



2016 SPARC GW symposium

Momentum flux of Convective Gravity Waves: Spatiotemporal Variations at Source-level and Dissipation in the Stratosphere

Min-Jee Kang and Hye-Yeong Chun

Department of Atmospheric Sciences, Yonsei University, Seoul, South Korea

kangmj@yonsei.ac.kr

Introduction

- **Parameterizations** of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) showed that momentum flux of CGWs at the source-level (cloud-top) (**CTMF**) is determined not only from **convective source** but also from wave-filtering and resonance factor (**WFRF**).
- Choi and Chun (2011) updated and validated Song and Chun (2005) by comparing CTMF spectra with those from **3-D mesoscale simulation**.
- Implementation of this parameterization to global climate model (GCM) reproduced quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013).
- In this study, we focus on understanding CTMF spectrum and its **variations** through the **long-term off-line** calculation of **updated version of Choi and Chun (2011)**. Also we show the connection between CTMF spectrum and the gravity-wave drag (**GWDC**) in the stratosphere.


Introduction

- **Parameterizations** of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) showed that momentum flux of CGWs at the source-level (cloud-top) (**CTMF**) is determined not only from **convective source** but also from wave-filtering and resonance factor (**WFRF**).
- Choi and Chun (2011) updated and validated Song and Chun (2005) by comparing CTMF spectra with those from **3-D mesoscale simulation**.
- Implementation of this parameterization to global climate model (GCM) reproduced quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013). → **On-line test**
- In this study, we focus on understanding CTMF spectrum and its **variations** through the **long-term off-line** calculation of **updated version of Choi and Chun (2011)**. Also we show the connection between CTMF spectrum and the gravity-wave drag (**GWDC**) in the stratosphere.

Introduction

- **Parameterizations** of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) showed that momentum flux of CGWs at the source-level (cloud-top) (**CTMF**) is determined not only from **convective source** but also from wave-filtering and resonance factor (**WFRF**).
- Choi and Chun (2011) updated and validated Song and Chun (2005) by comparing CTMF spectra with those from **3-D mesoscale simulation**.
- Implementation of this parameterization to global climate model (GCM) reproduced quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013). → **On-line test**
- In this study, we focus on understanding CTMF spectrum and its **variations** through the **long-term off-line** calculation of **updated version of Choi and Chun (2011)**. Also we show the connection between CTMF spectrum and the gravity-wave drag (**GWDC**) in the stratosphere.

Objectives

1. Parameterization of physically, mathematically consistent source-level gravity wave momentum flux (CTMF) spectrum
 2. Off-line calculation of CTMF with realistic background
- 

1. To understand **which factors determine** CTMF spectrum
2. To understand **variabilities of CTMF** itself
3. To know how the source spectrum (CTMF) and background condition contribute to the **GWDC** in the stratosphere

Data and methodology

Data	CFSR (NCEP Climate Forecast System Reanalysis)
Period	1979.01-2010.12 (2002.01-2010.12)
Horizontal resolution	0.5° × 0.5° (zonal wind, meridional wind, temperature, geopotential height, cloud top pressure, cloud bottom pressure) 1° × 1° (deep convective heating rate)
Temporal resolution	1 hour (6-hourly analysis, 1-hourly forecast)
Vertical resolution	37 pressure levels (1000 hPa ~ 1 hPa)

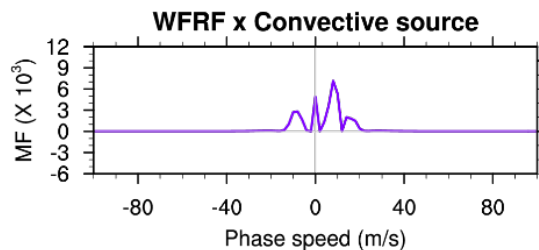
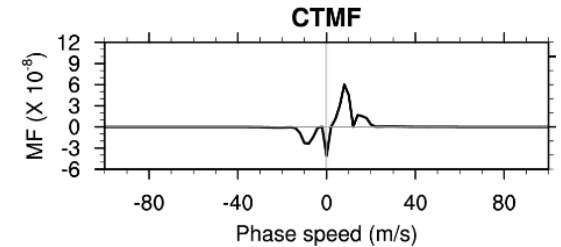
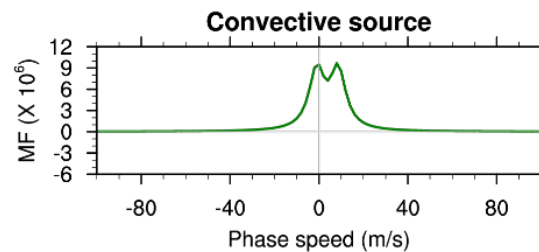
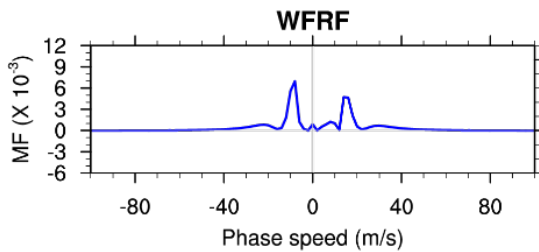
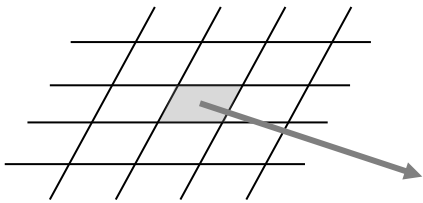
Data and methodology

Parameterization: CTMF (cloud-top GWMF)

Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source



Data and methodology

Parameterization: CTMF (cloud-top GWMF)

