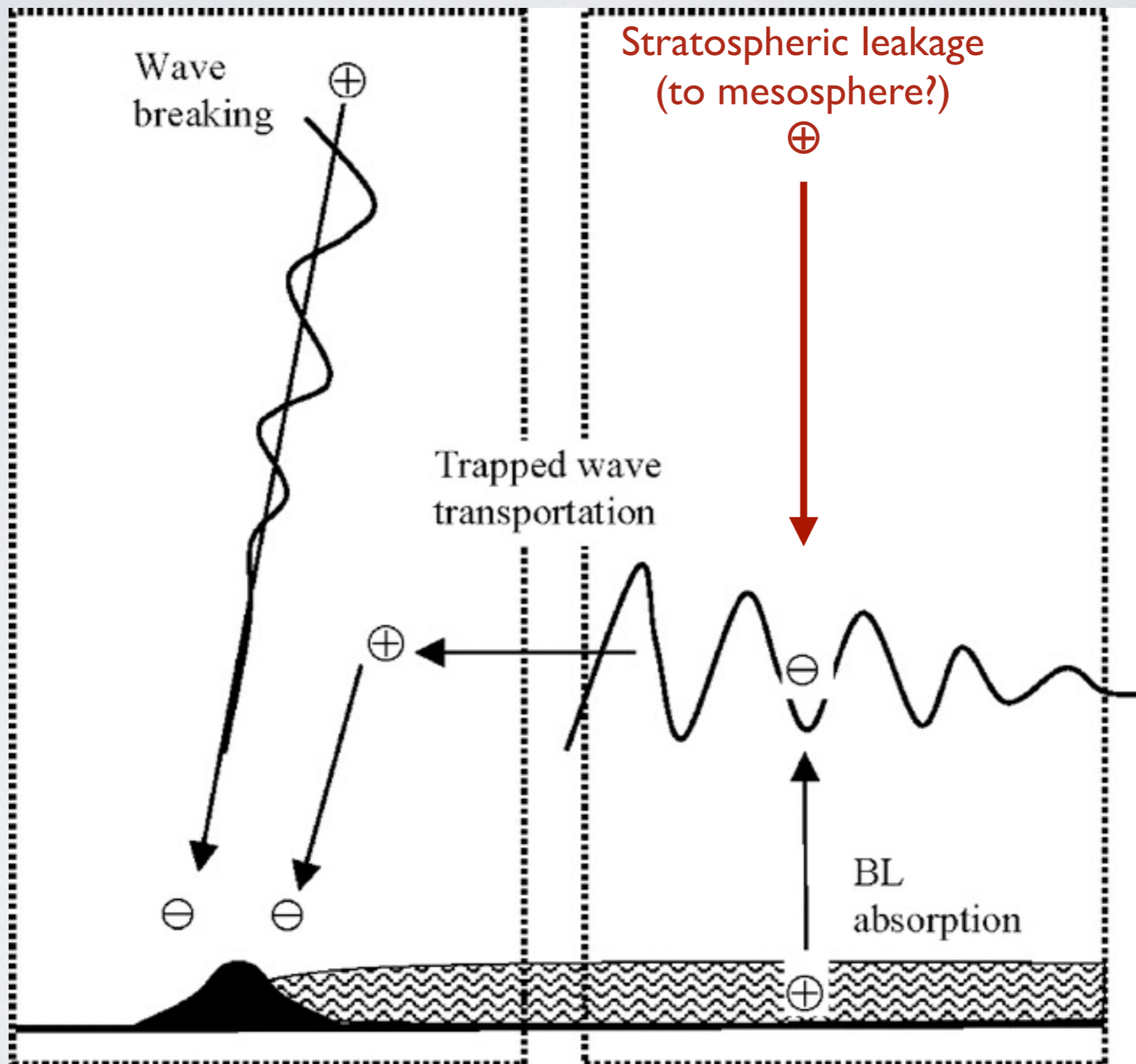


# The relative importance of the boundary layer and the stratosphere in the dissipation of trapped lee waves

Dale Durran<sup>1</sup>, Matt Hills<sup>2</sup> Peter Blossey<sup>1</sup>  
University of Washington<sup>1</sup> / University of Utah<sup>2</sup>

# Impact on momentum budget



# Real-World Reference Values

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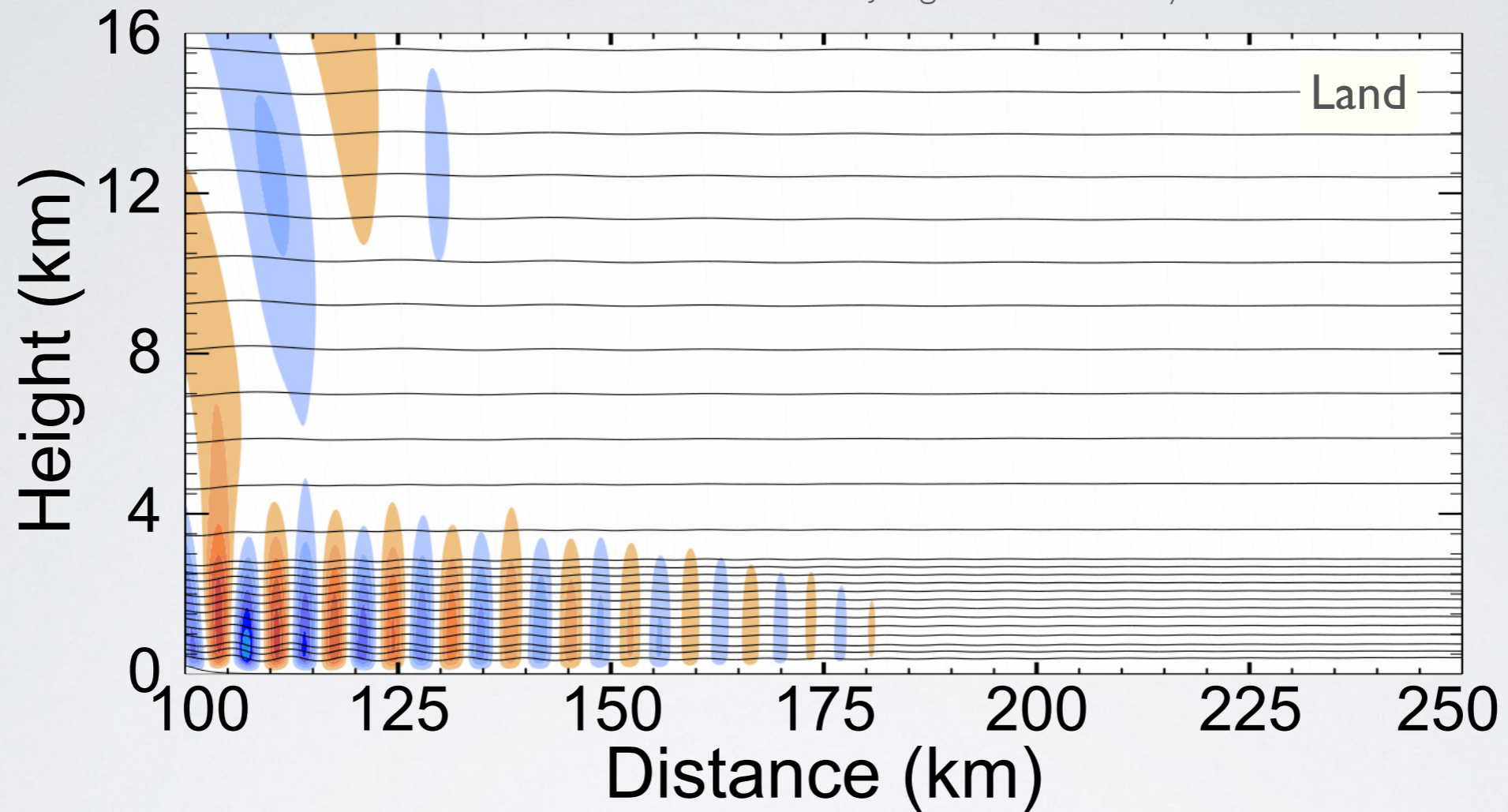
- Observed lee-wave wavelengths (Ralph et al., 1997)
  - 8.3 to 28.6 km
  - Average over 24 events was 15.8 km

# Real-World Reference Values

- Observed lee-wave wavelengths (Ralph et al., 1997)
  - 8.3 to 28.6 km
  - Average over 24 events was 15.8 km
- Characteristic surface roughnesses
  - Ocean:  $z_0=0.0001$  m
  - Land (open country):  $z_0=0.1$  m

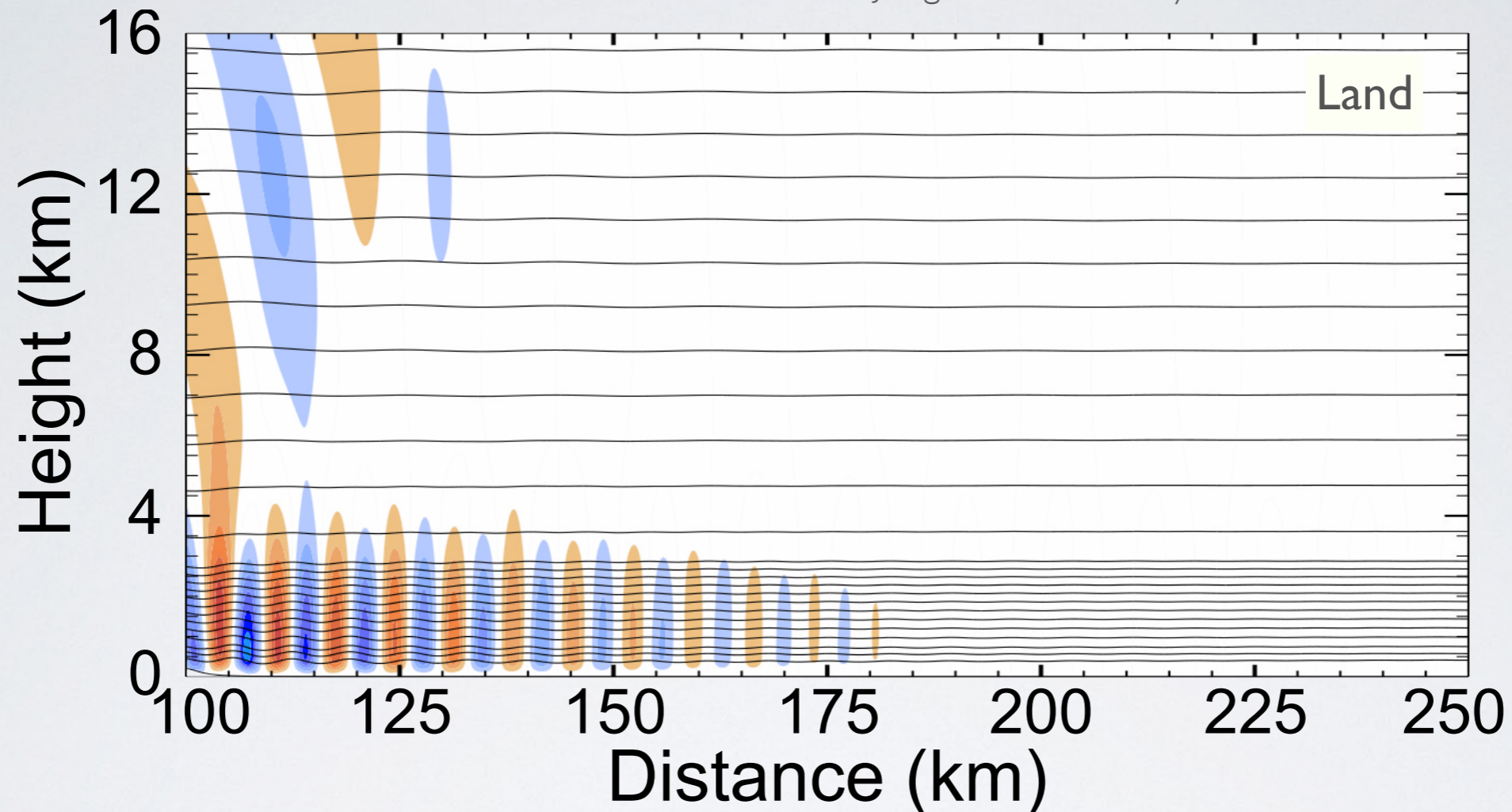
# 2 Layers, $\lambda_i=7.5$ km

Jiang et al., 2006, Doyle & Durran, 2002



## 2 Layers, $\lambda_i=7.5$ km

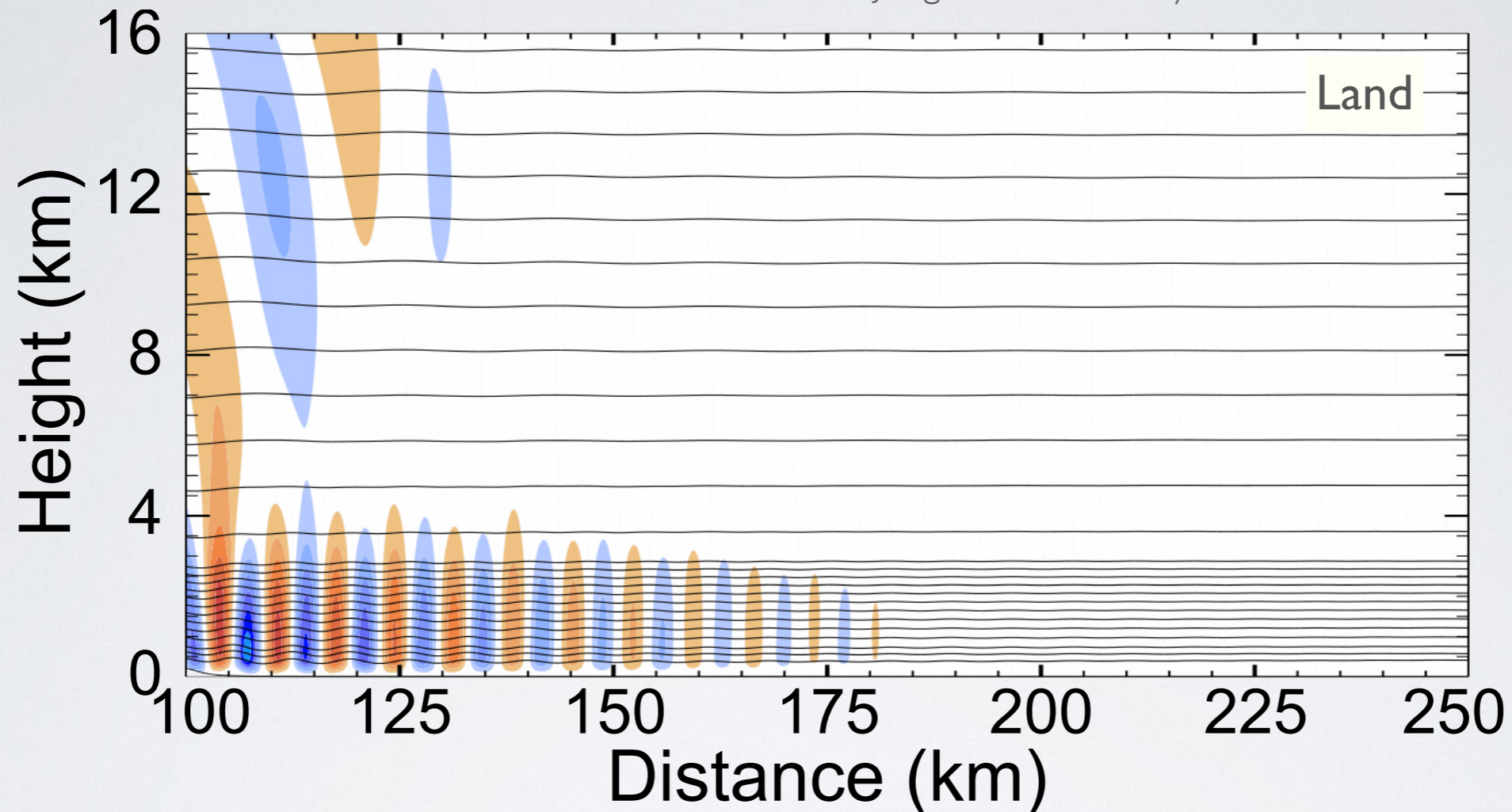
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- Short-wavelength waves decay vertically before reaching typical tropopause heights.

