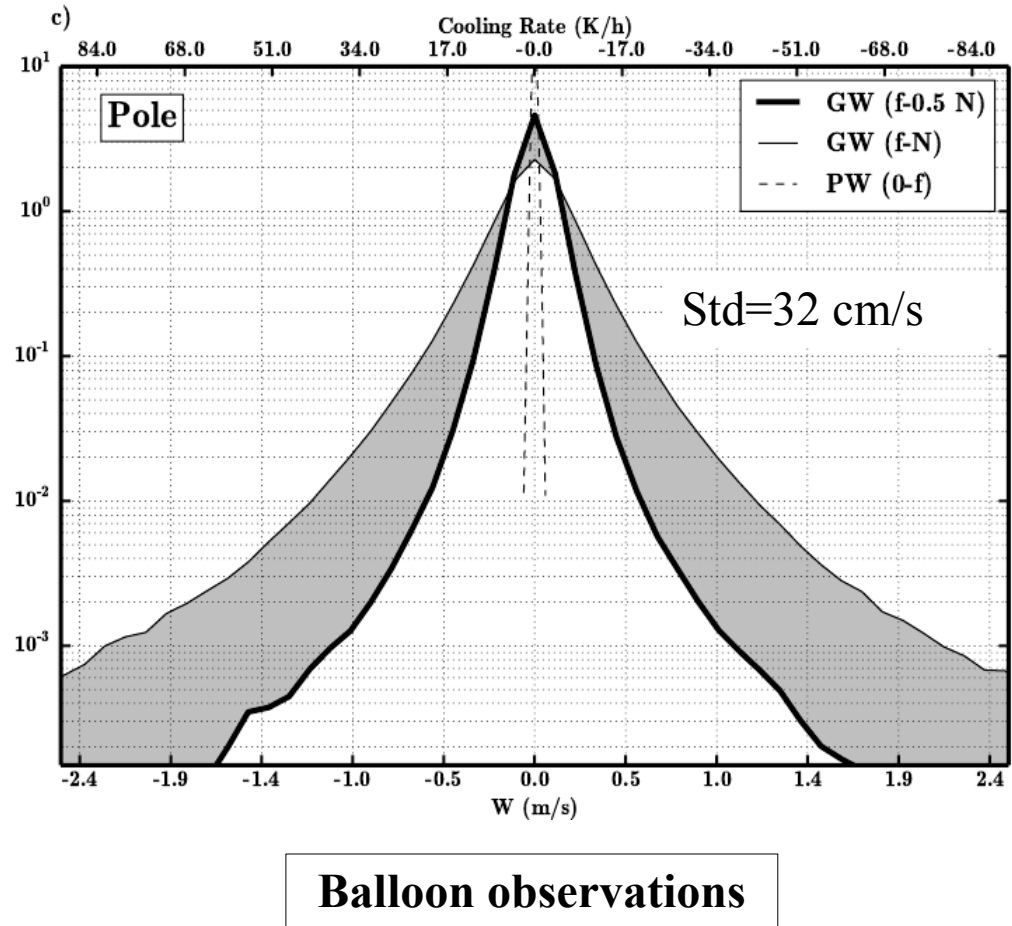
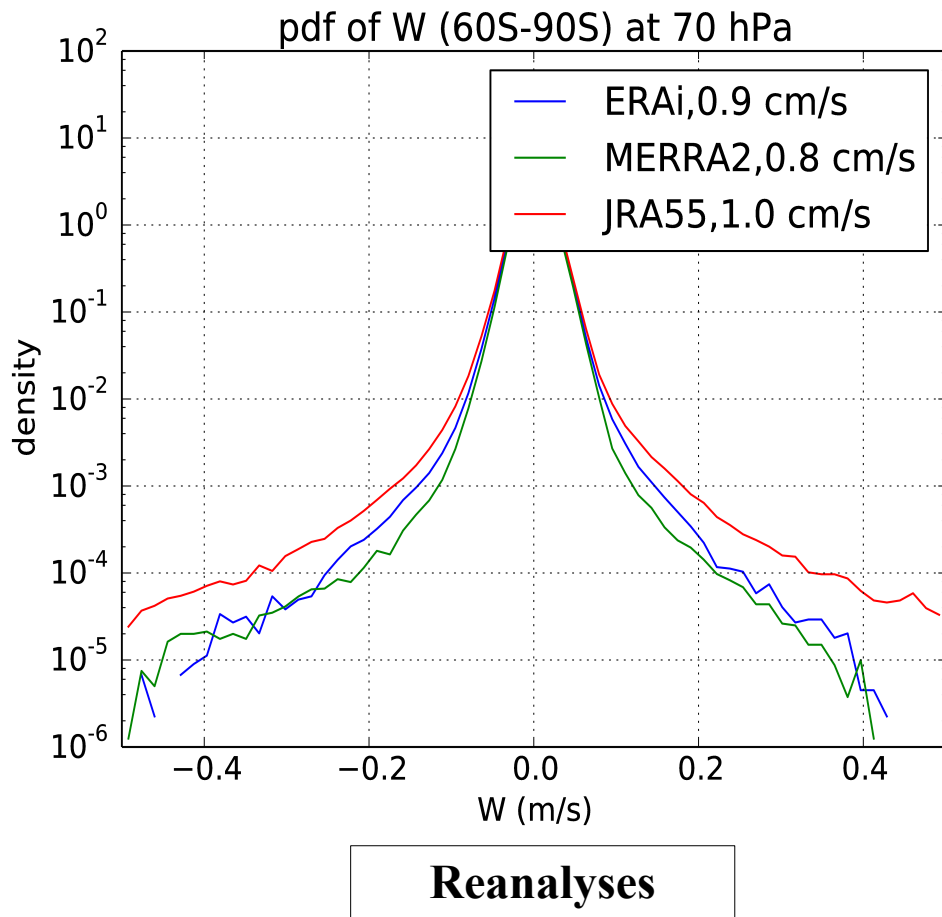
# Synthetic Lagrangian temperature time series