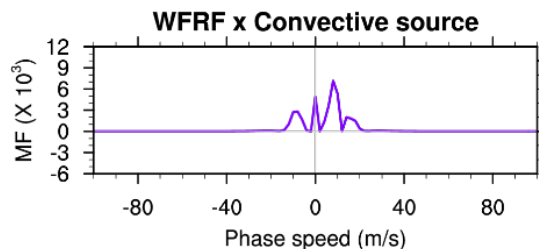
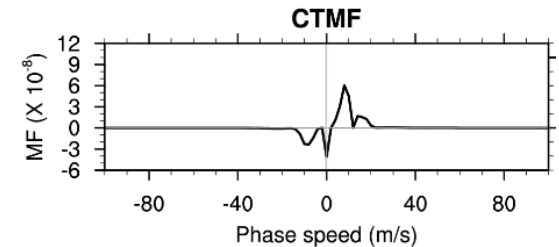
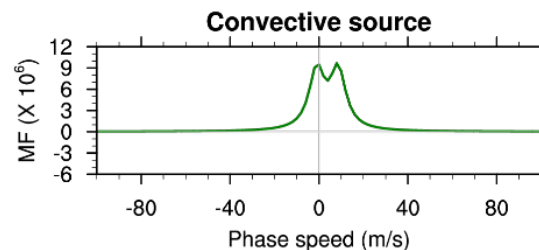
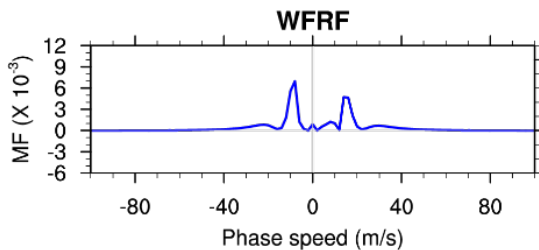
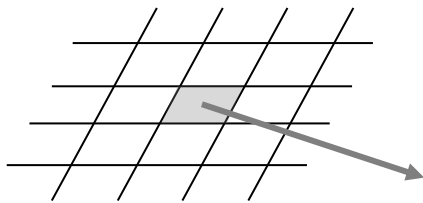
Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF)

Convective source

Determine spectral shape of CTMF



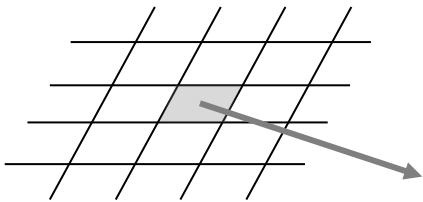
Data and methodology

Parameterization: CTMF (cloud-top GWMF)

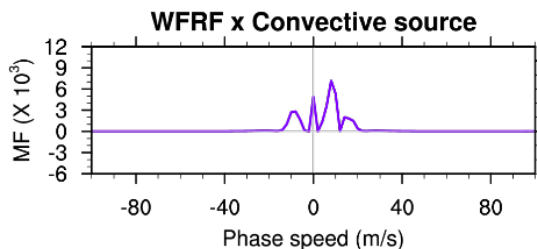
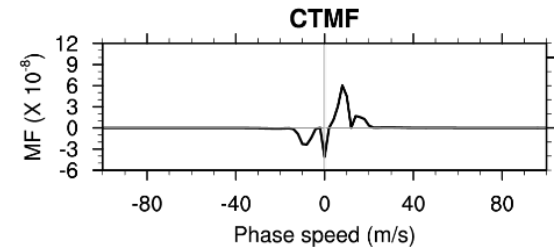
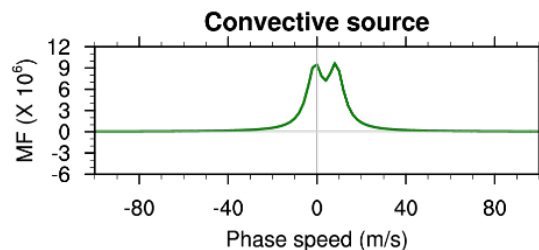
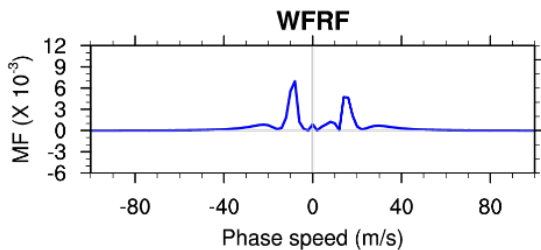
Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source Nonlinear forcing effect
 (Chun et al. 2008)



Determine spectral shape of CTMF



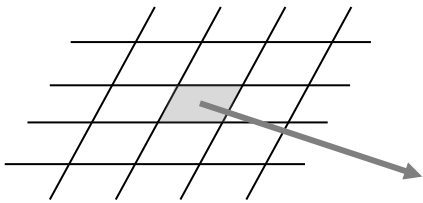
Data and methodology

Parameterization: CTMF (cloud-top GWMF)