## 2 Layers, $\lambda_i=7.5$ km

Jiang et al., 2006, Doyle & Durran, 2002



- Short-wavelength waves decay vertically before reaching typical tropopause heights.
- Stratospheric leakage is totally dominated by BL friction.

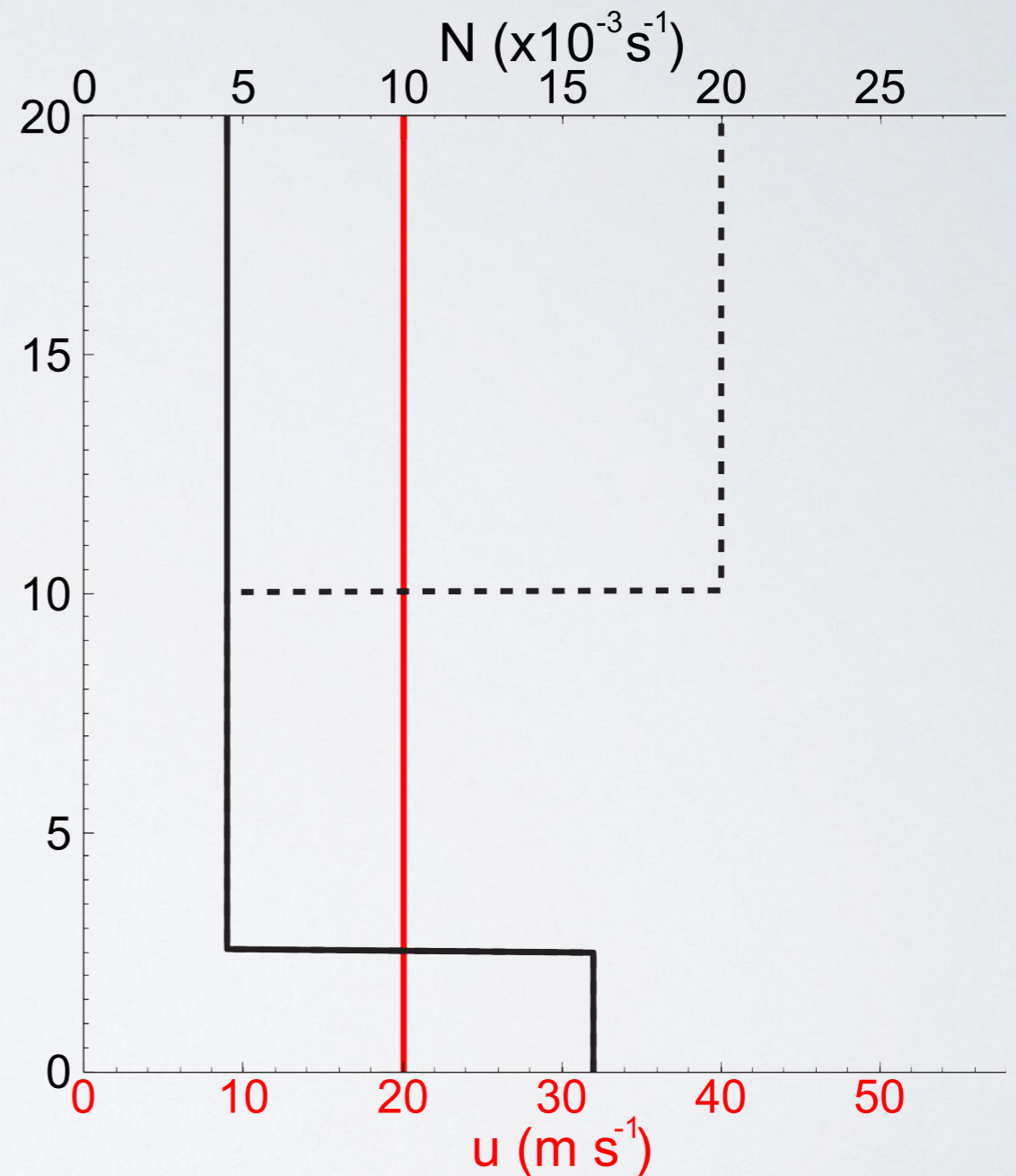


## 2-layers, $\lambda_i=20.5$ km

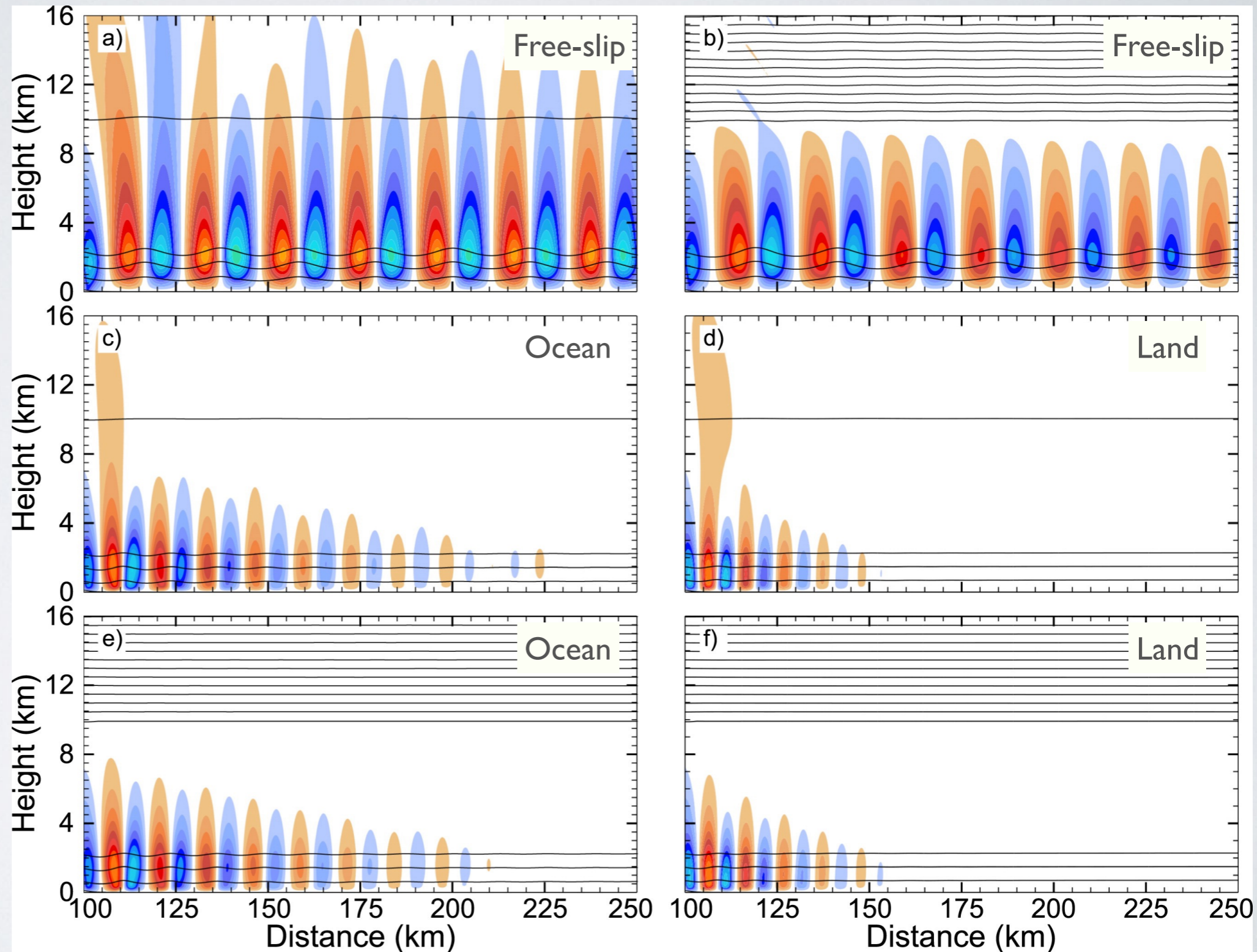
- For constant upper-layer Scorer parameter, e-folding decay scale is