Satisfactory agreement with ATTREX MMS data for the deep tropics



*Jensen et al.* , submitted to GRL

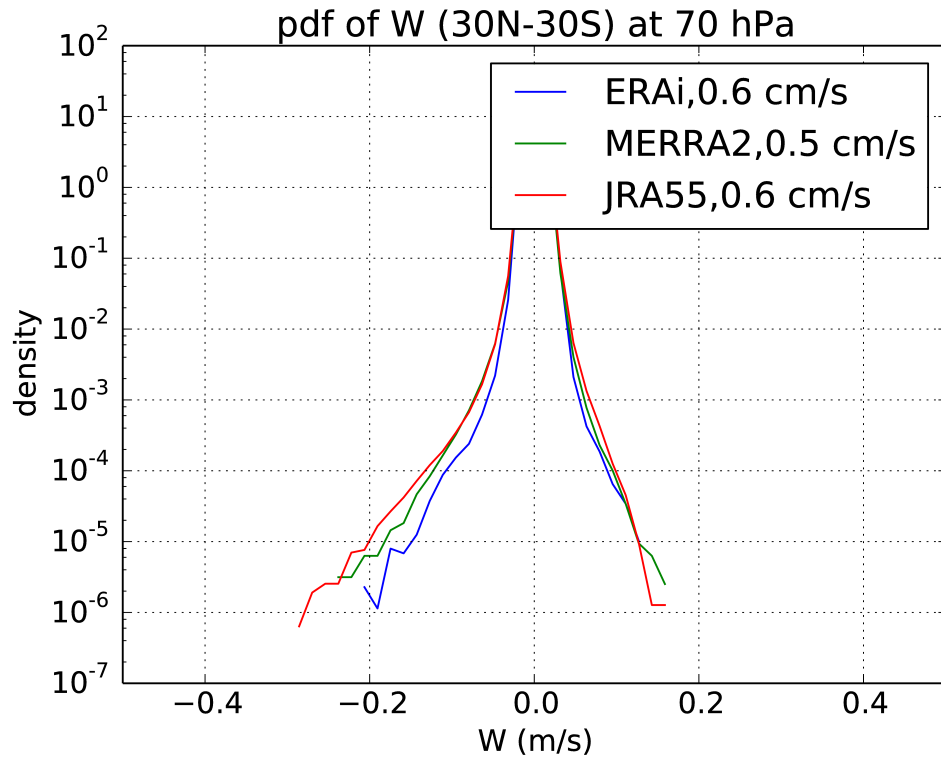
# Vertical velocity in reanalyses



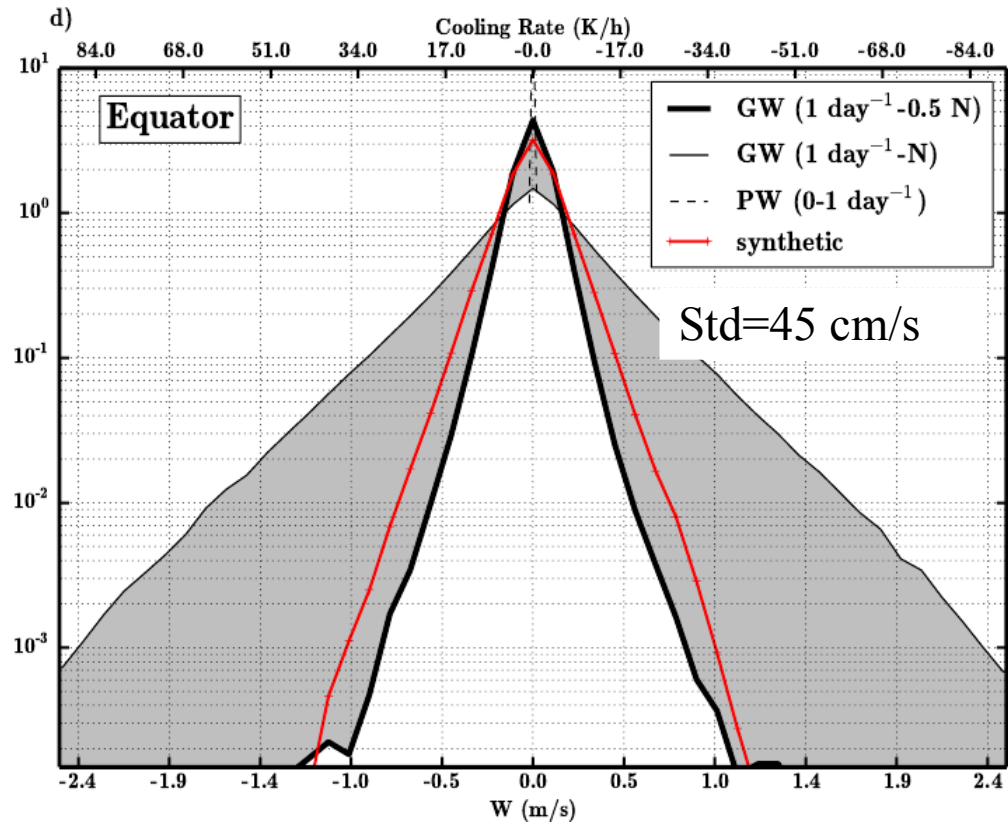
Strong underestimation of the vertical velocity in the tropics in modern reanalyses, comparable shapes