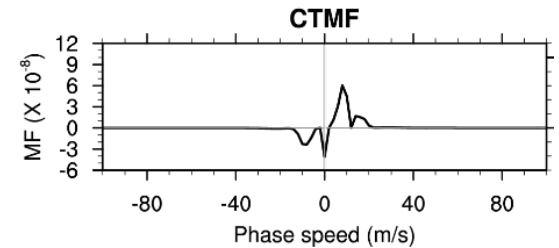
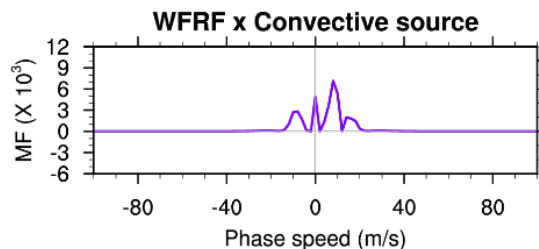
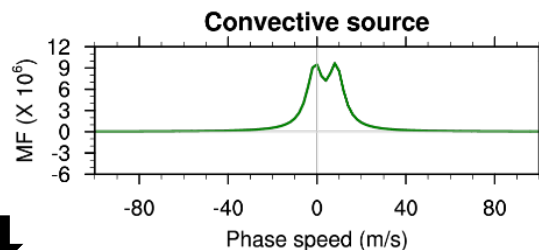
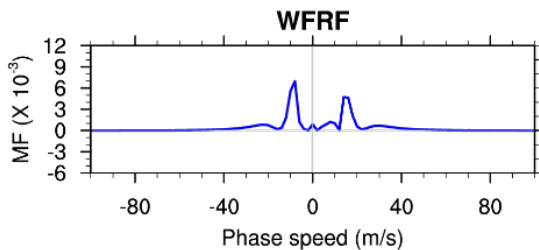
Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source Nonlinear forcing effect
 (Chun et al. 2008)



Determine spectral shape of CTMF



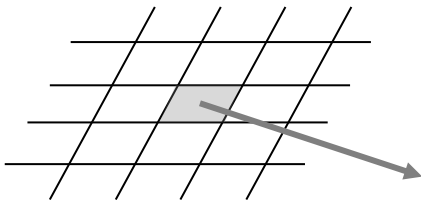
Data and methodology

Parameterization: CTMF (cloud-top GWMF)

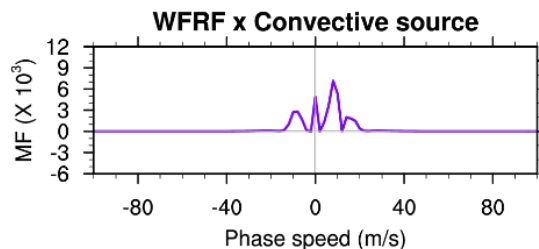
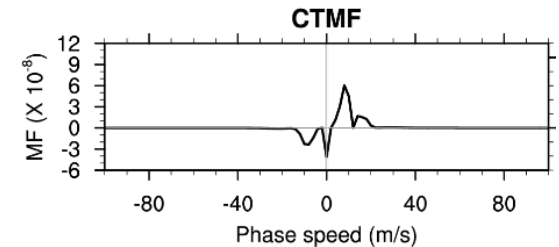
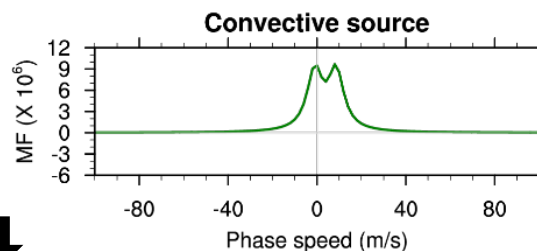
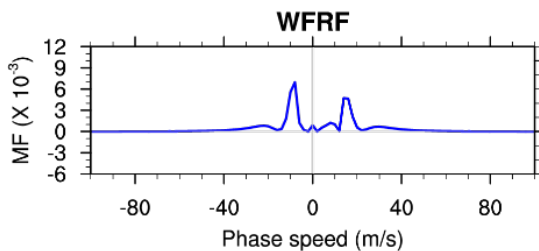
Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source Nonlinear forcing effect
 (Chun et al. 2008)



Determine spectral shape of CTMF



Sign & magnitude
 $\text{sgn}[c - U] \times \text{Nonlinear forcing effect} \times$
 Several conditions within convection

Data and methodology

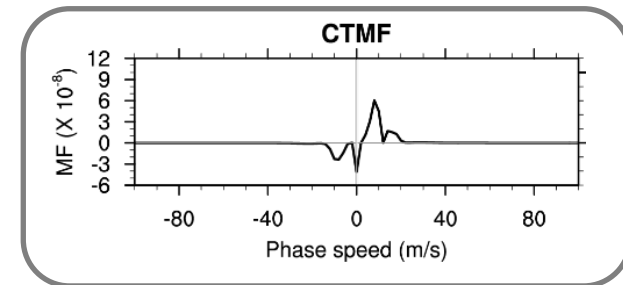
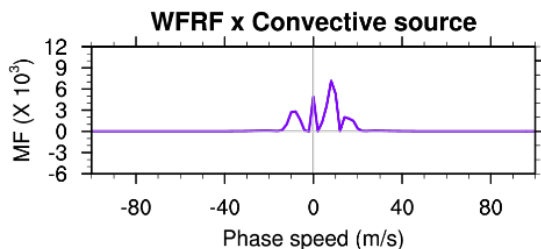
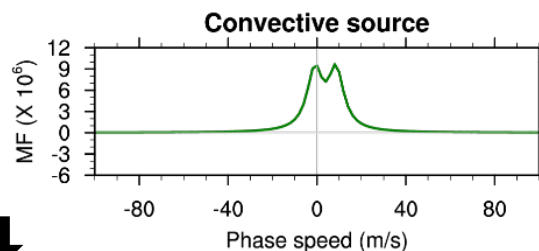
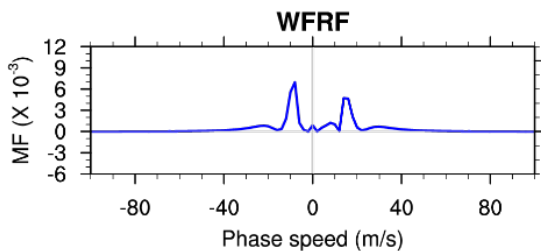
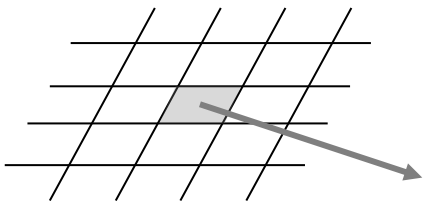
Parameterization: CTMF (cloud-top GWMF)