$$\left[ \left( \frac{2\pi}{\lambda} \right)^2 - l_u^2 \right]^{-1/2}$$

- Decay scale decreases as  $\lambda$  decreases

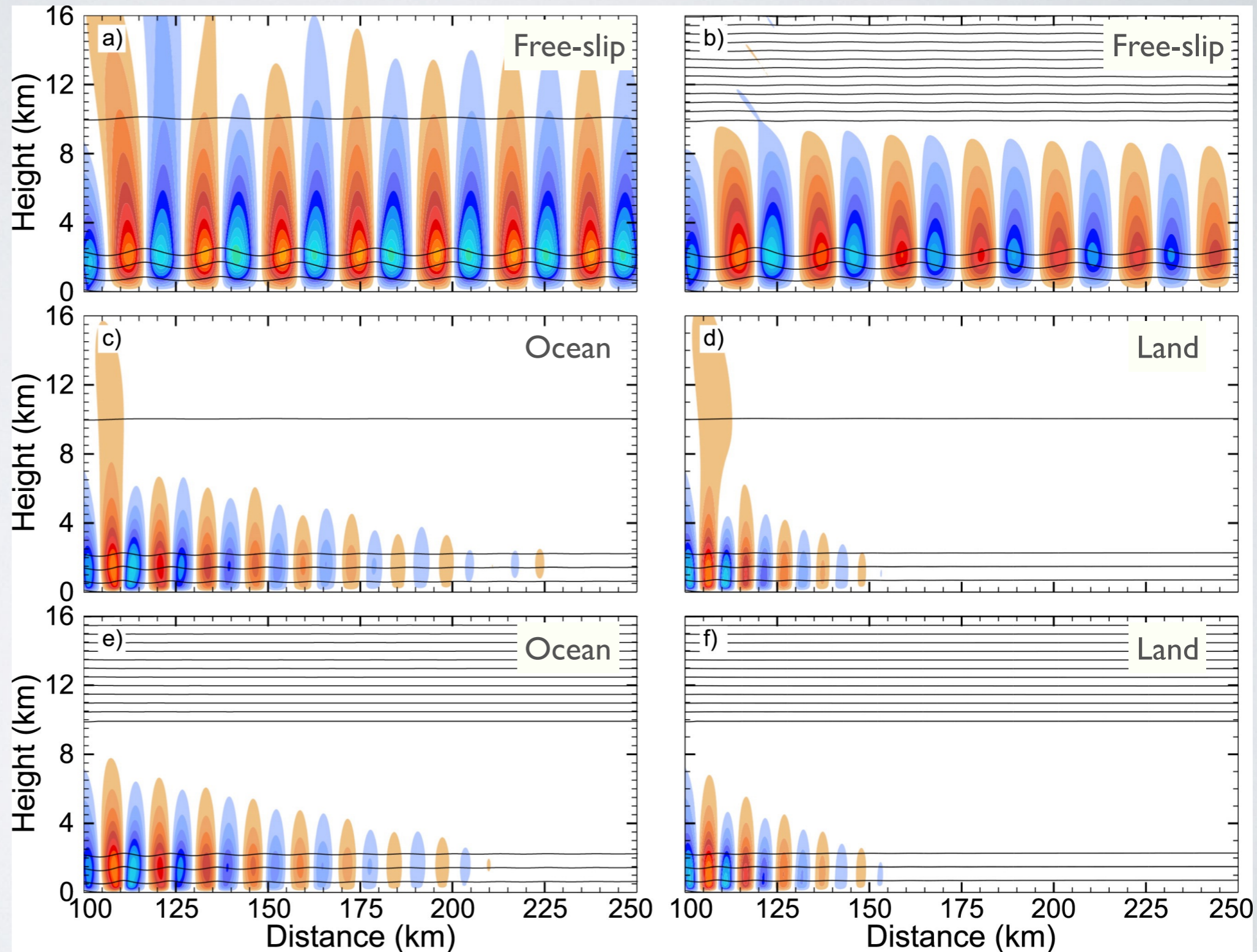


# 2 or 3 uniform layers: $\lambda_i=20.5$ km

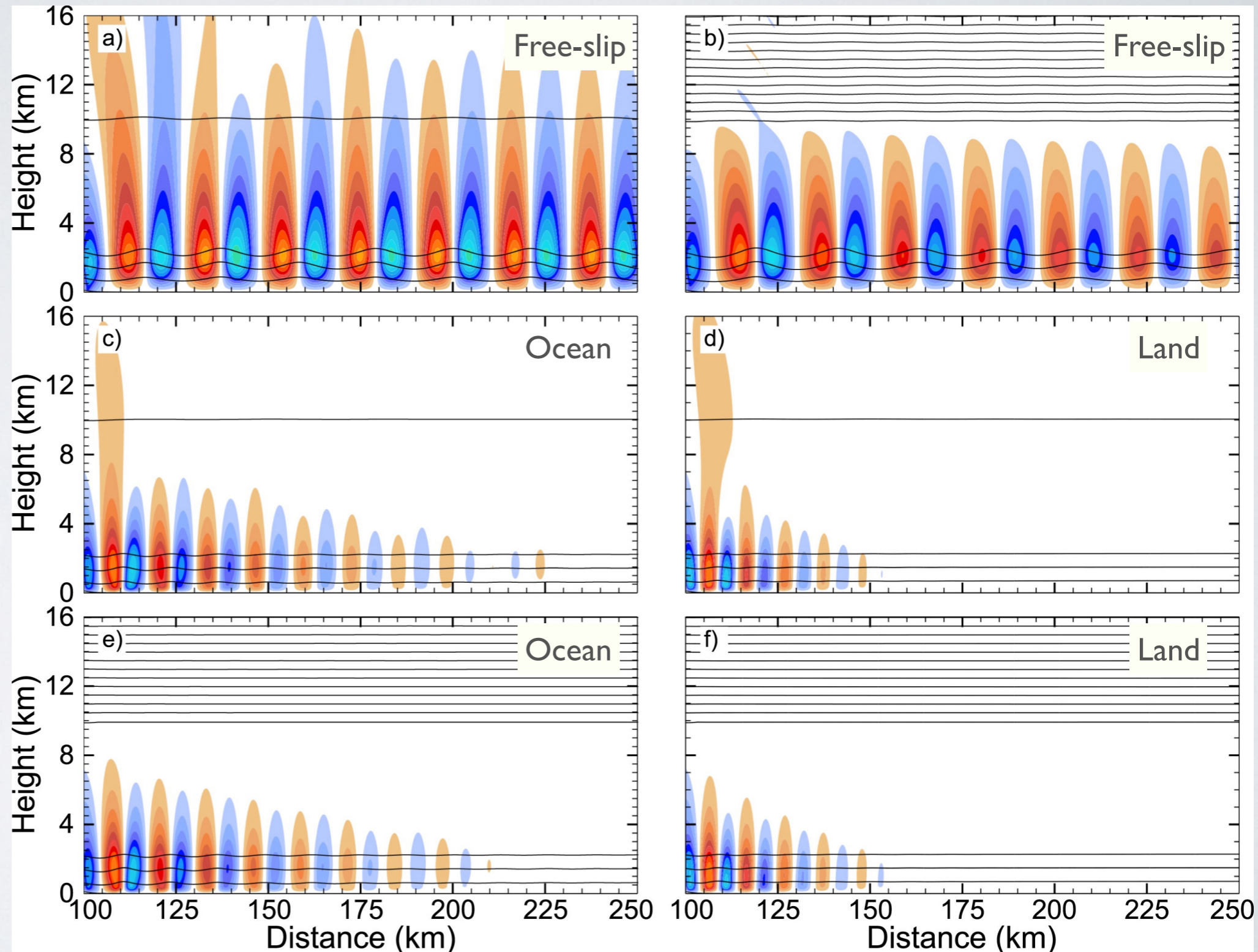


# 2 or 3 uniform layers: $\lambda_i=20.5$ km

Surface friction  
reduces  $\lambda$



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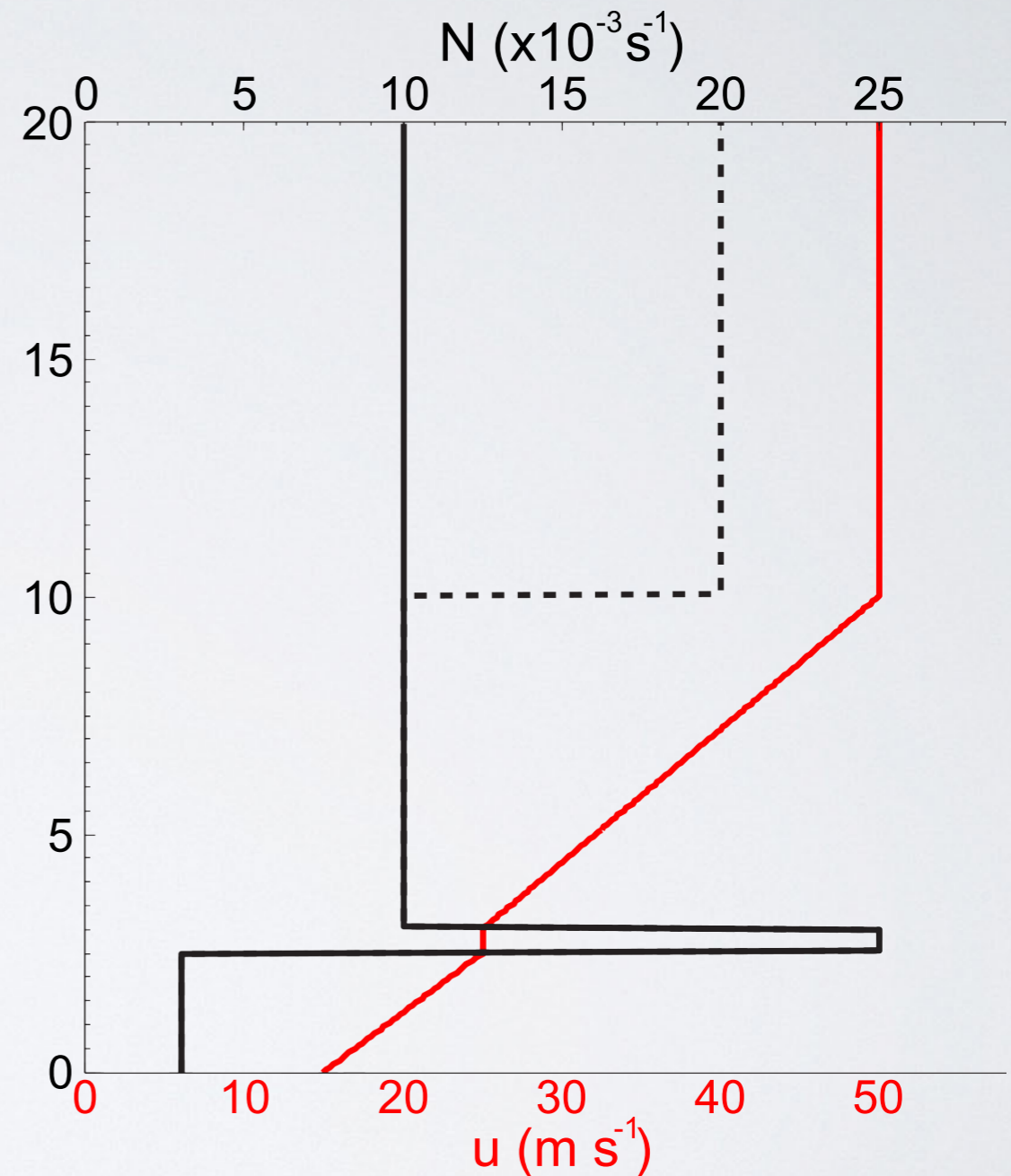


Surface friction  
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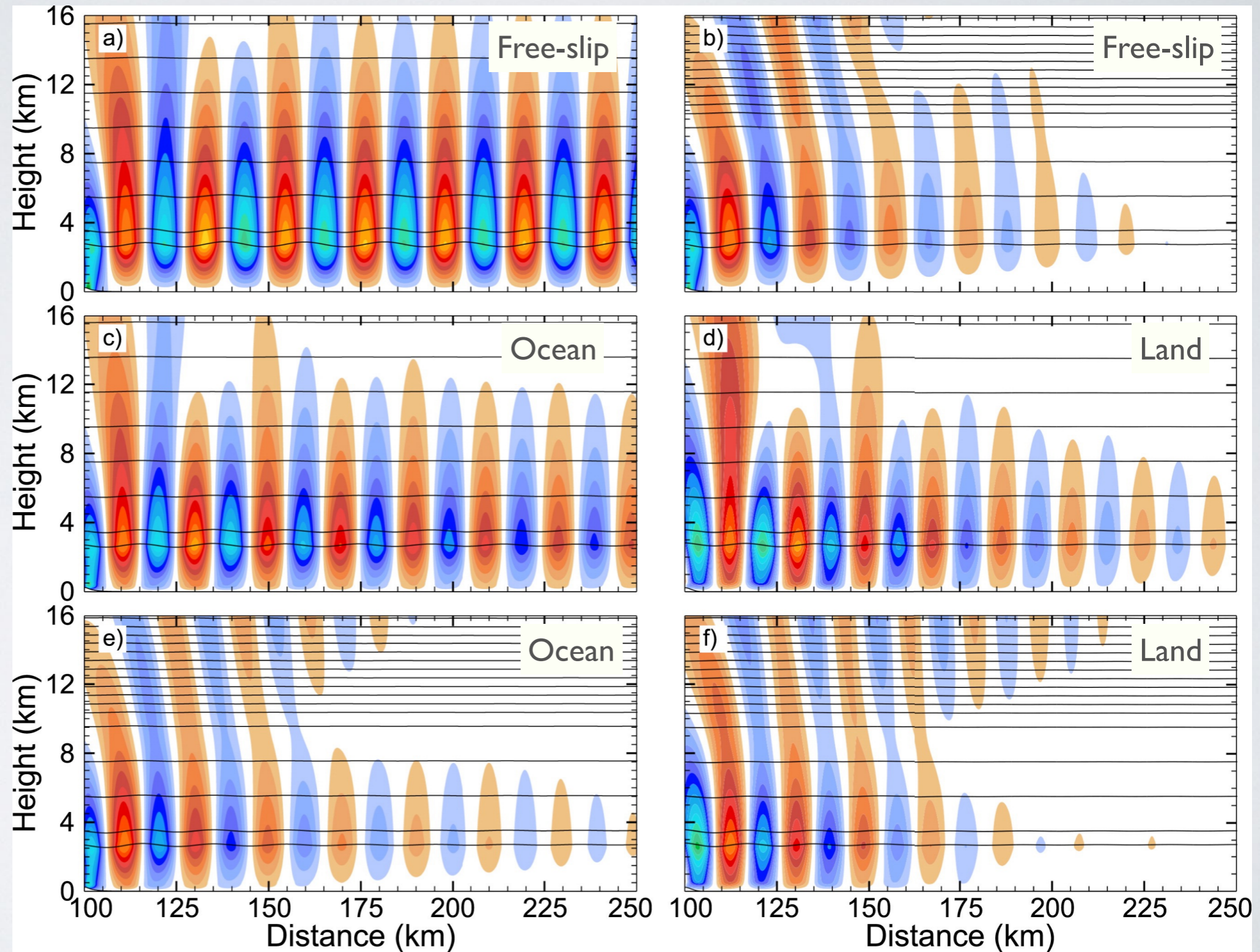
Frictional  
dissipation  
dominates

# Elevated inversion & shear, $\lambda_i=21.8$ km

- Typical of many observed events

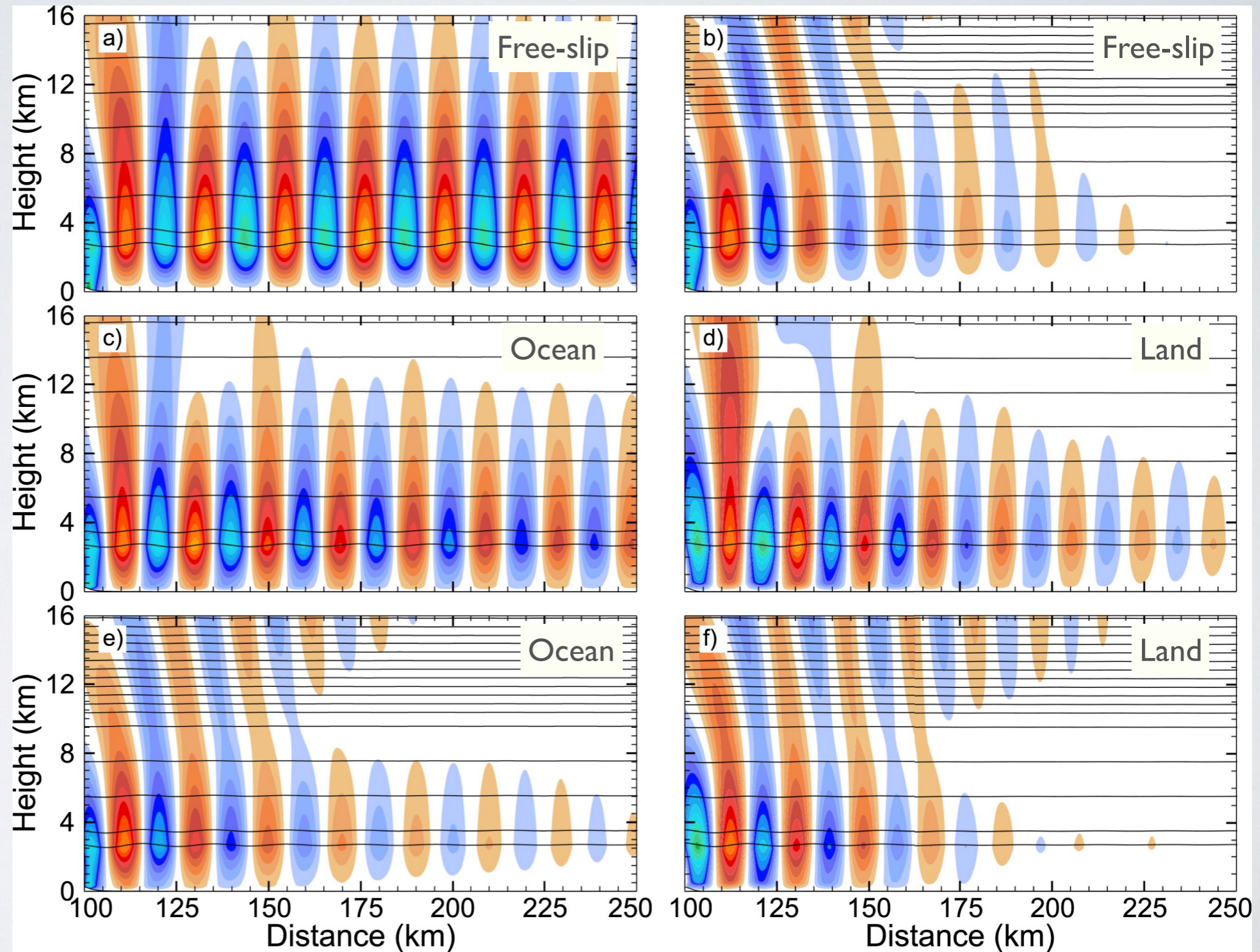


# Elevated inversion & shear: $\lambda_i=21.8$ km



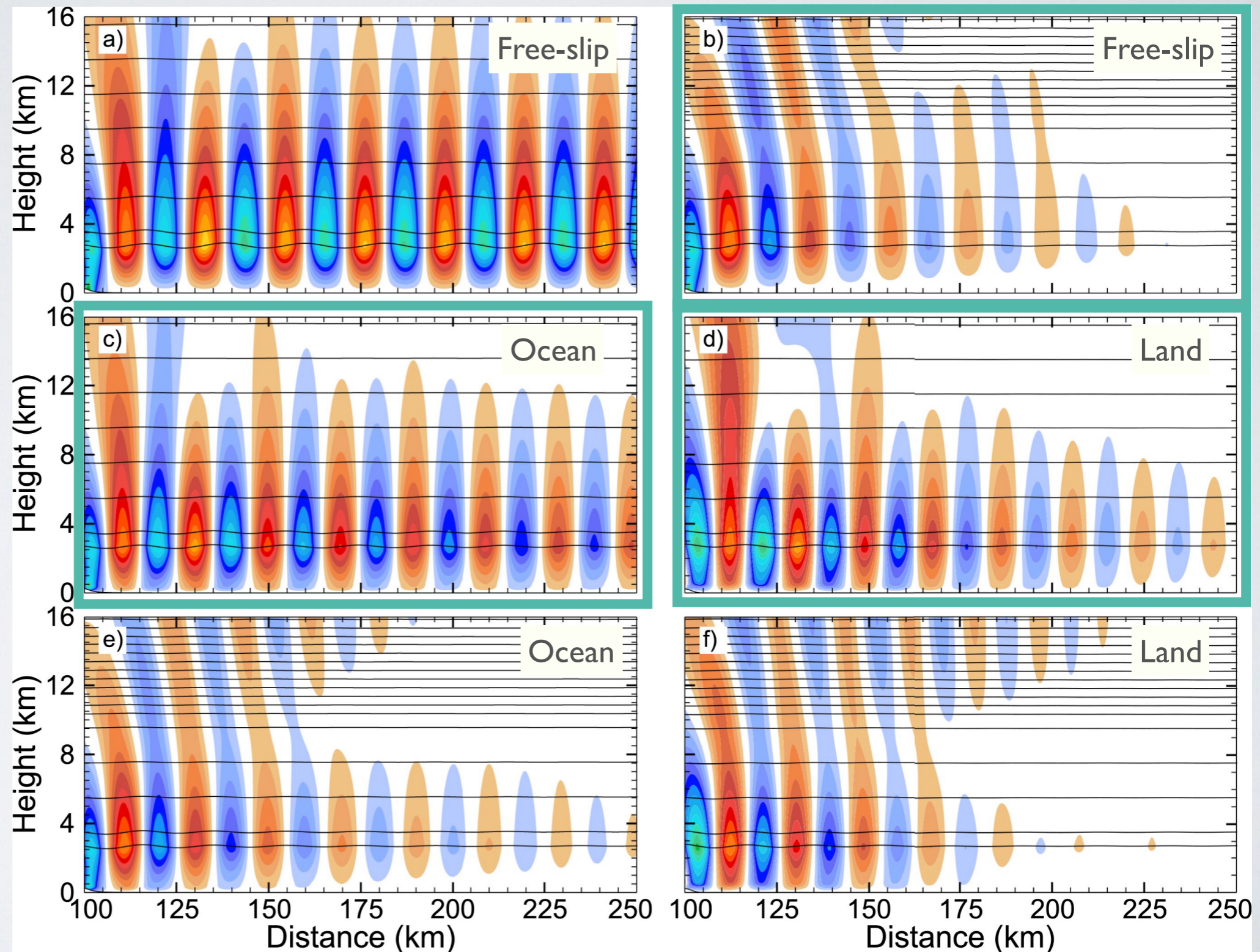
# Elevated inversion & shear: $\lambda_i=21.8$ km