# Vertical velocity in reanalyses



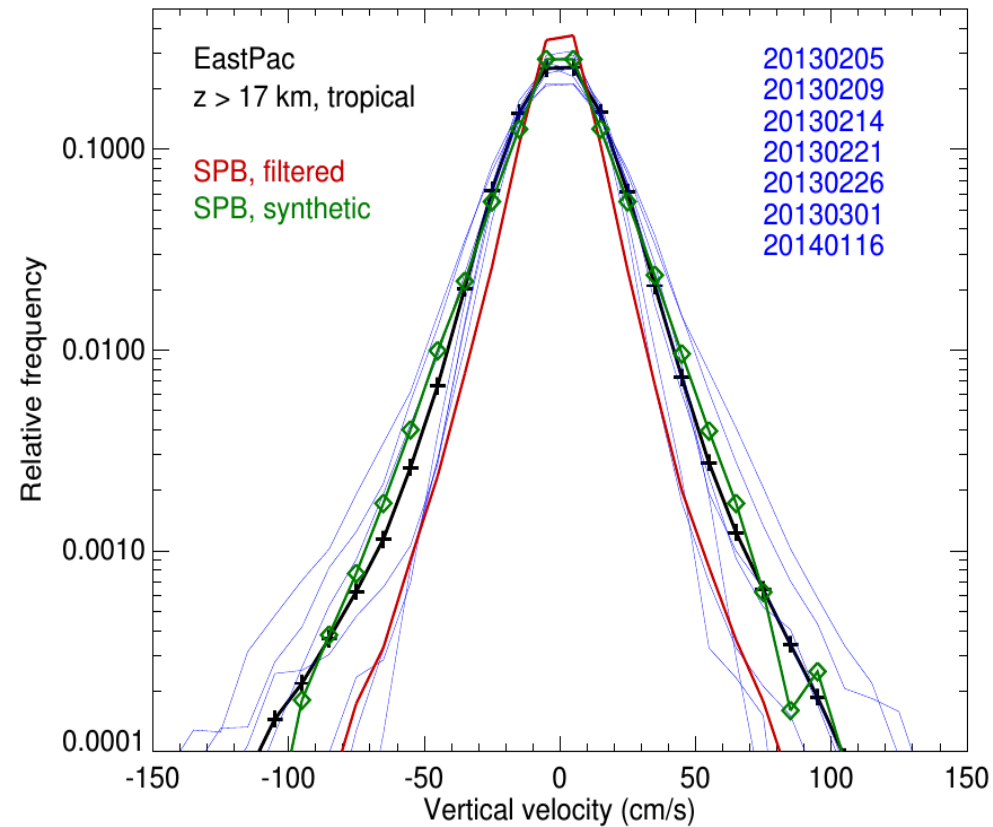
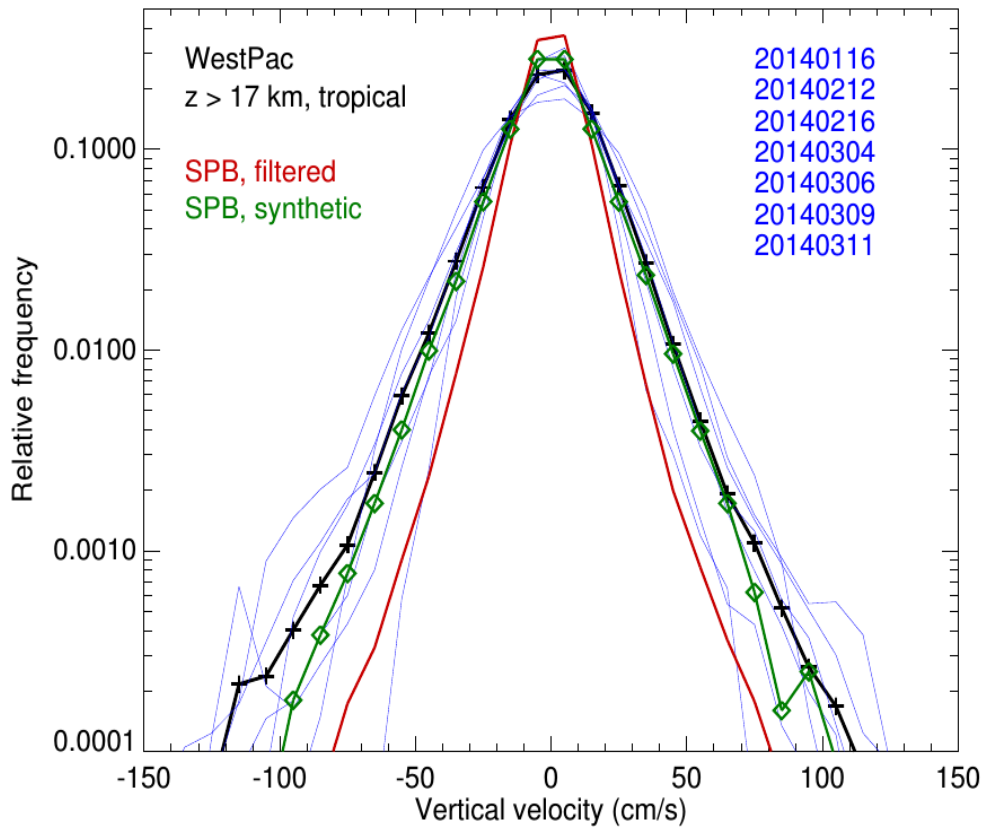
**Reanalyses**