Choi and Chun (2011) + nonlinear forcing effect

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source Nonlinear forcing effect
 (Chun et al. 2008)

Determine spectral shape of CTMF



Sign & magnitude
 $\text{sgn}[c - U] \times \text{Nonlinear forcing effect} \times$
 Several conditions within convection

Data and methodology

Parameterization: CTMF (cloud-top GWMF)

Choi and Chun (2011) + nonlinear forcing effect

$$M_{ct}(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

Wave-filtering and resonance factor (WFRF) Convective source Nonlinear forcing effect

Parameterization: propagation

Lindzen-type method

(Kiehl et al. 1996; Song and Chun, 2006)

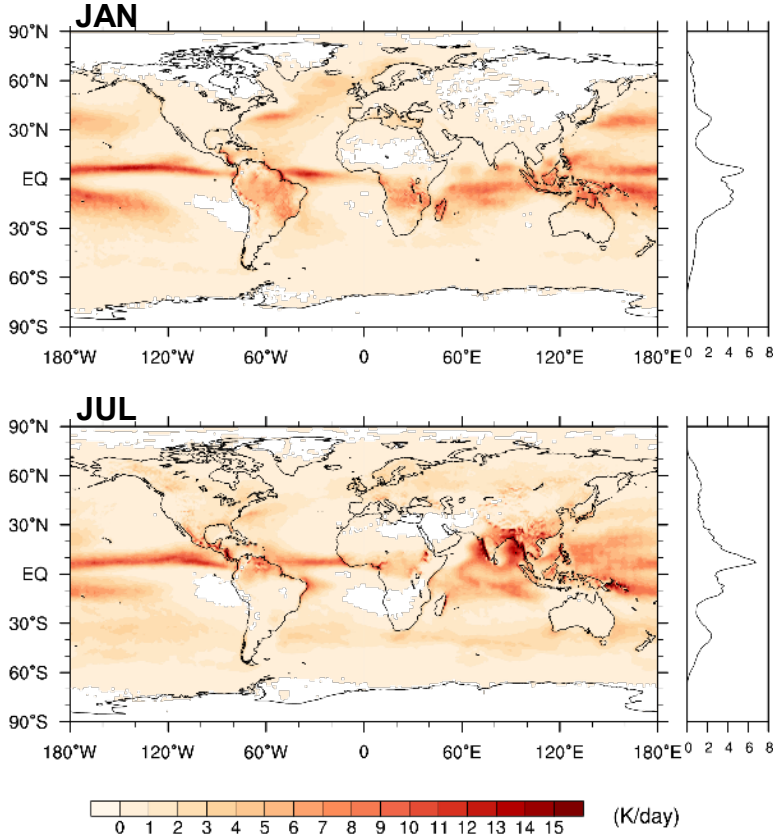
Columnar propagation

Spatiotemporal variations

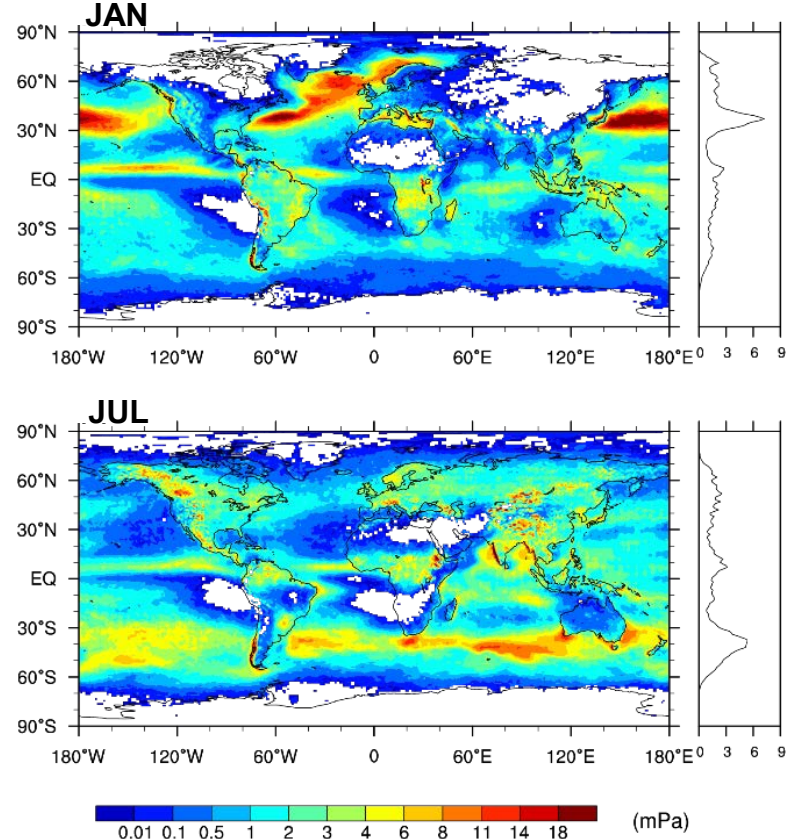
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source \propto DCH

Deep Convective Heating rate



Absolute CTMF



2002-2010 avg.