Surface friction only slightly reduces  $\lambda$



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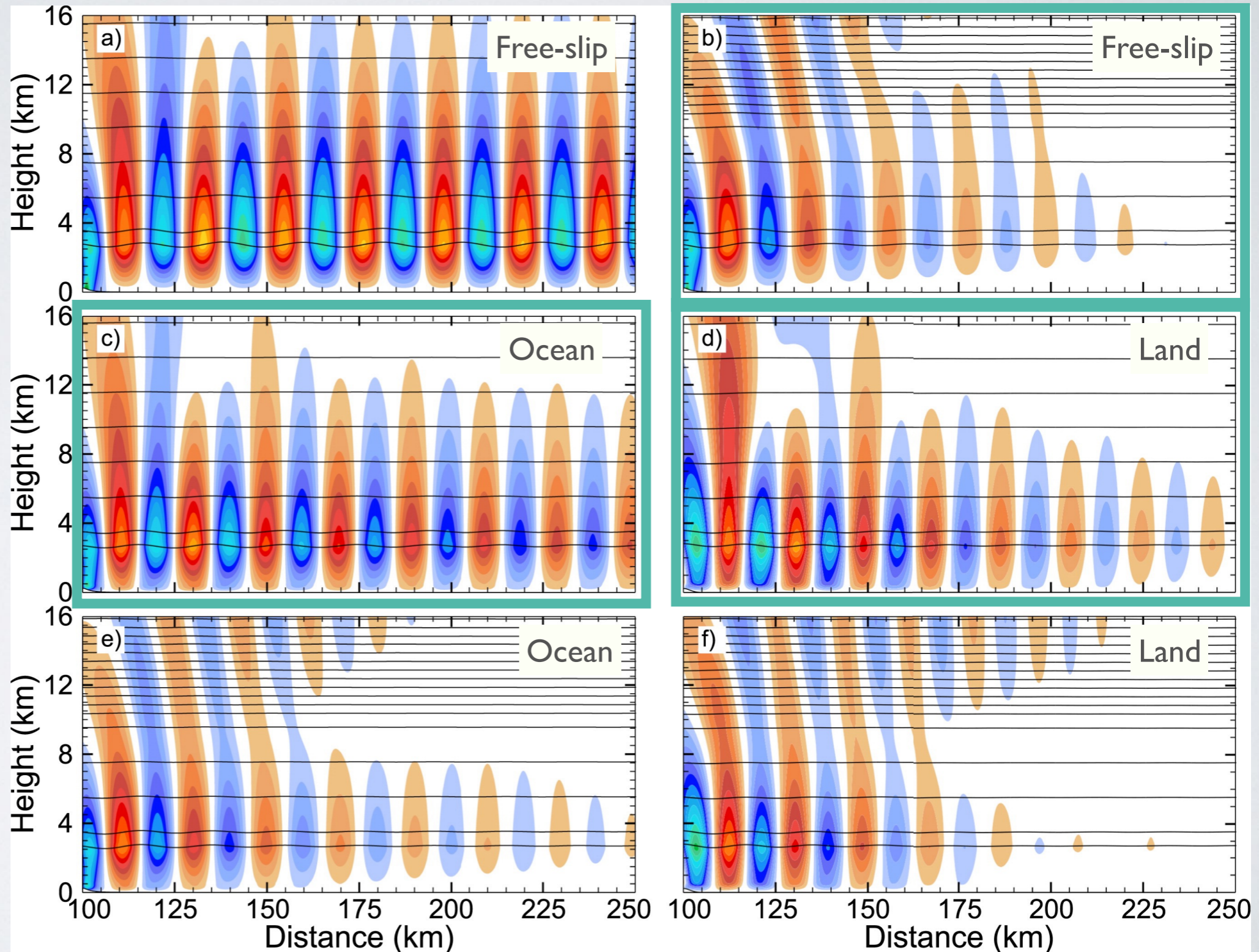




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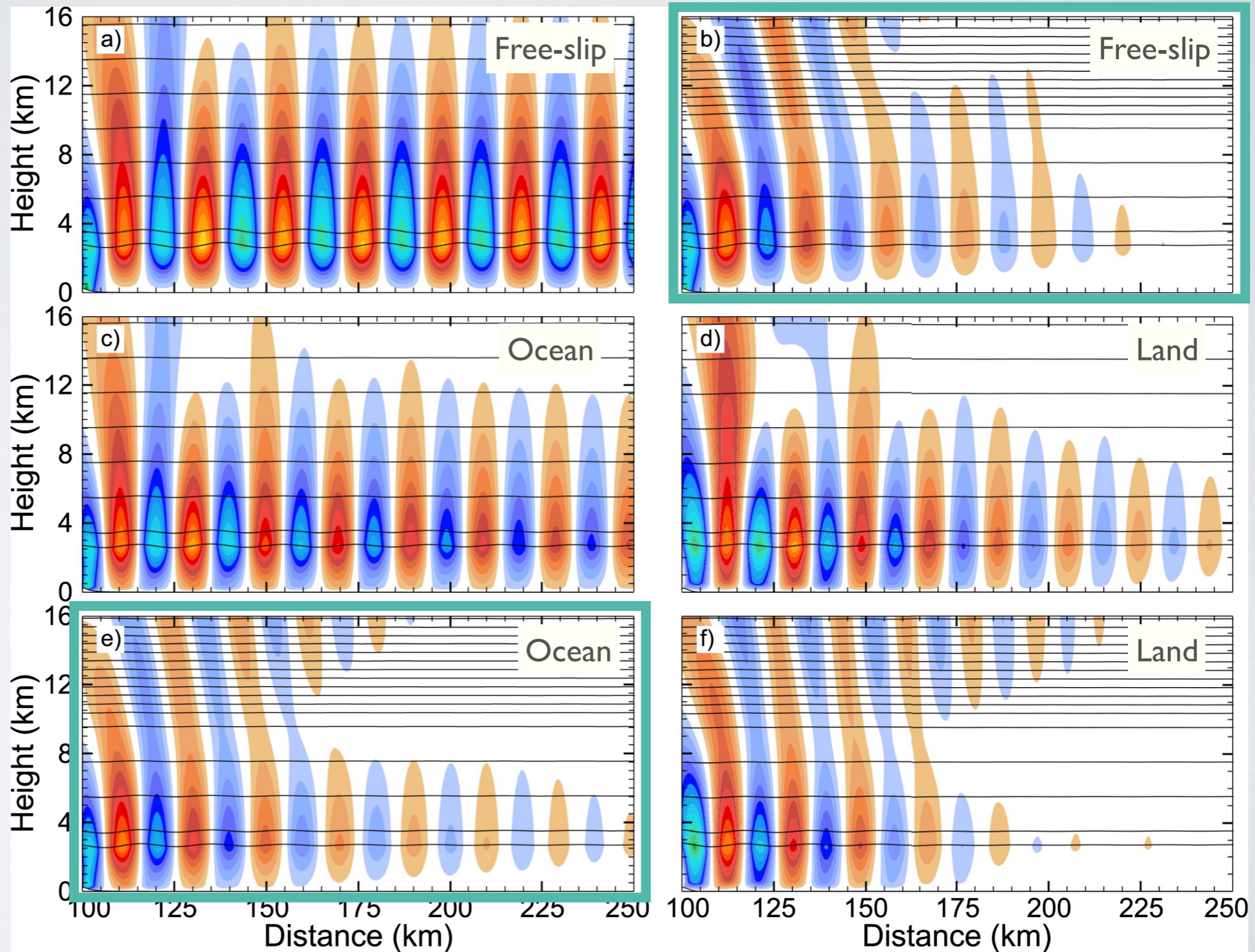
Stratospheric  
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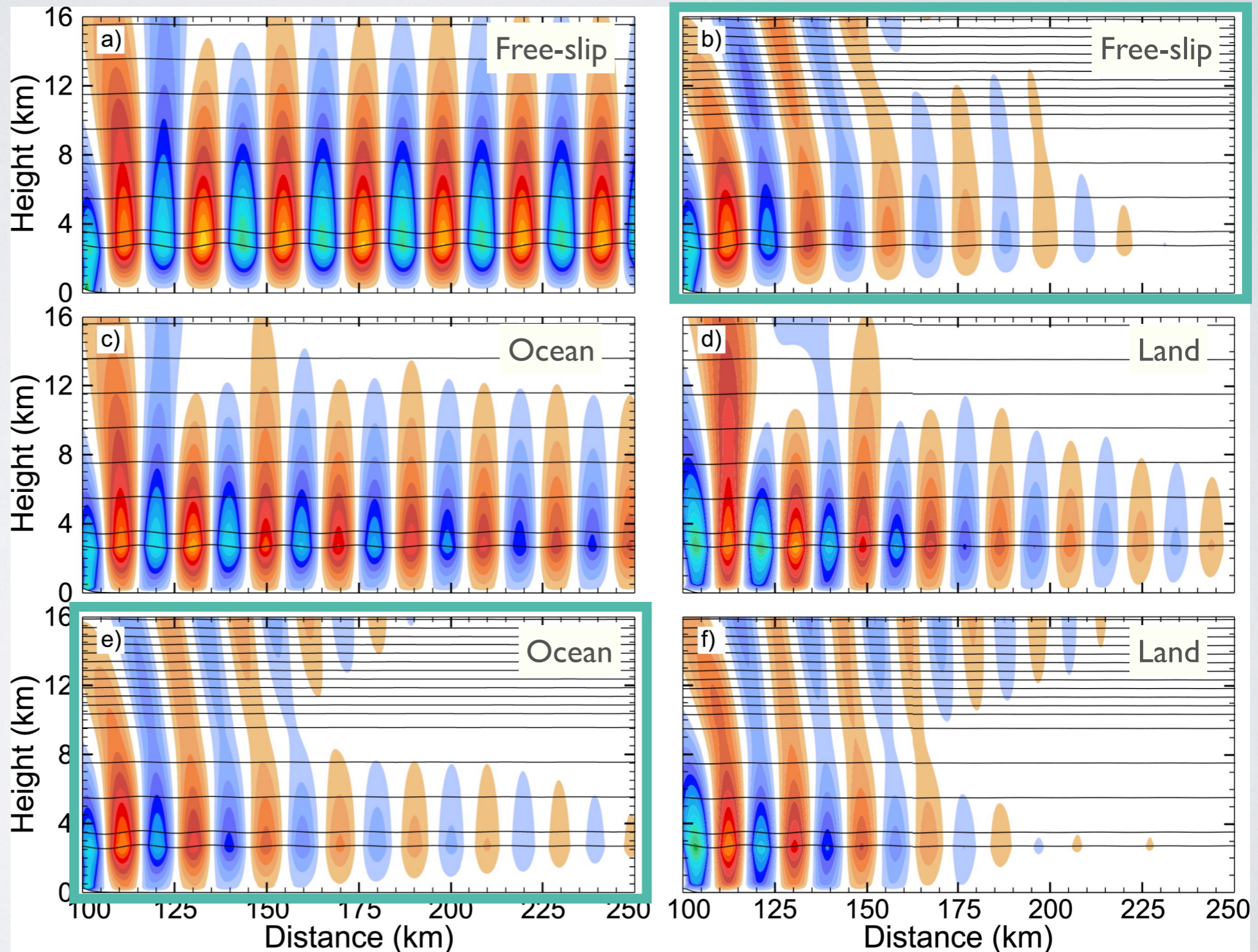


# Elevated inversion & shear: $\lambda_i=21.8$ km

Surface friction only slightly reduces  $\lambda$

Stratospheric leakage dominates

Ocean gives less leakage than free-slip



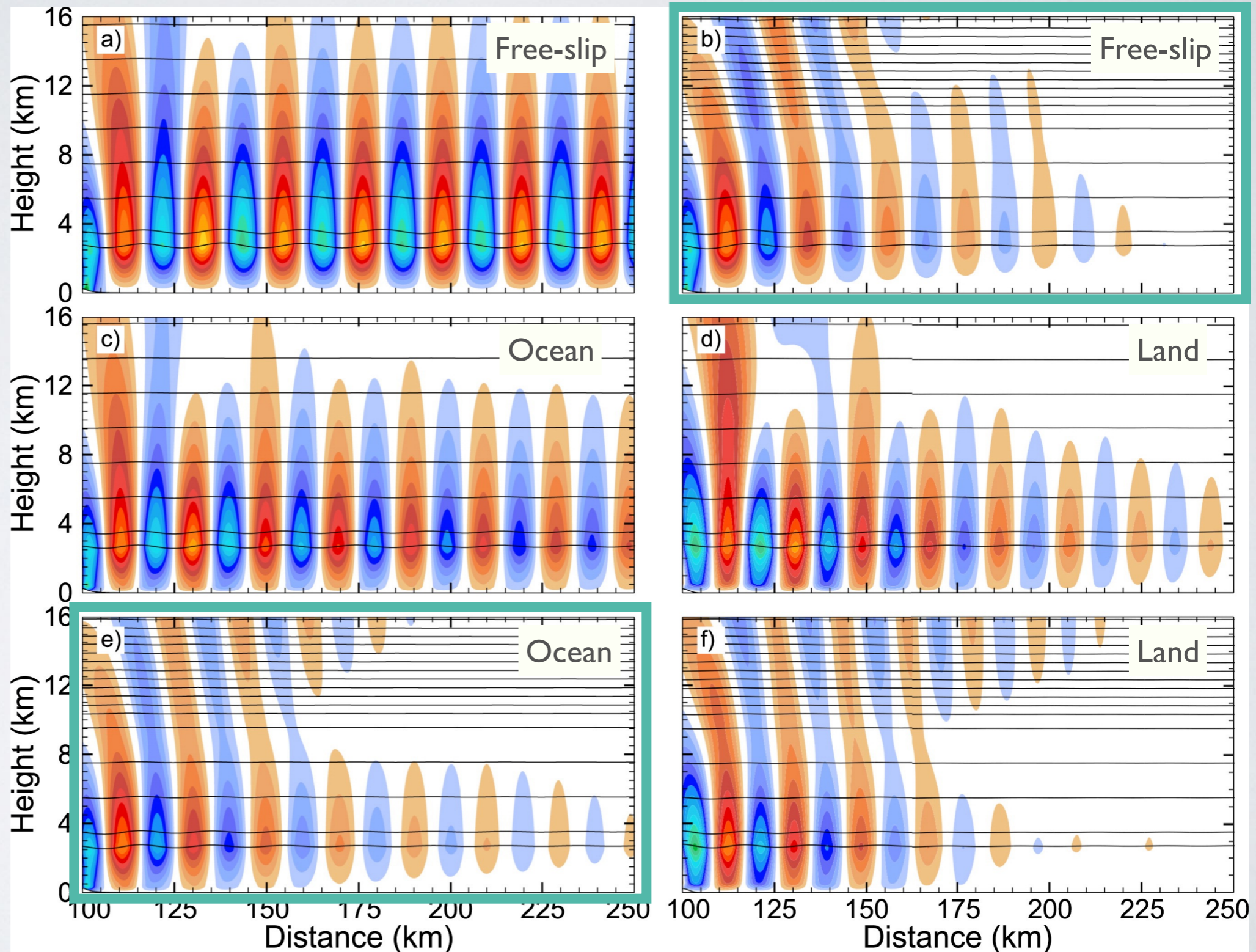
# Elevated inversion & shear: $\lambda_i=21.8$ km

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Stratospheric leakage dominates