**Balloon observations**

Strong underestimation of the vertical velocity in the tropics in modern reanalyses, comparable shapes

# The distribution of vertical velocity in the tropical lower stratosphere agrees between the balloon and aircraft observations



*Jensen et al.* , in revision for GRL

# Lagrangian temperature vs Eulerian temperature fluctuations

Eulerian and Lagrangian temperature fluctuations are both due to the vertical displacement  $\zeta_\theta$  of air parcels, for different reasons:

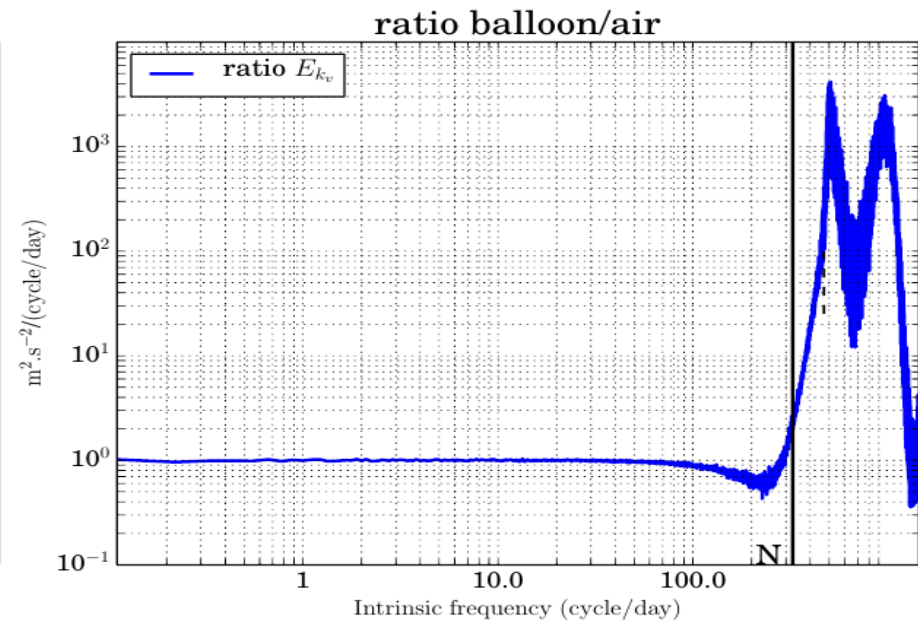
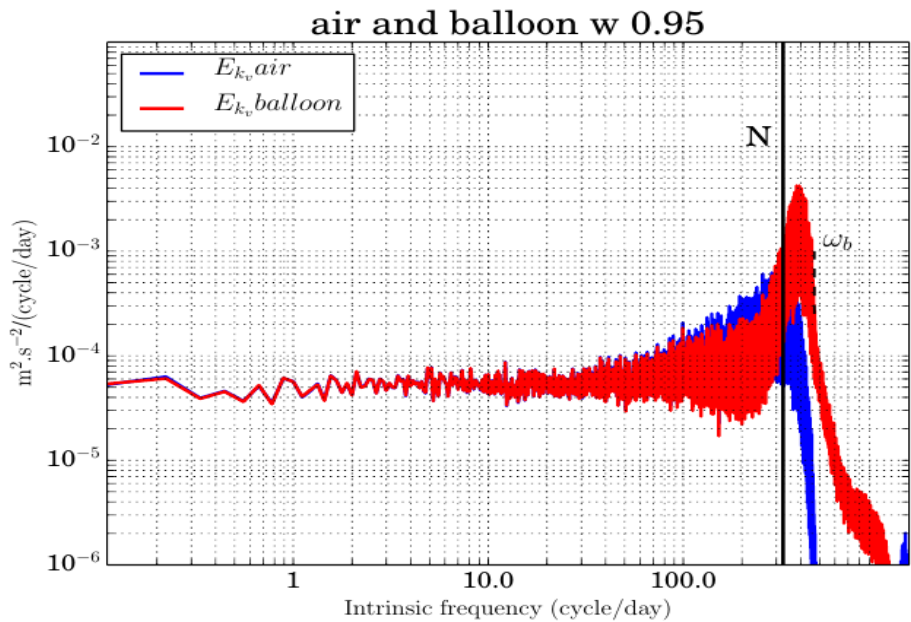
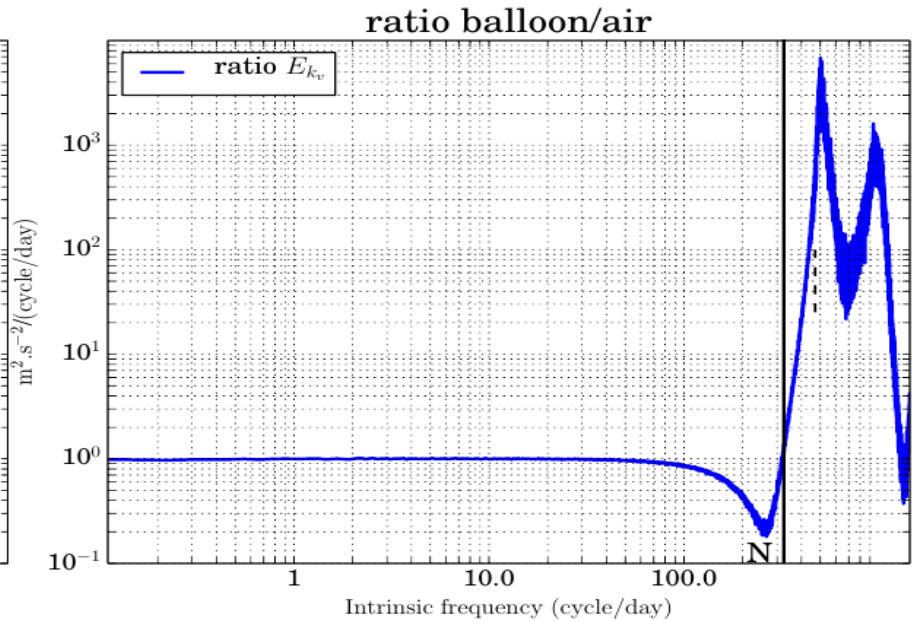
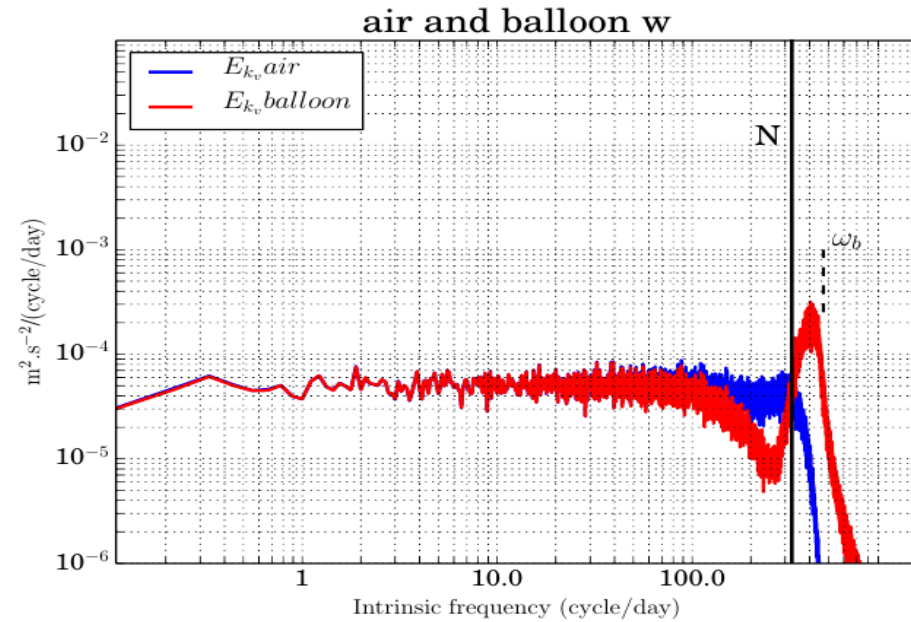
The Lagrangian temperature fluctuations are mainly due to adiabatic expansion :

$$T'_l = -\frac{g}{C_P} \zeta_\theta$$

While the Eulerian ones are due to vertical advection in a stable (non isentropic,  $N^2 > 0$ )

$$T'_l = T' + \zeta_\theta \frac{d\bar{T}}{dz}$$
$$T' = -\zeta_\theta \left( \frac{g}{C_P} + \frac{d\bar{T}}{dz} \right) = \frac{C_P}{g^2} \bar{T} N^2 T'_l$$