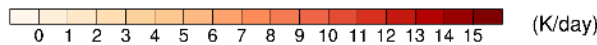
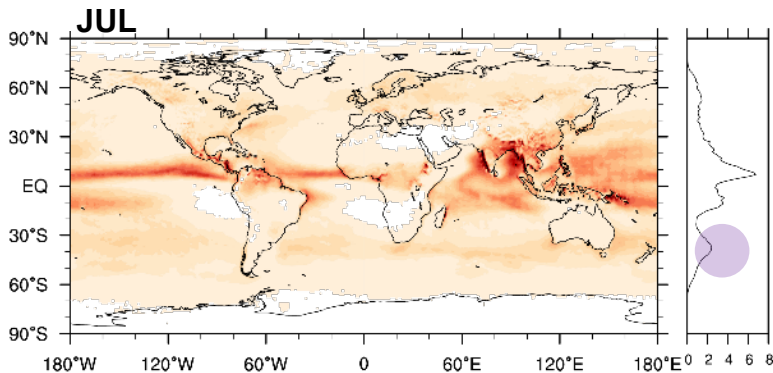
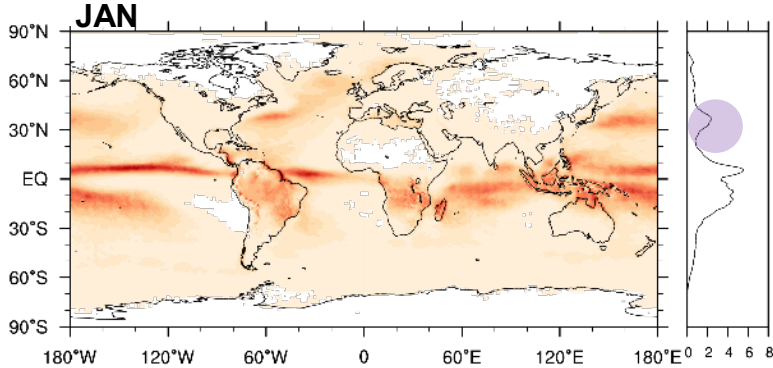
- **CTMF** is not solely proportional to **DCH**.
- **WFRF** (wave-filtering and resonance factor), several conditions within convection (T_q , N_q), and nonlinearity also affect the magnitude of CTMF.

Spatiotemporal variations

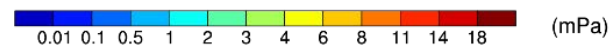
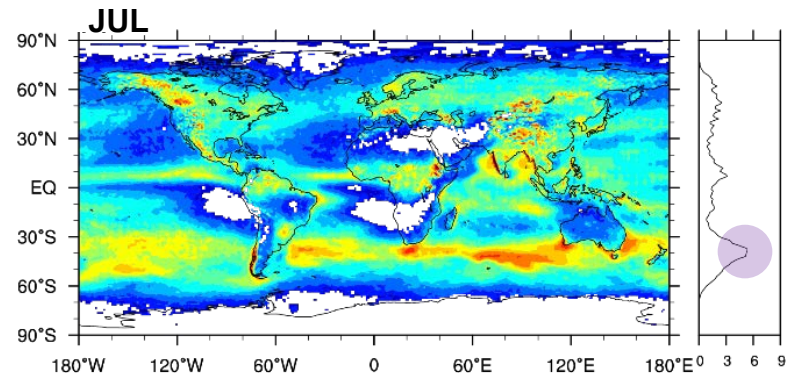
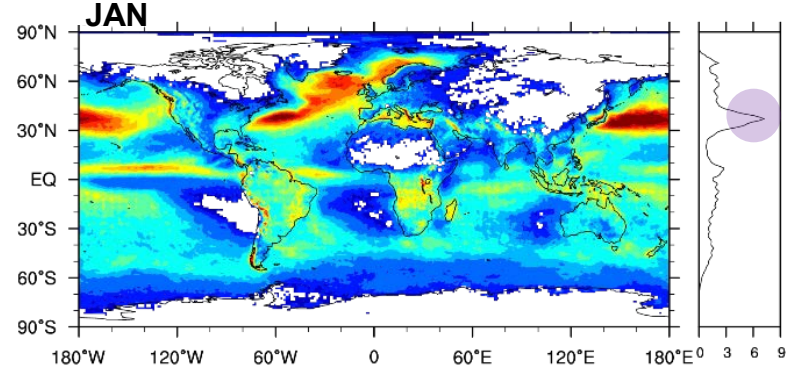
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source \propto DCH

Deep Convective Heating rate



Absolute CTMF



2002-2010 avg.

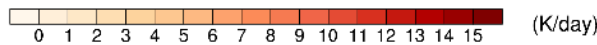
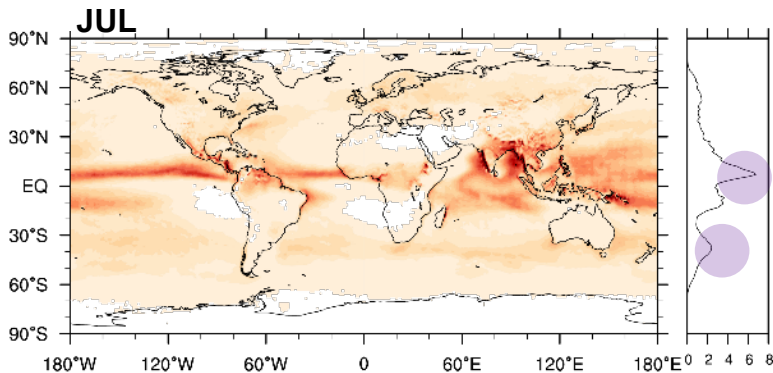
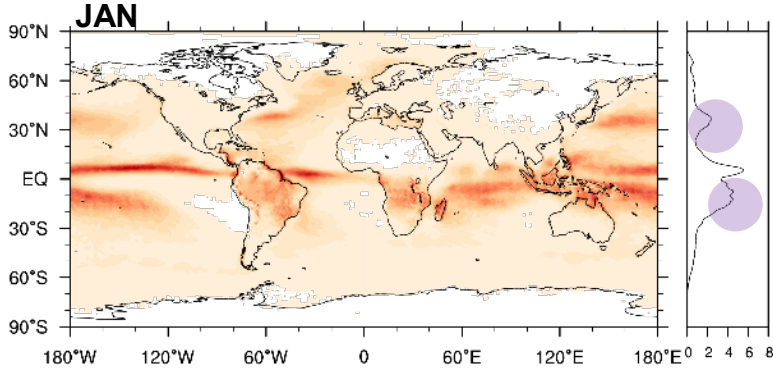
- **CTMF** is not solely proportional to **DCH**.
- **WFRF** (wave-filtering and resonance factor), several conditions within convection (T_q , N_q), and nonlinearity also affect the magnitude of CTMF.