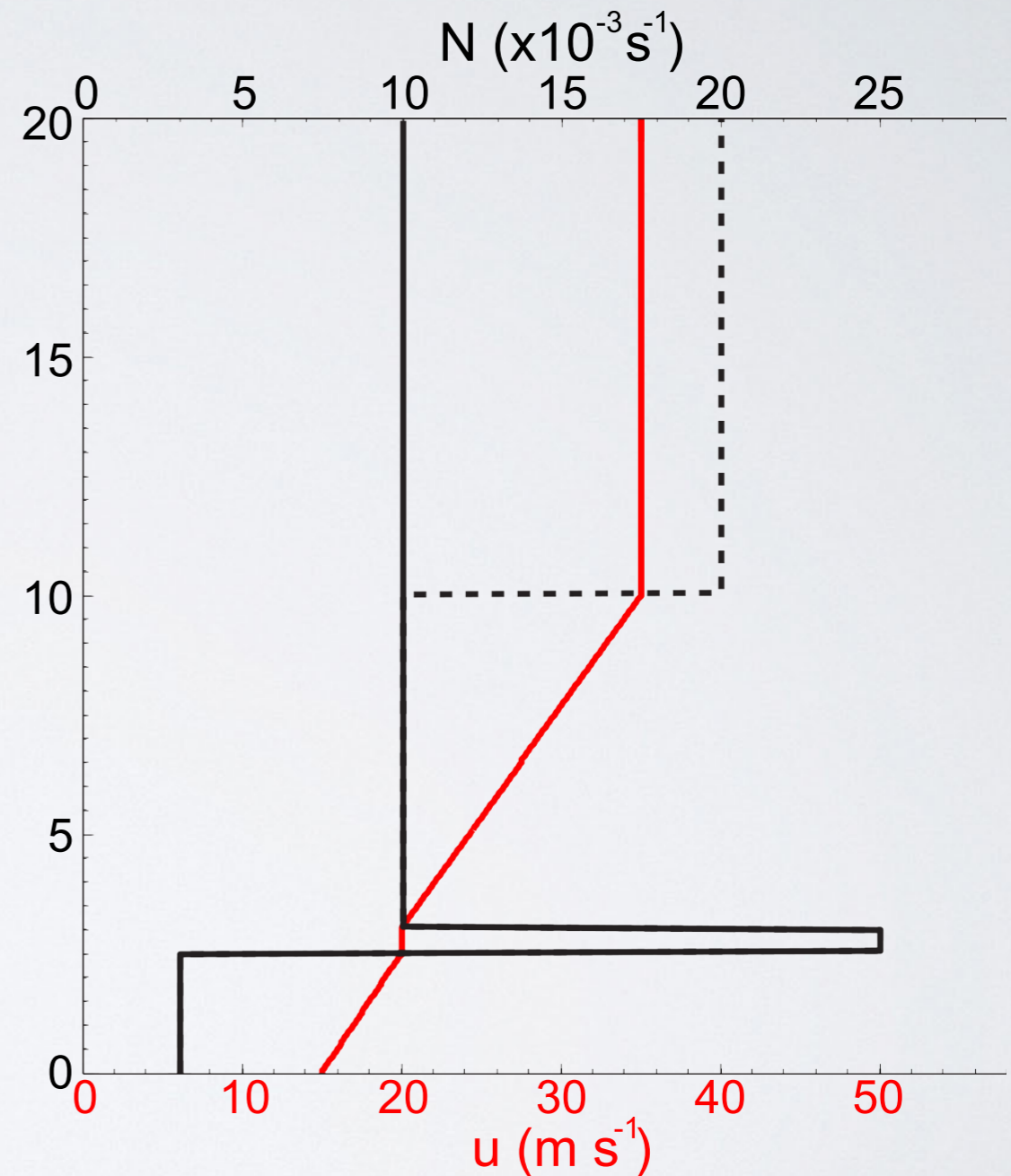
Ocean gives less leakage than free-slip

$\lambda$  reduced to 19.8 km is better trapped.

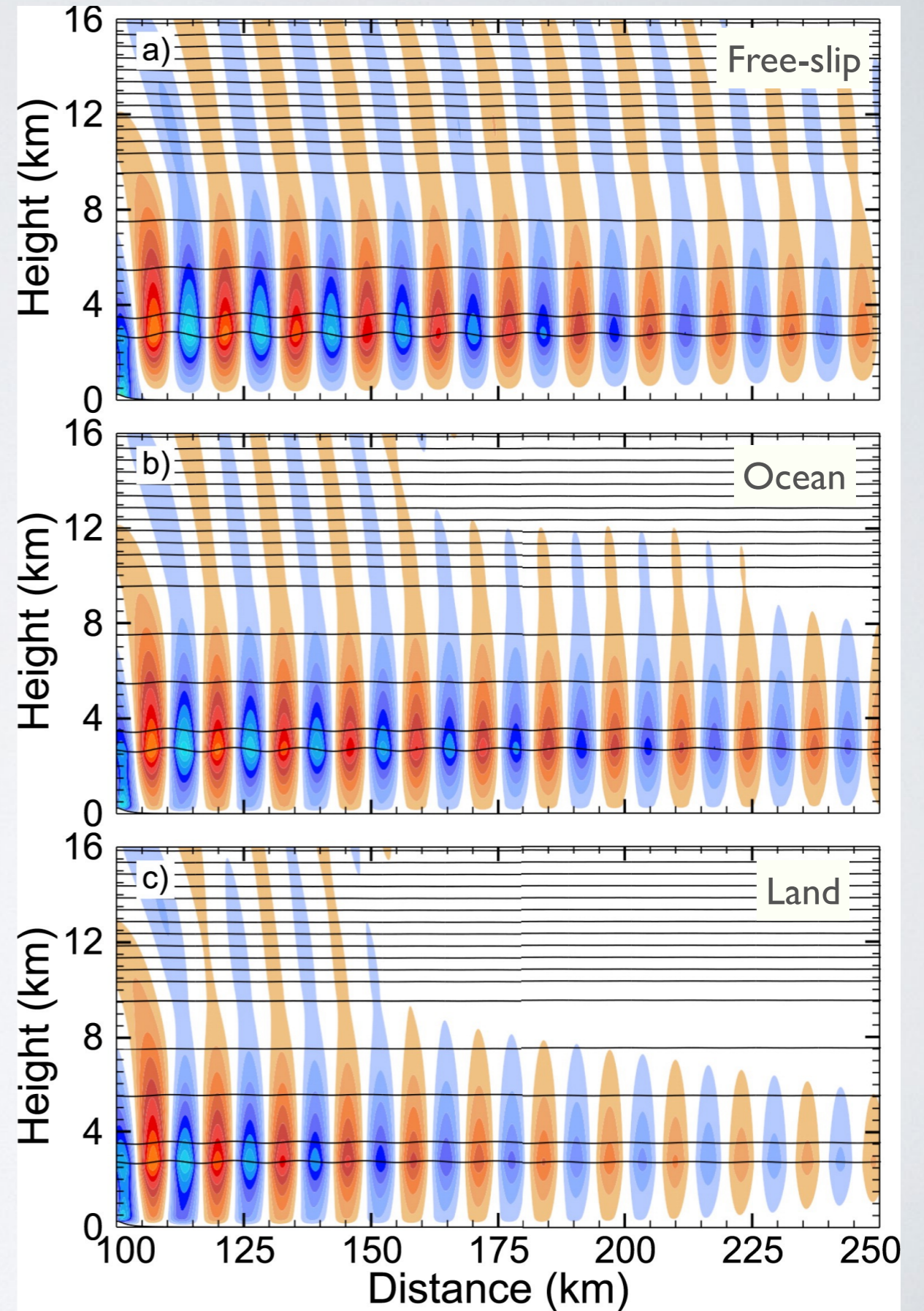
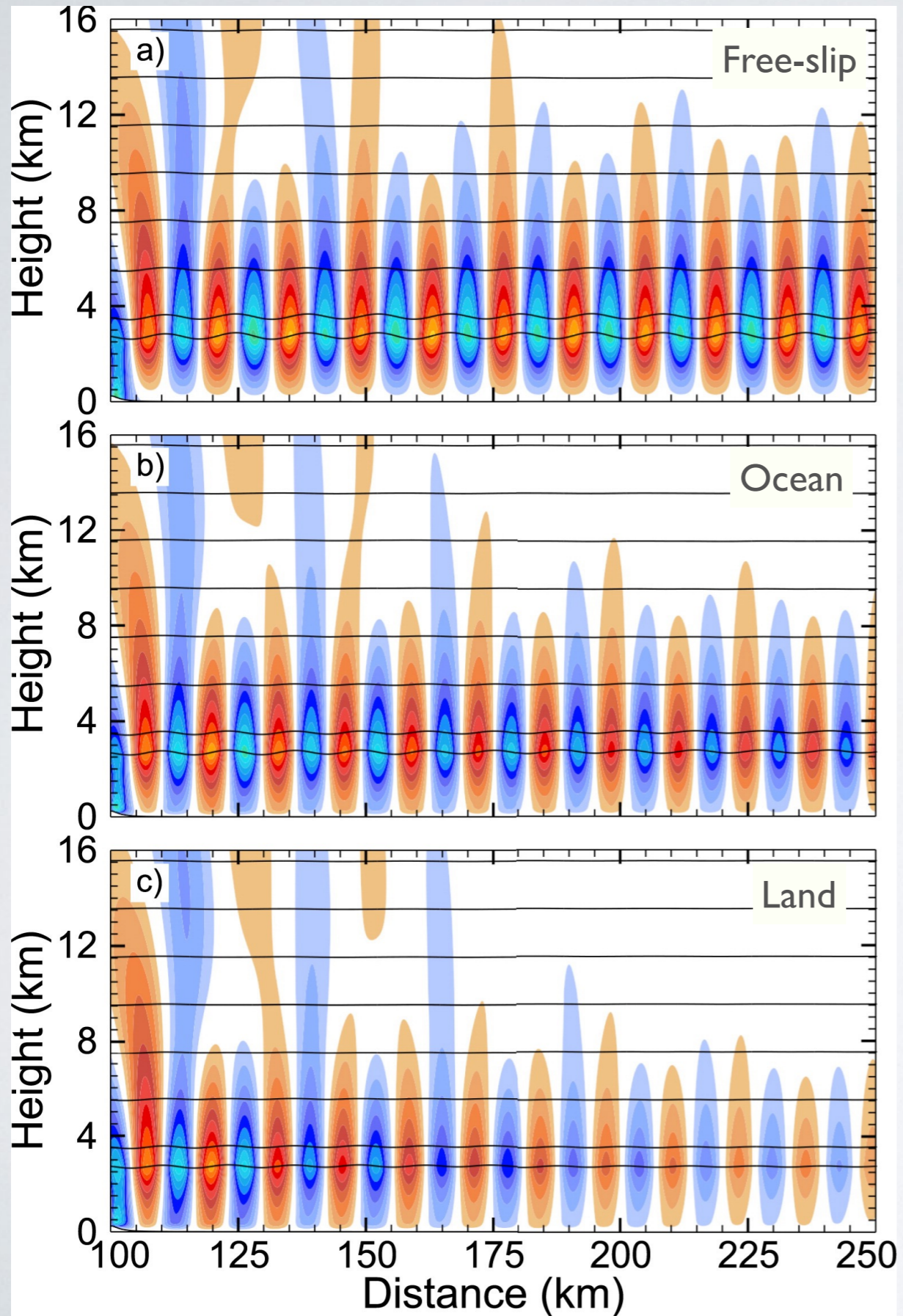


# Elevated inversion & shear, $\lambda_i = 13.9$ km

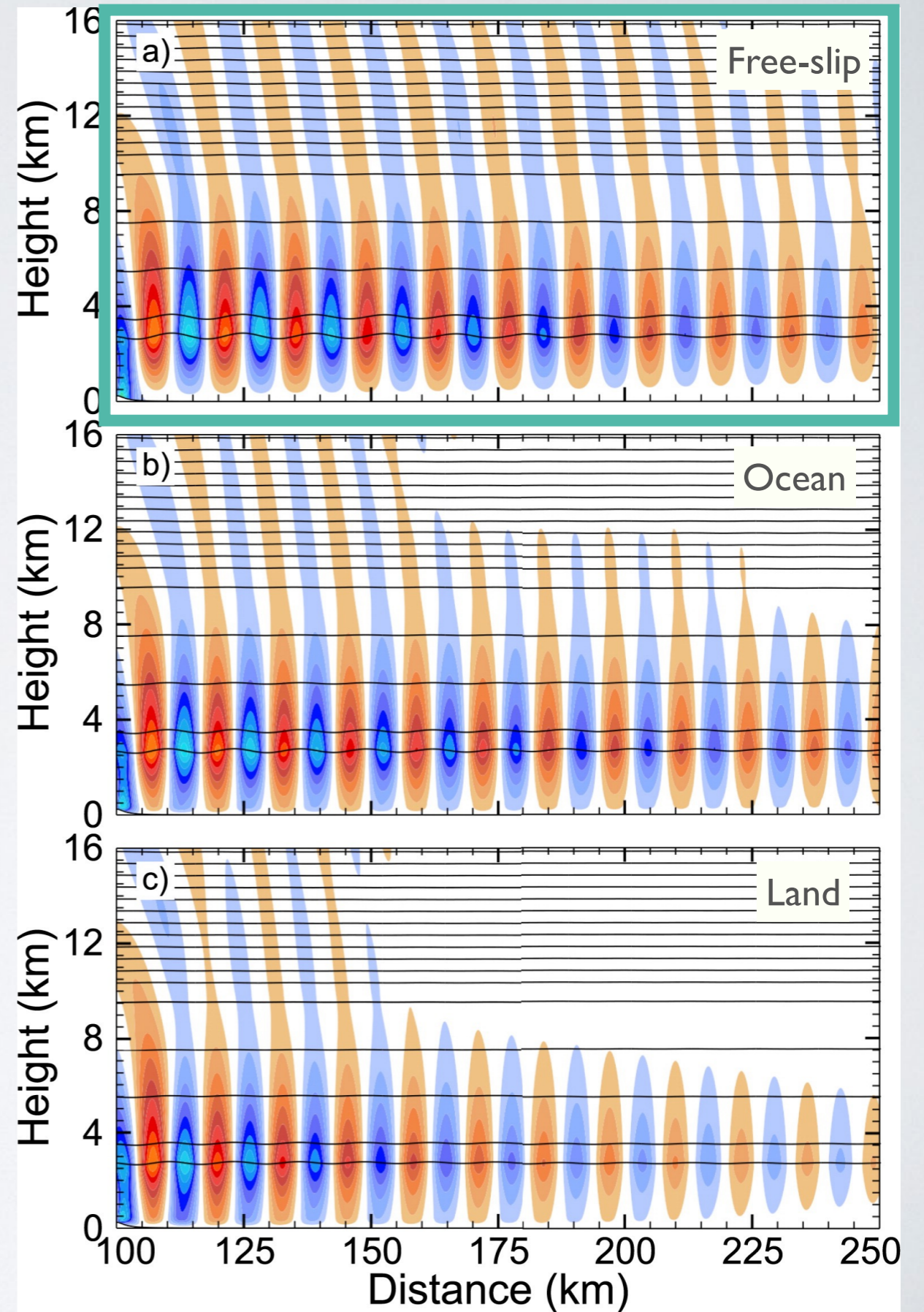
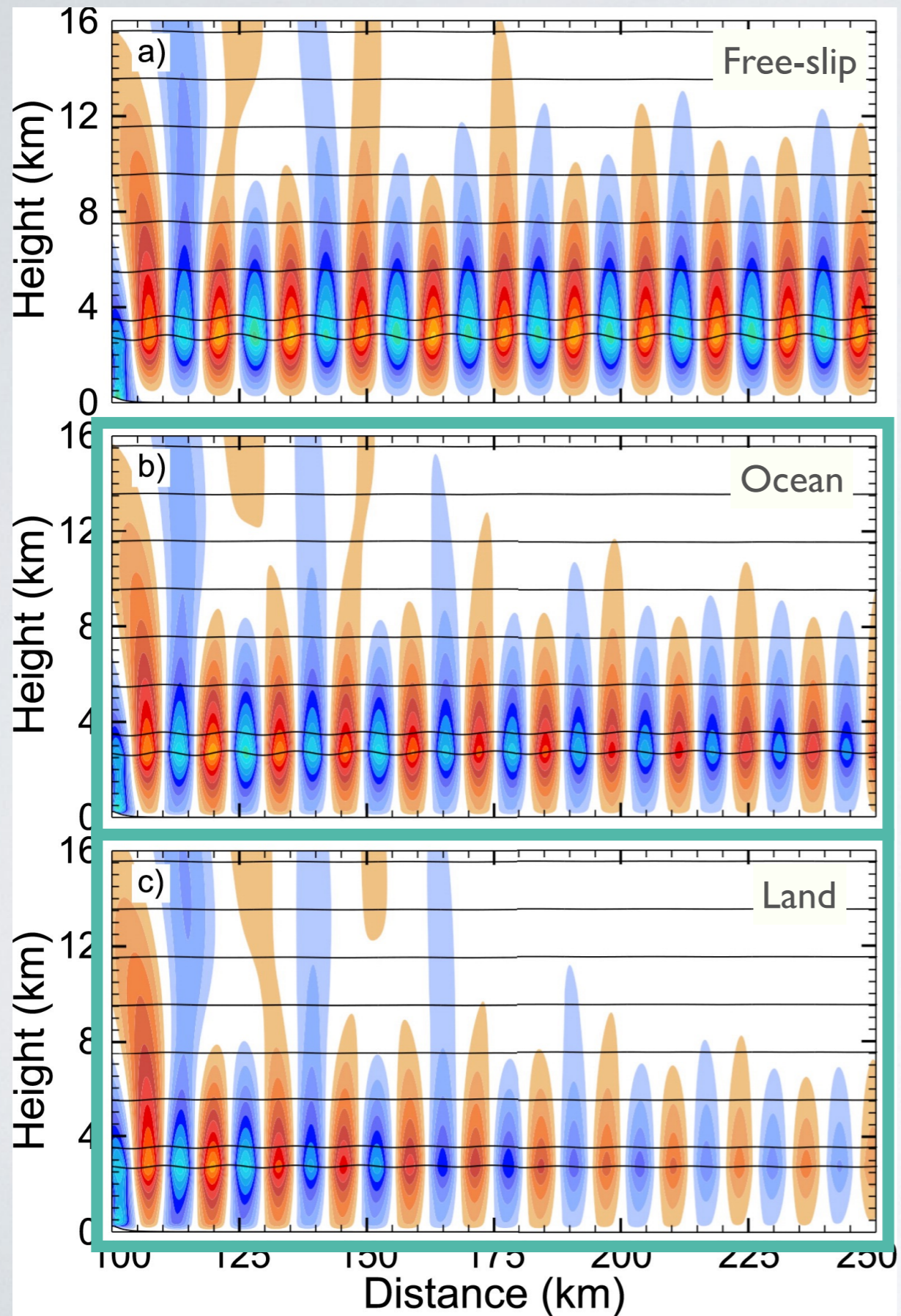
- Weaker winds aloft
- Shorter  $\lambda$  than observed average
- Consider tropopause heights  $z_t$  of 9 and 10 km