# Balloon response to air motions and variance at the Brunt Vaisala frequency

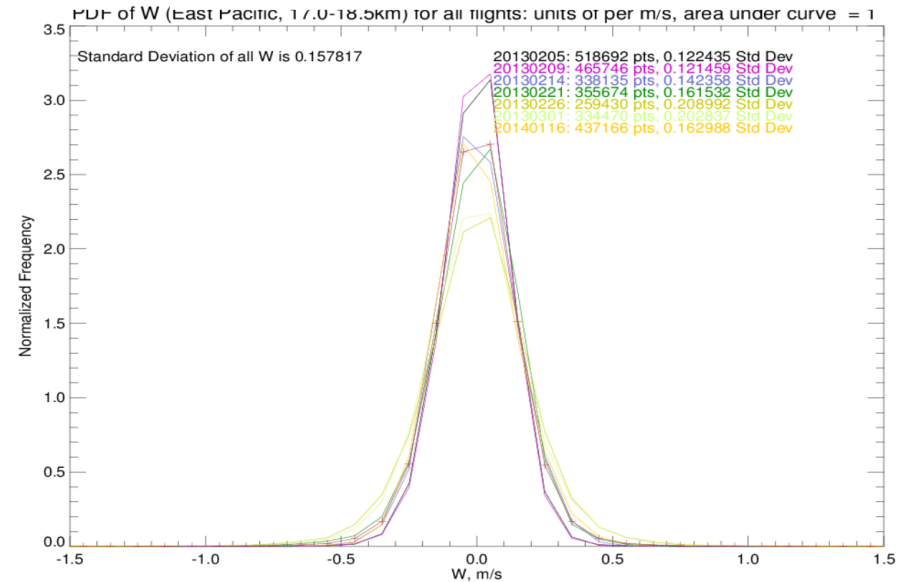
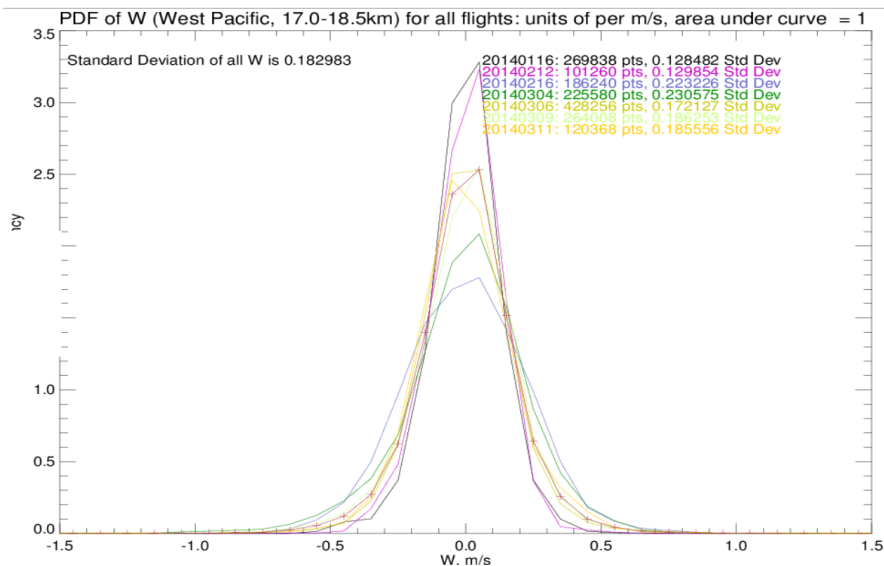


# Altitude correction for Lagrangian temperature perturbations

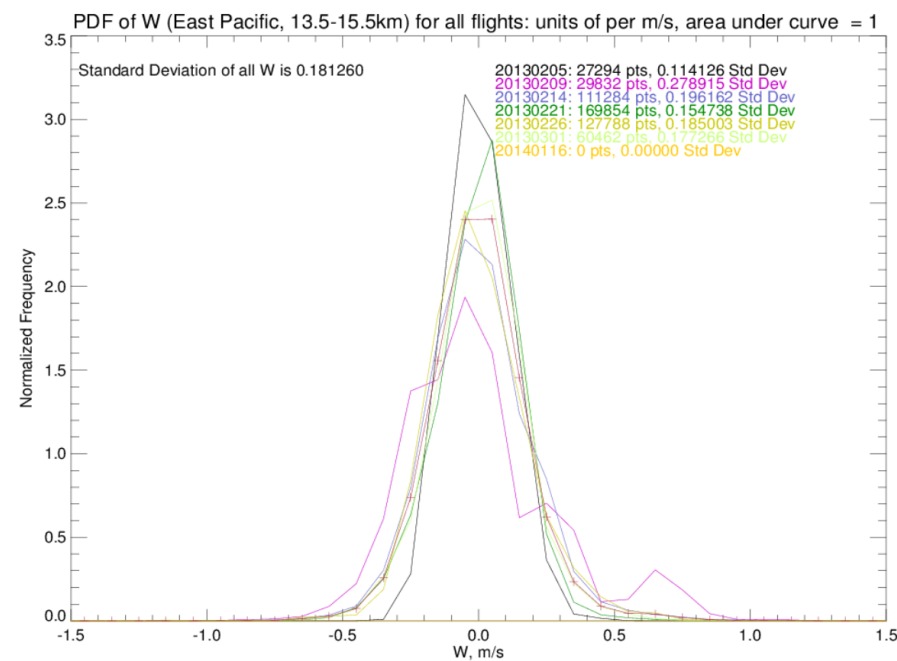
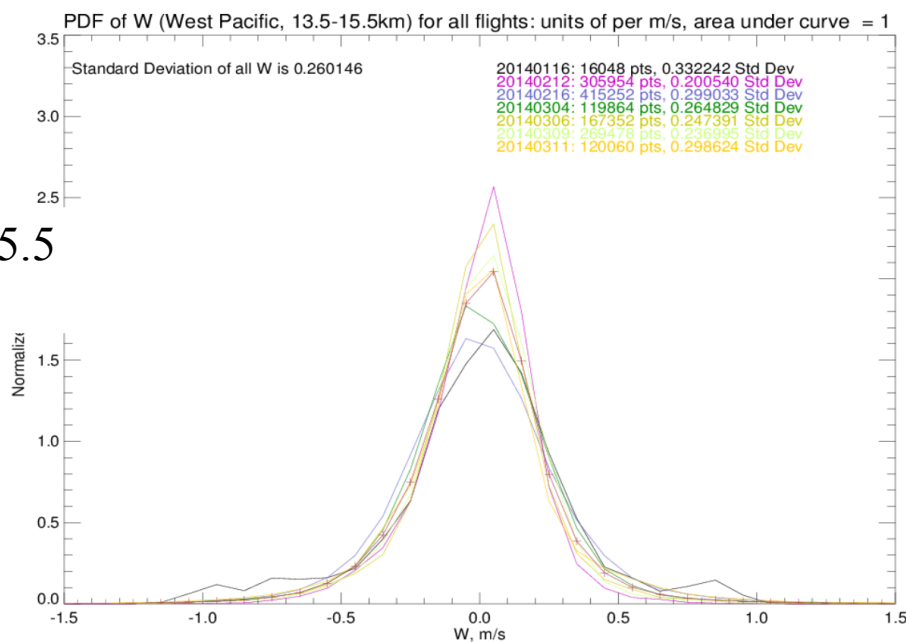
## ATTREX Western Pacific