Spatiotemporal variations

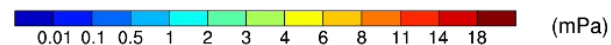
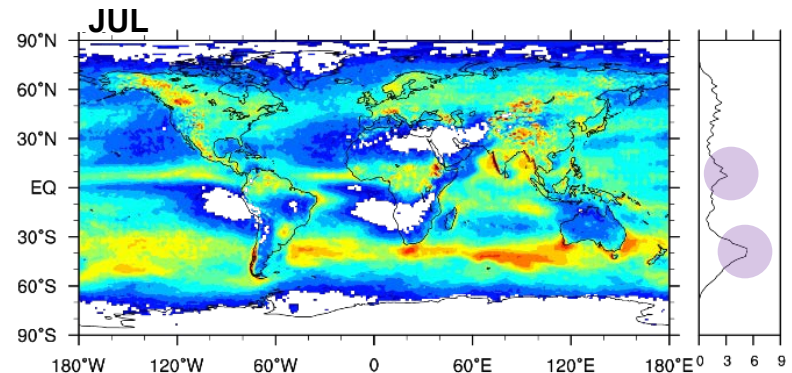
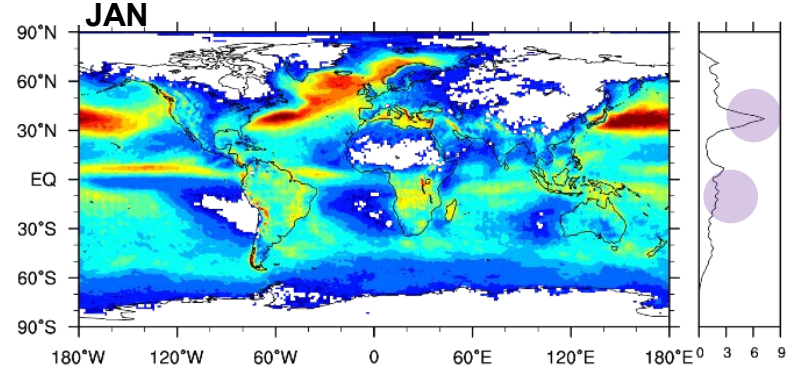
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_{ct} N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source \propto DCH

Deep Convective Heating rate



Absolute CTMF

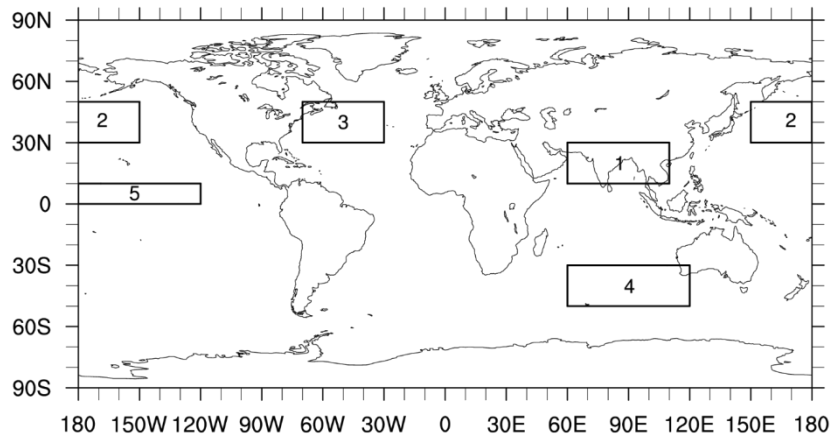


2002-2010 avg.