# PBL-stratosphere comparison, $z_t = 10$ km

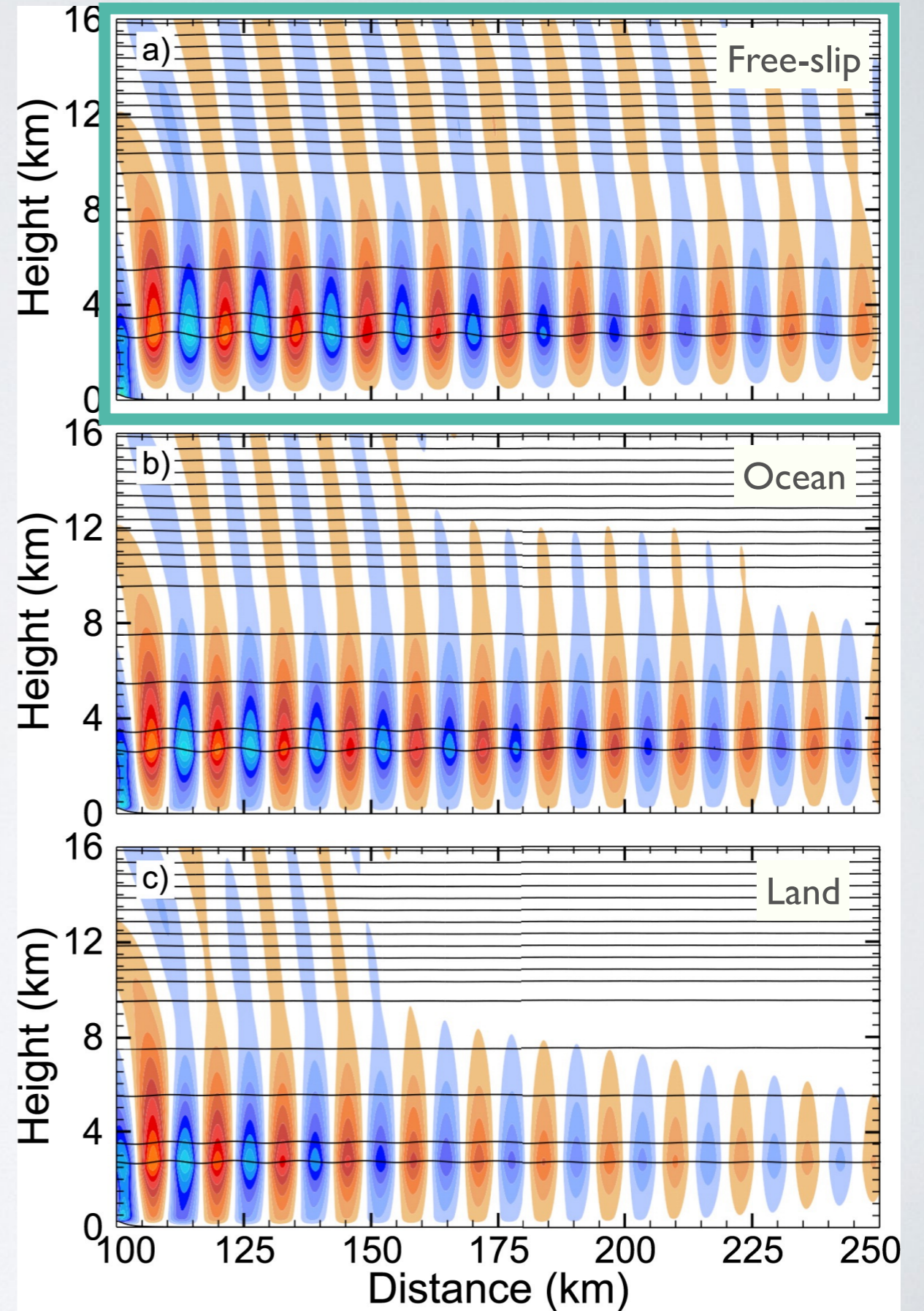
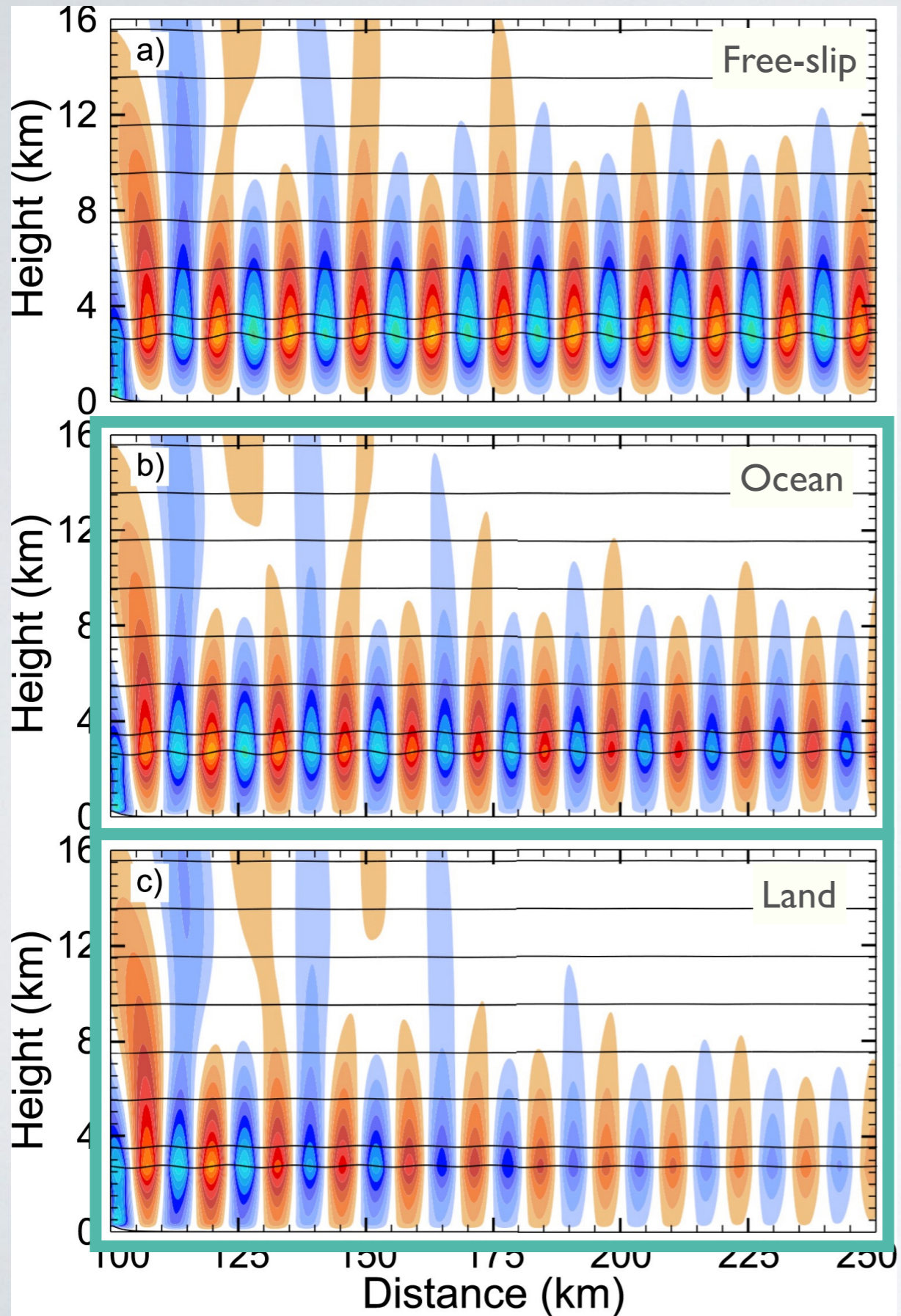


# PBL-stratosphere comparison, $z_t = 10$ km



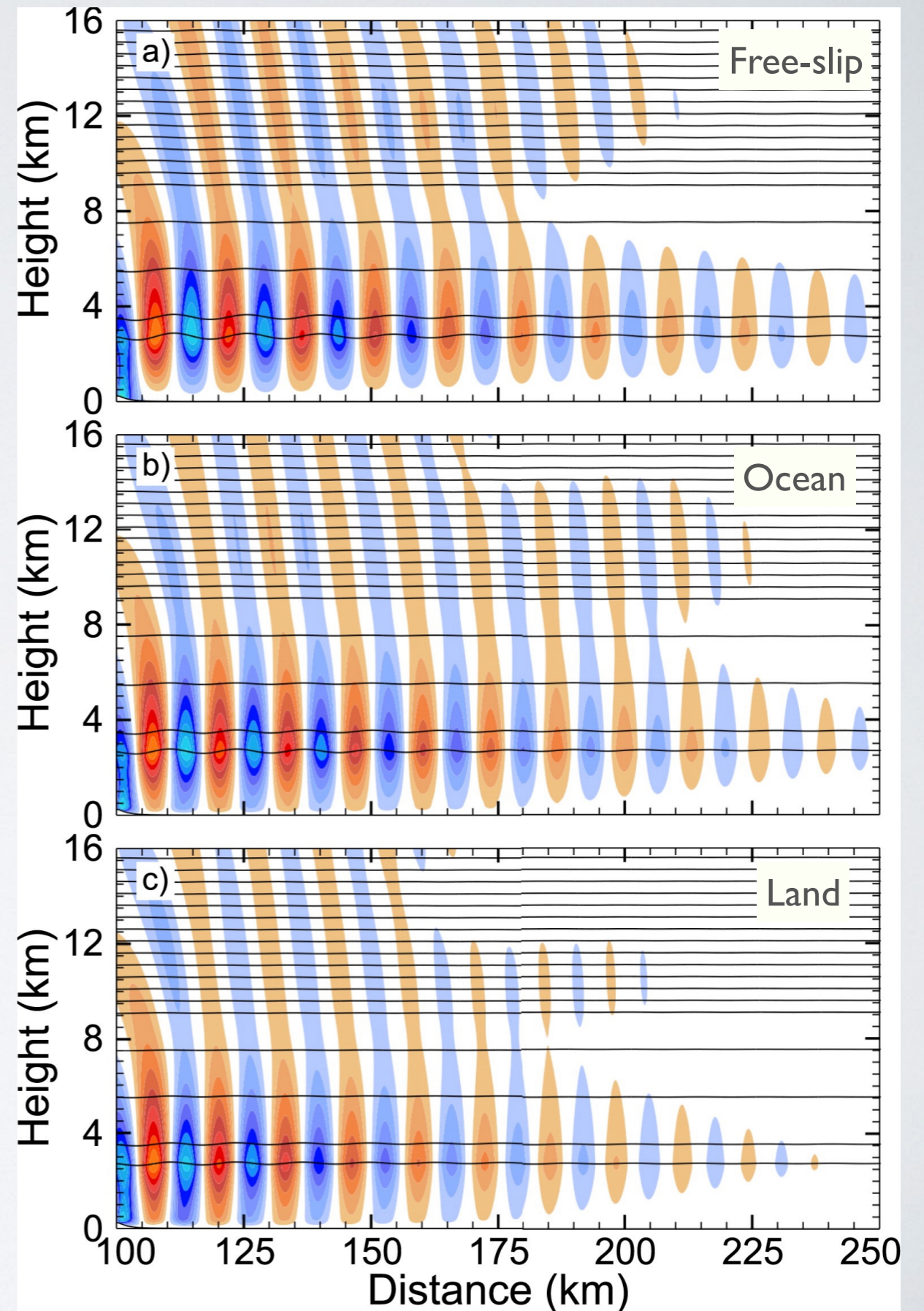
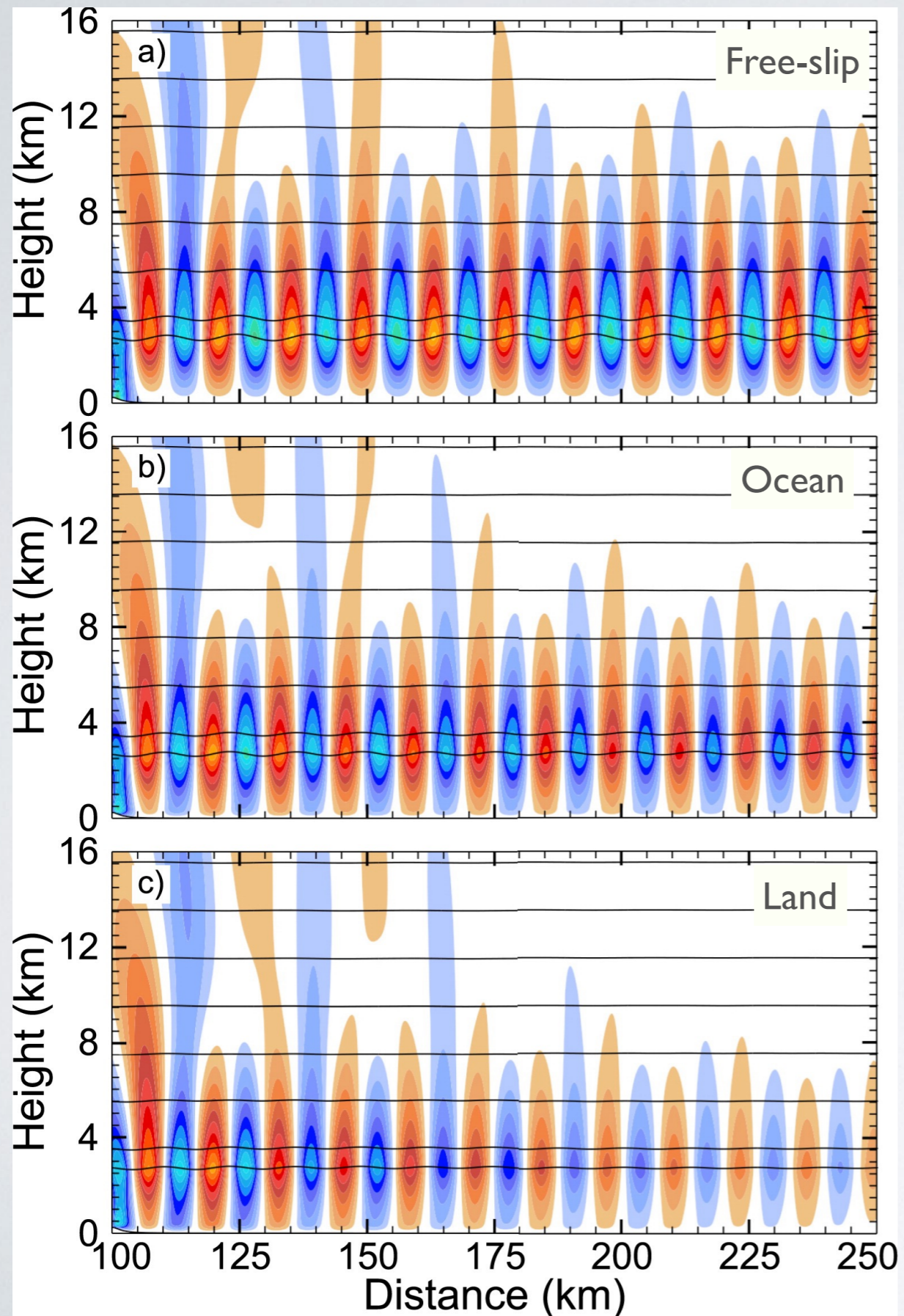
# PBL-stratosphere comparison, $z_t = 10$ km