## ATTREX Eastern Pacific

17-18.5 km



13.5-15.5 km





# Lagrangian temperature vs Eulerian temperature perturbations

Eulerian and Lagrangian temperature fluctuations are both due to the vertical displacement  $\zeta_\theta$  of air parcels, for different reasons:

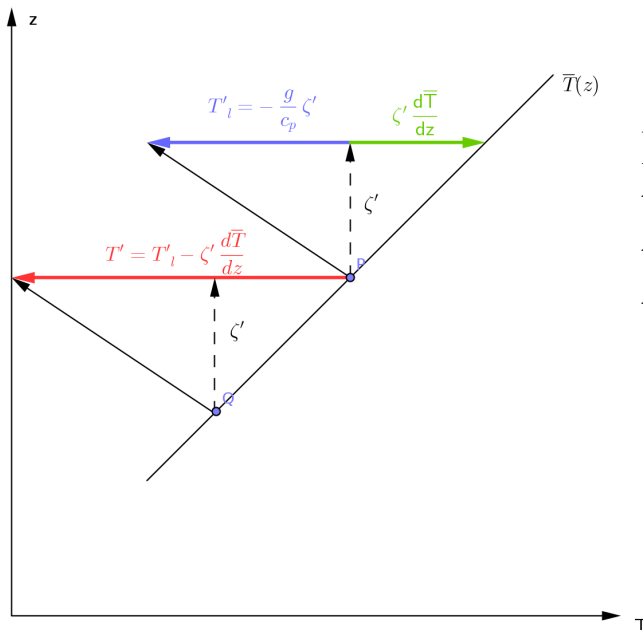
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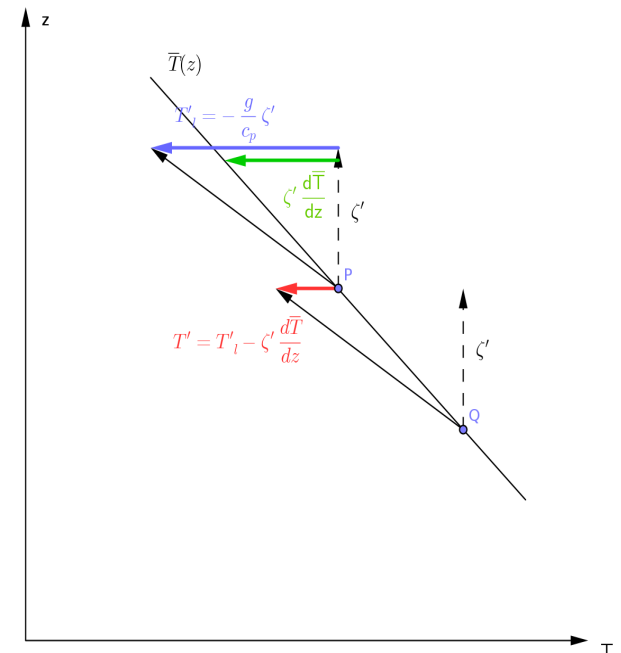
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$$T' = -\zeta_\theta \left( \frac{g}{C_P} + \frac{d\bar{T}}{dz} \right) = \frac{C_P}{g^2} \bar{T} N^2 T'_l$$