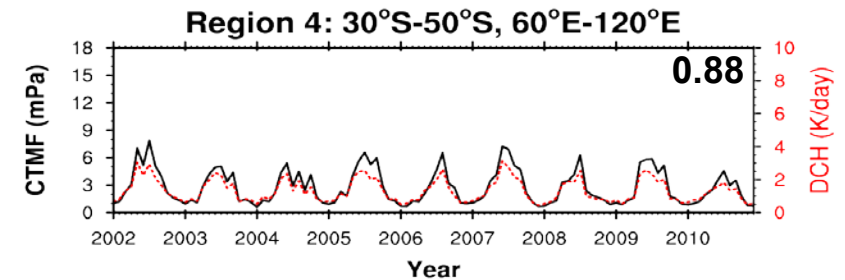
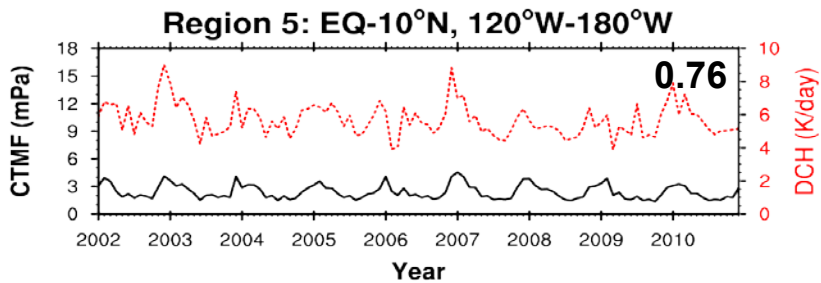
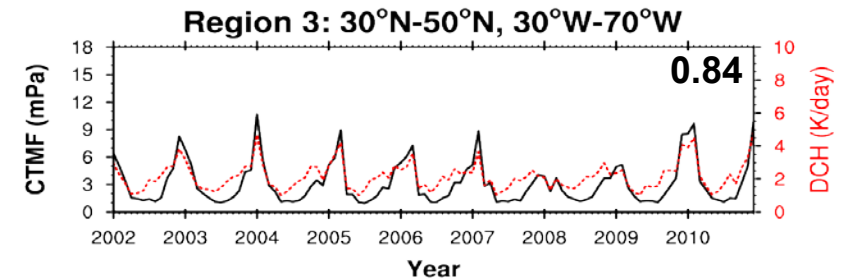
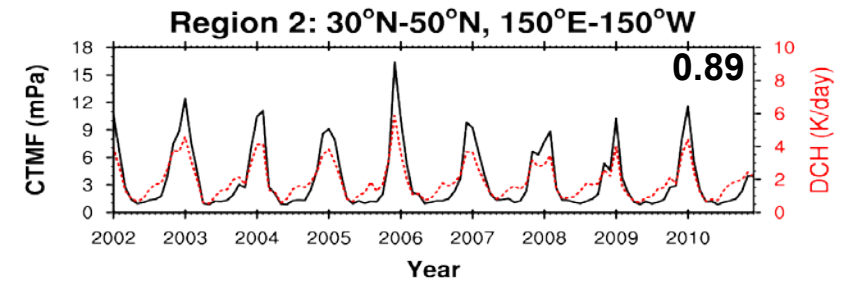
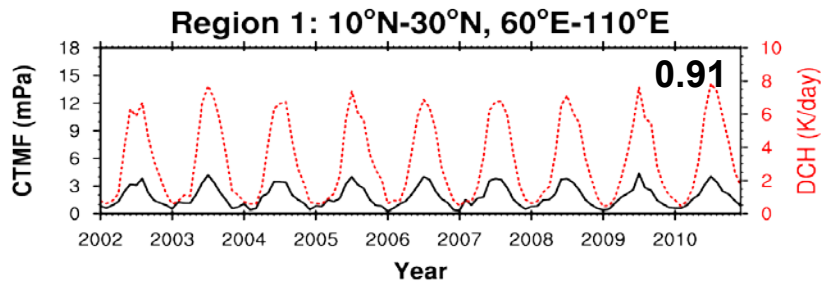
- **CTMF** is not solely proportional to **DCH**.
- **WFRF** (wave-filtering and resonance factor), several conditions within convection (T_q , N_q), and nonlinearity also affect the magnitude of CTMF.

Spatiotemporal variations

Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5).
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.