Leakage  $\sim$  friction

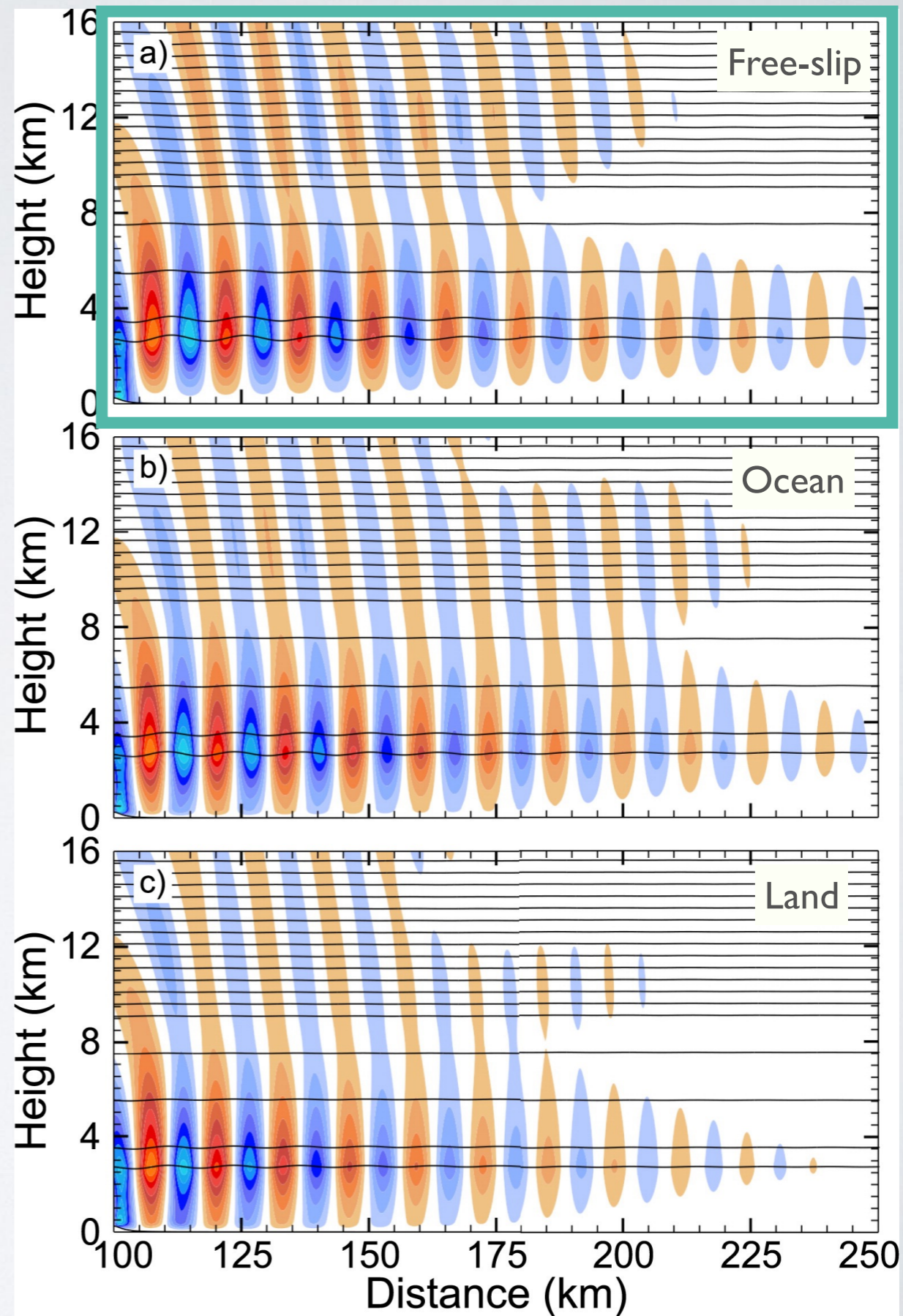
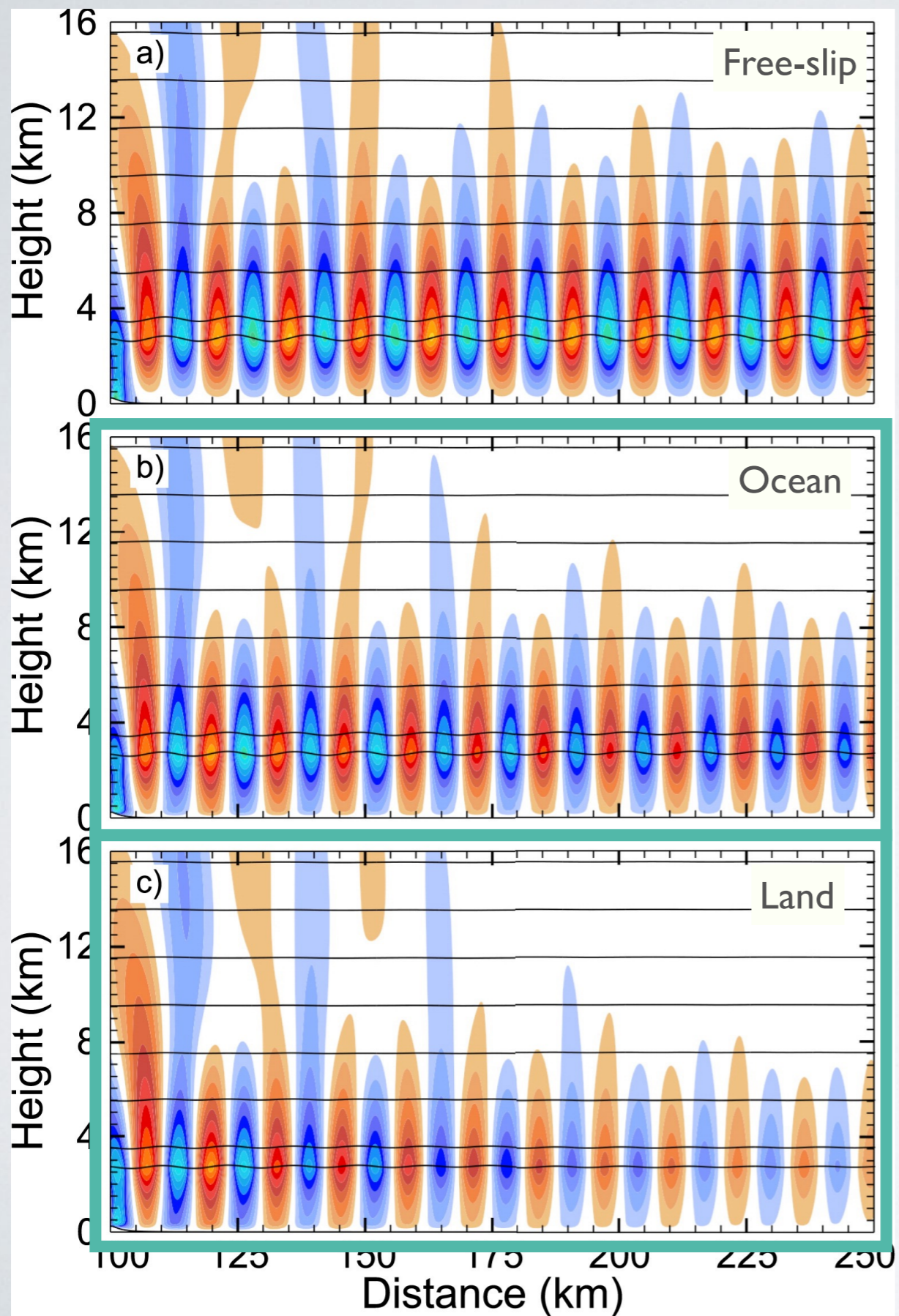




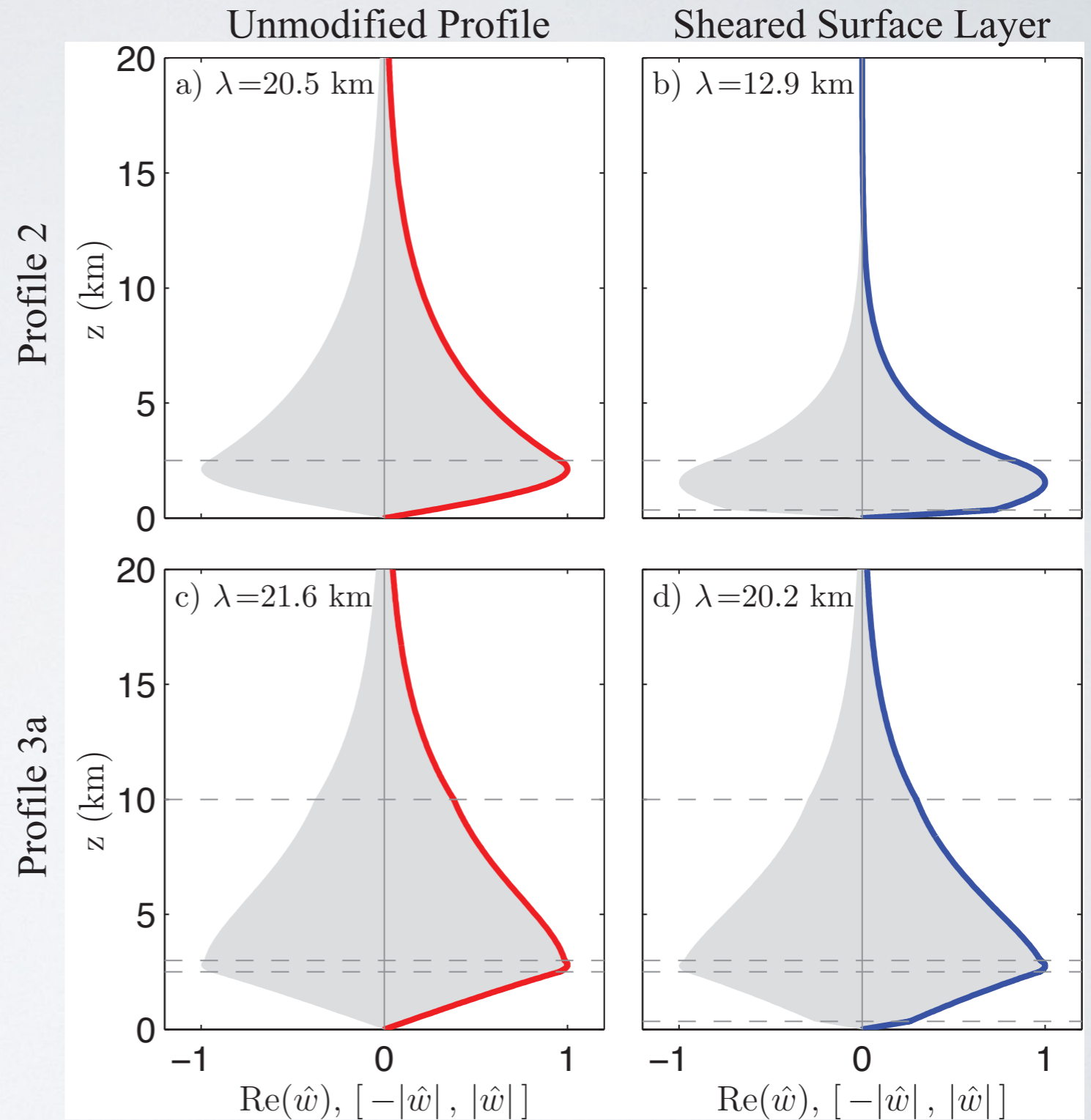
# PBL-stratosphere comparison, $z_t=9$ km