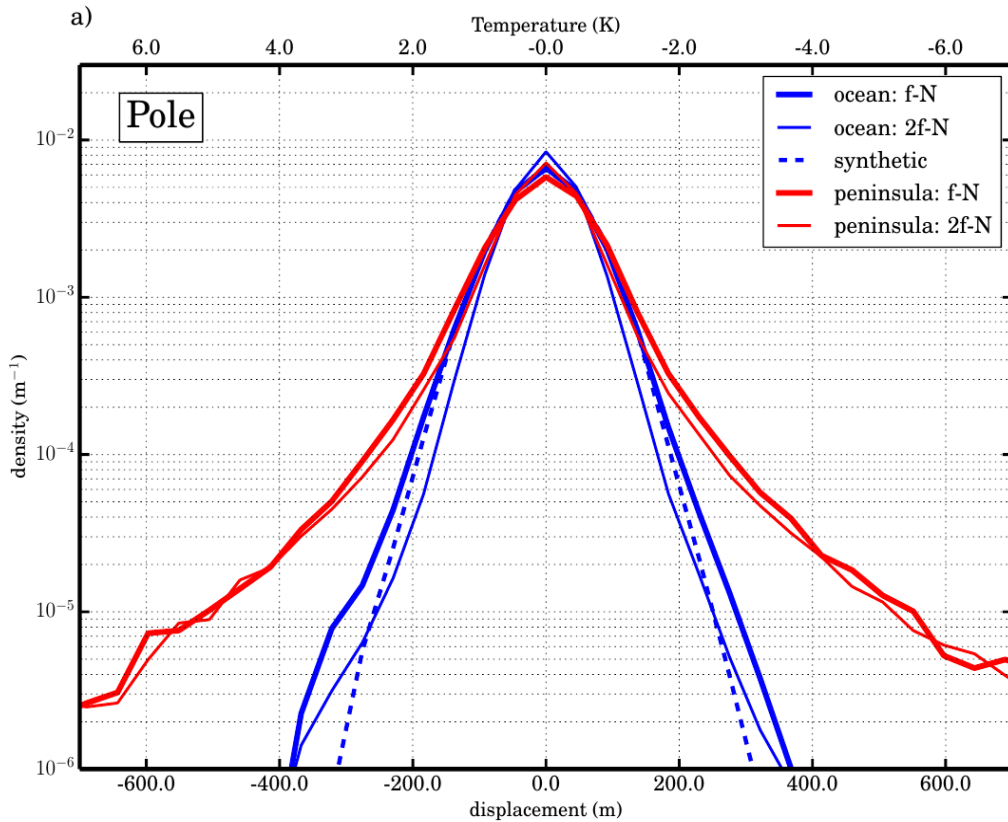


Eulerian vs Lagrangian temperature perturbation in the stratosphere (left) and troposphere (right)

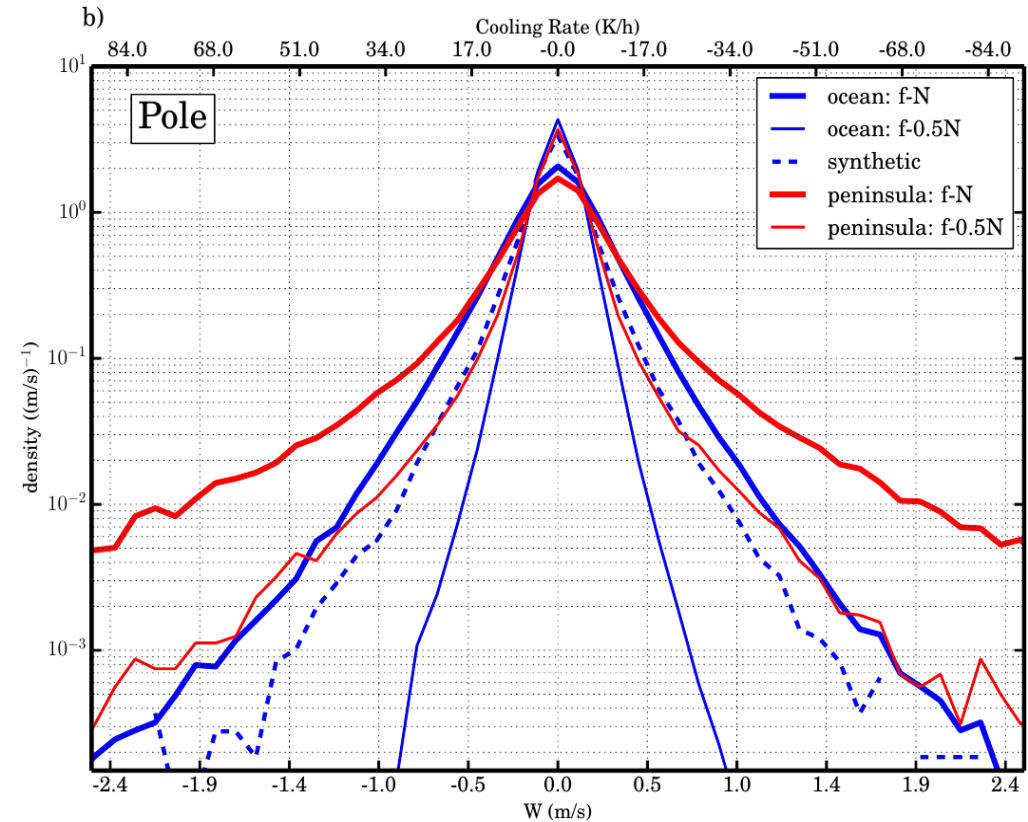


# Observed vertical velocities

## Regional contributions over the pole



Temperature



Vertical velocity

**Large wings** over the pole are associated with **mountain waves** (regions of high topographic gradients : Antarctic peninsula versus ocean and the flat Antarctic plateau), both for temperature and vertical velocity