# PBL-stratosphere comparison, $z_t=9$ km Leakage dominates

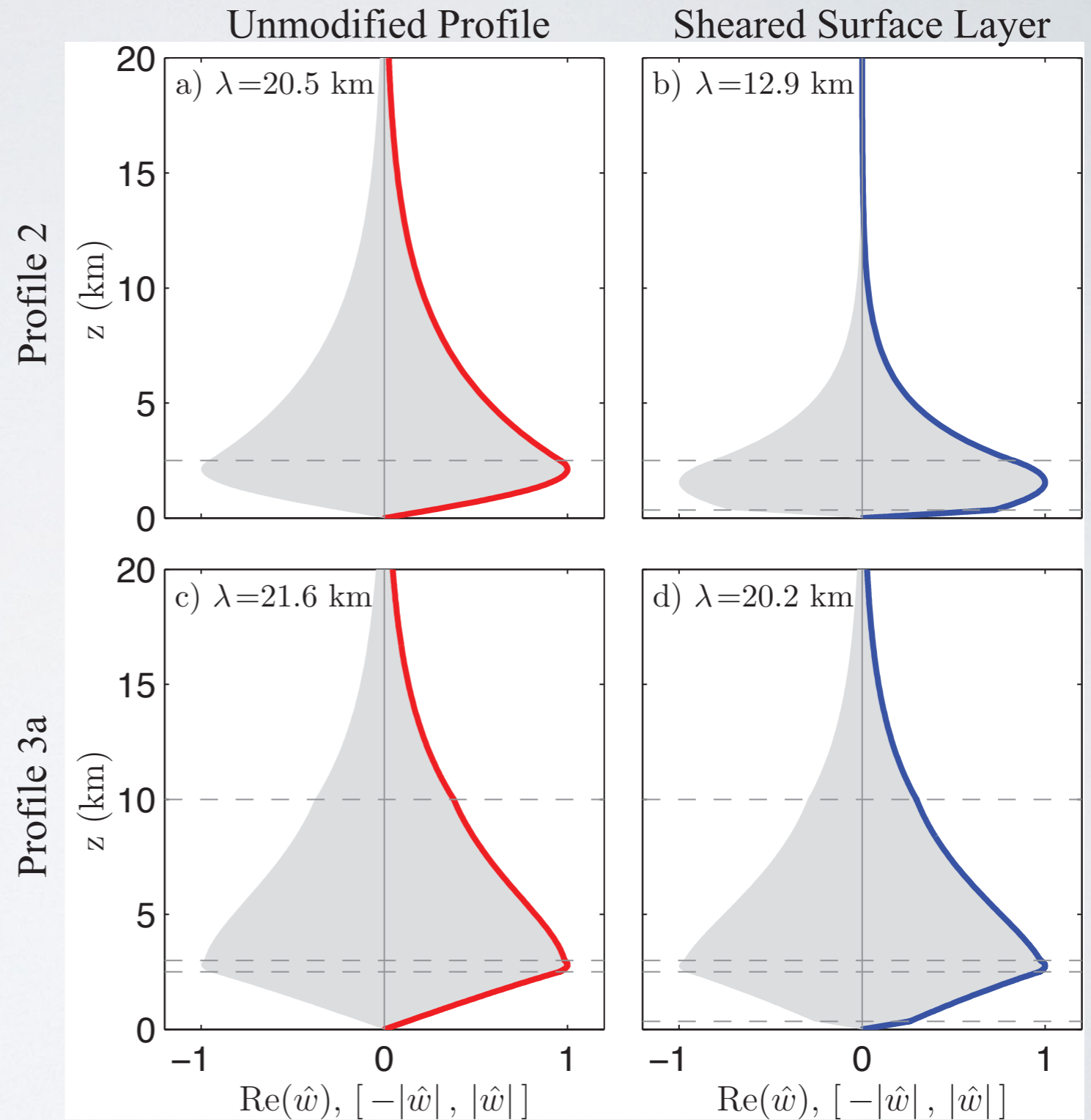


# Surface friction reduces $\lambda$ by changing the mean low-level wind



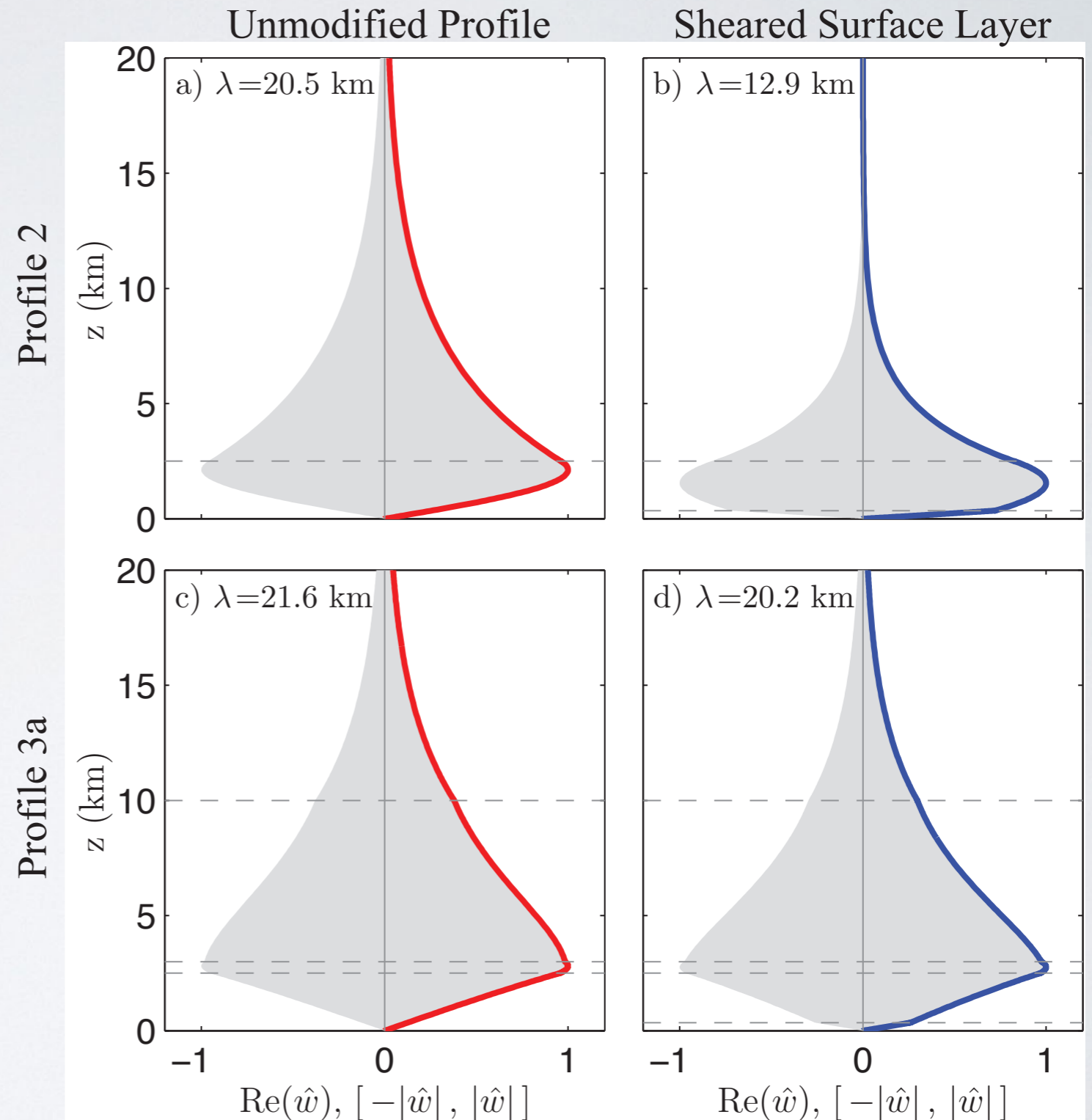
# Surface friction reduces $\lambda$ by changing the mean low-level wind

- Inviscid problem with friction induced low-level shear layer predicts modified  $\lambda$ .



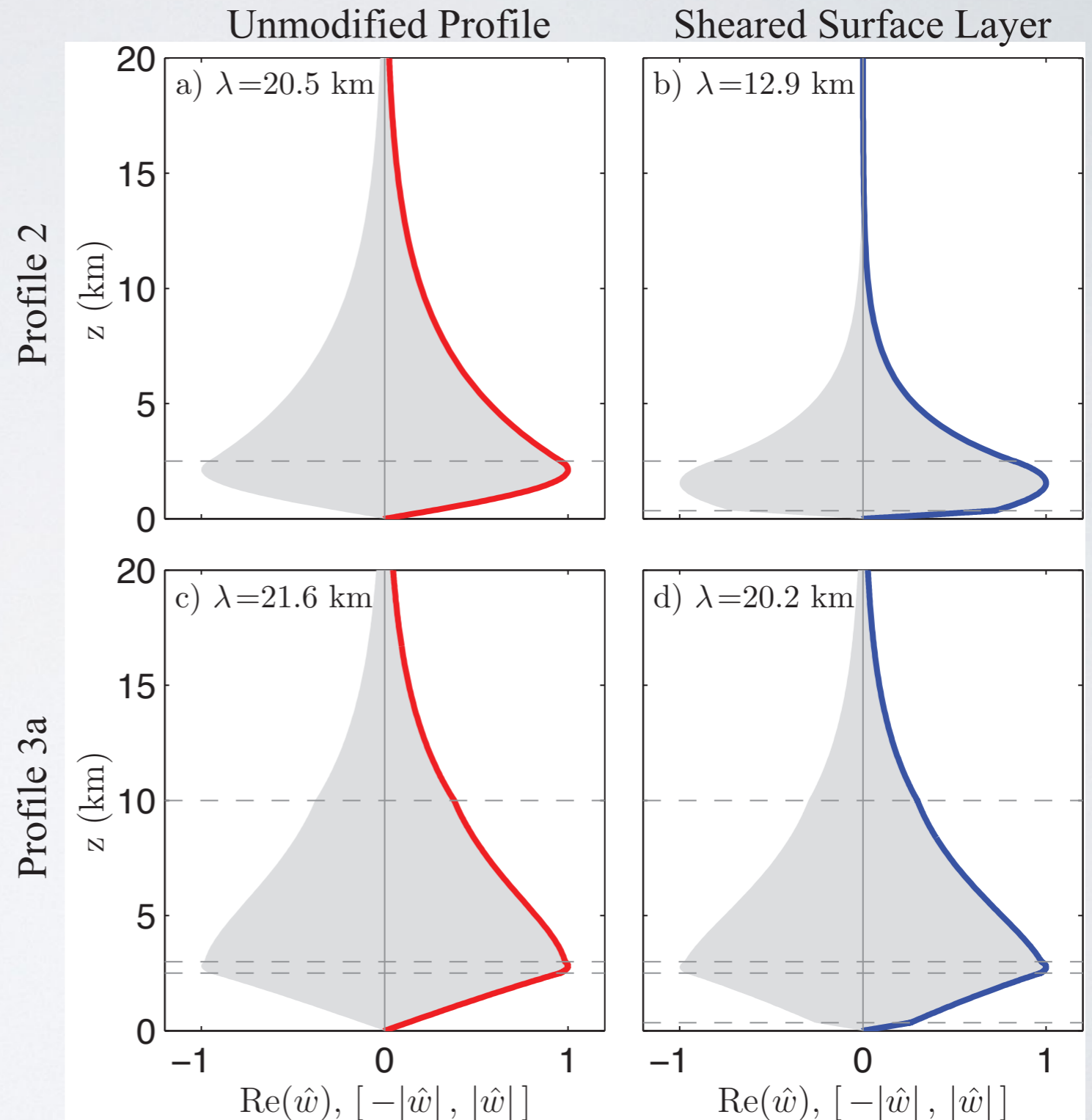
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- Large change in low-level vertical wavelength in 2-layer case where
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- Large change in low-level vertical wavelength in 2-layer case where
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  - large reduction in  $\lambda_i$
- Little change low-level vertical wavelength with elevated inversion
  - little reduction in  $\lambda_i$



# Conclusions

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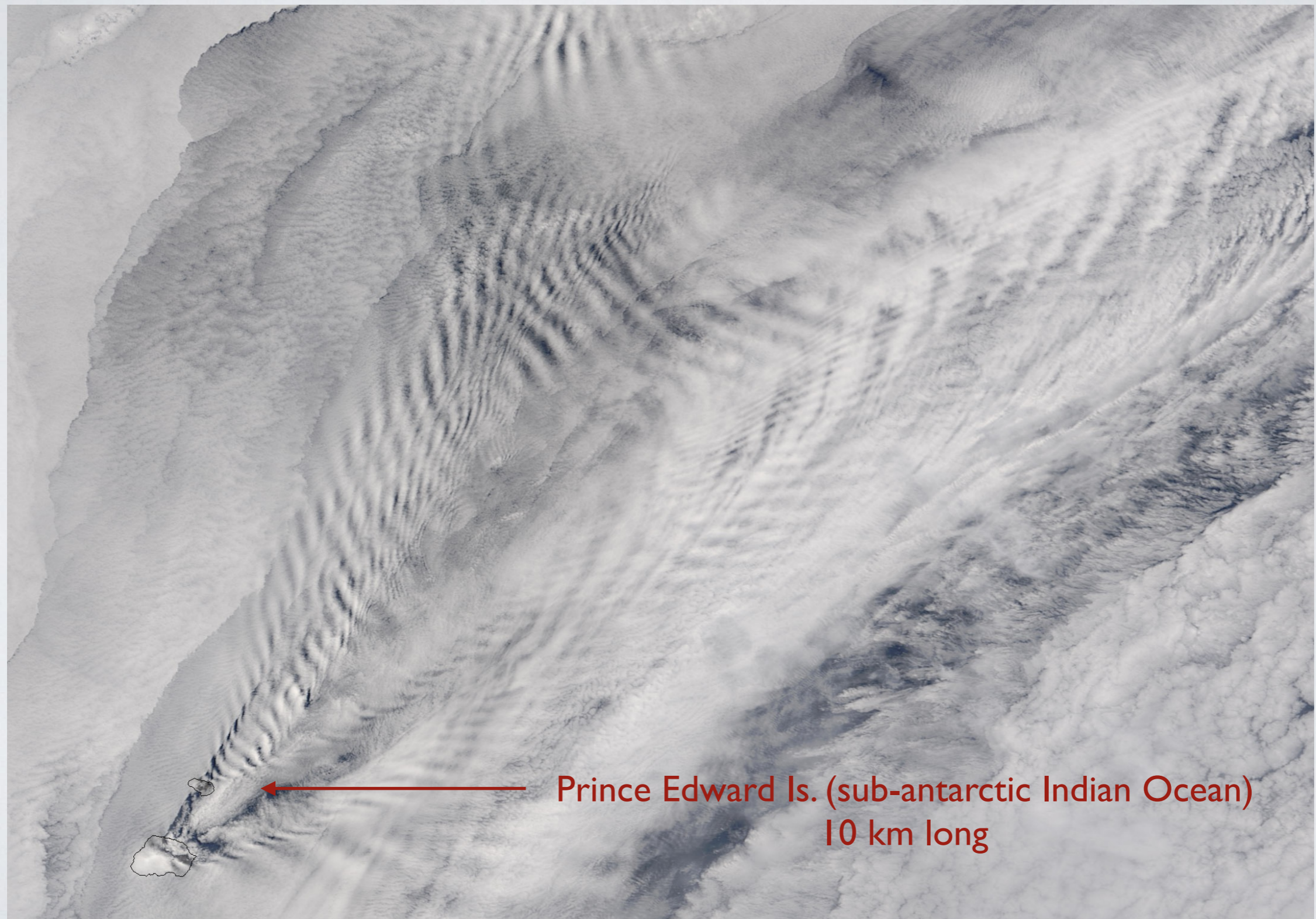
- Boundary layer friction is most important
  - For short wavelengths ( $\lambda$  approaching 8 km from above)
  - In idealized problems with high low-level static stability where the BL friction greatly reduces  $\lambda$



# Conclusions

- Boundary layer friction is most important
  - For short wavelengths ( $\lambda$  approaching 8 km from above)
  - In idealized problems with high low-level static stability where the BL friction greatly reduces  $\lambda$
- Stratospheric leakage is most important
  - For long wavelengths ( $\lambda$  approaching 28 km from below)
  - In cases with elevated inversions, where BL friction shows little tendency to reduce  $\lambda$ .

# Low BL friction key factor in length of oceanic lee-wave trains?



Prince Edward Is. (sub-antarctic Indian Ocean)  
10 km long

# Further Reading

Durran, D.R., M.O.G. Hills, and P.N. Blossey, 2015: The dissipation of trapped lee waves. Part I: Leakage of inviscid waves into the stratosphere. *J. Atmos. Sci.*, **72**, 1569-1584.

Hills, M.O.G., D.R. Durran and P.N. Blossey, 2016: The dissipation of trapped lee waves. Part II: The relative importance of the boundary layer and the stratosphere. *J. Atmos. Sci.*, **73**, 943-955.