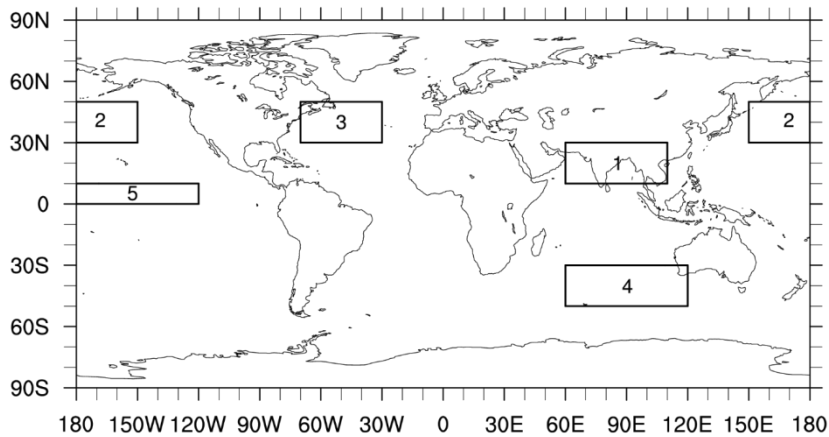


Low latitudes

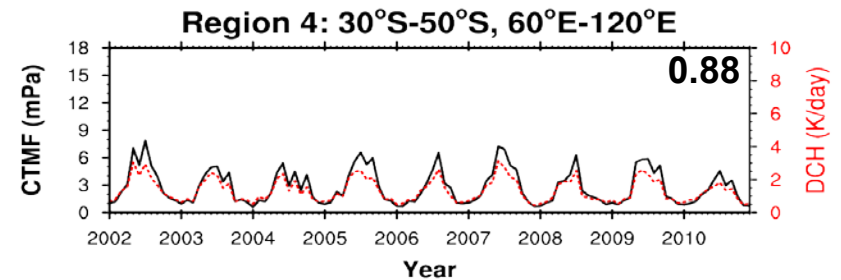
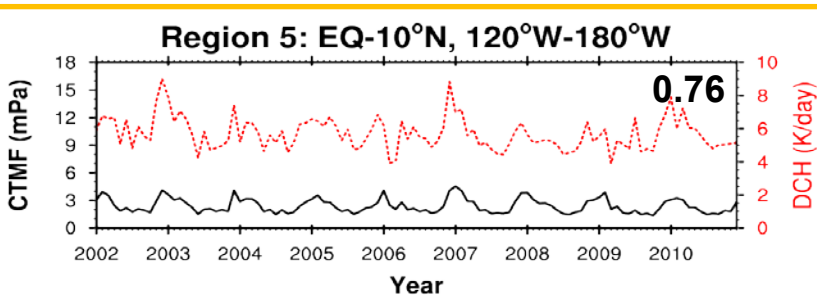
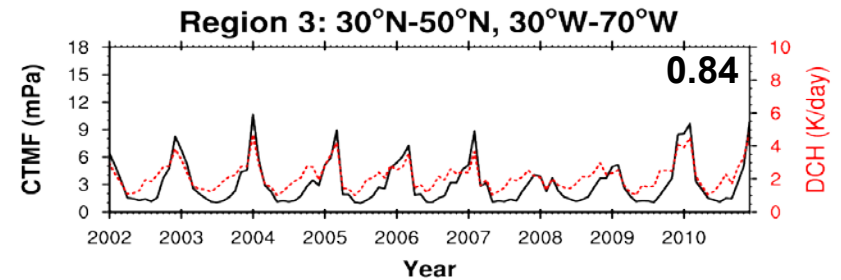
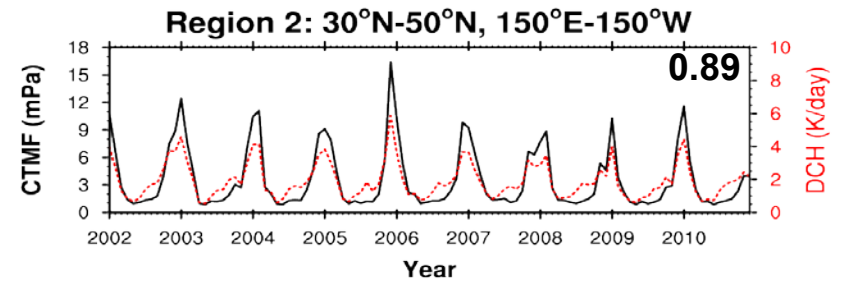
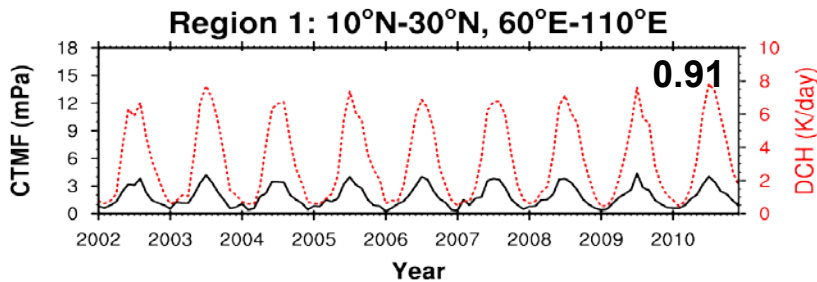
Storm-track region (midlatitudes)

Spatiotemporal variations

Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5).
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.

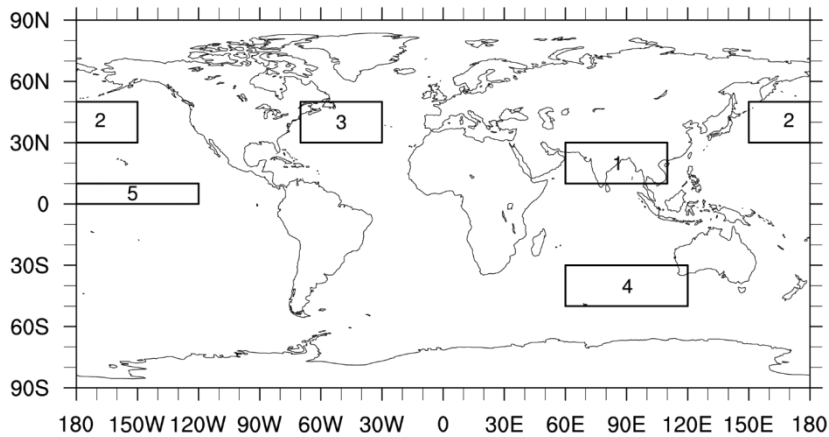


Low latitudes

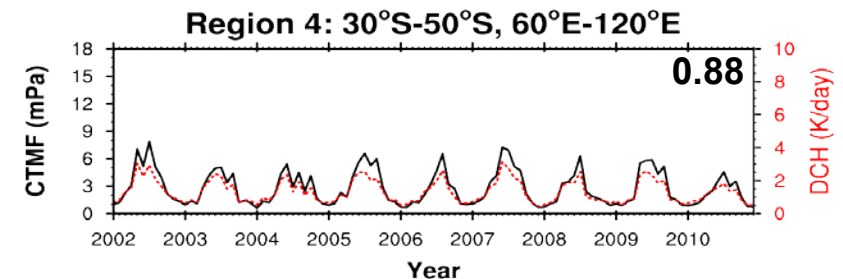
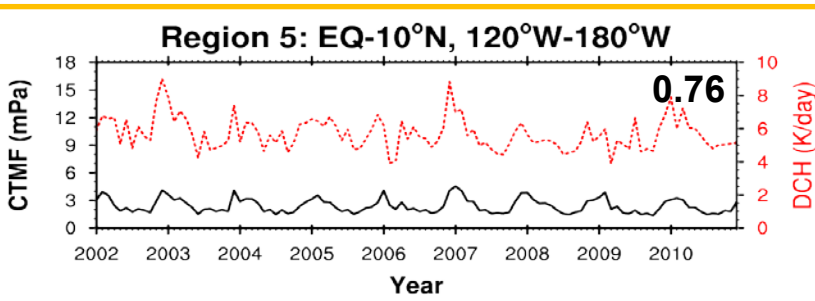
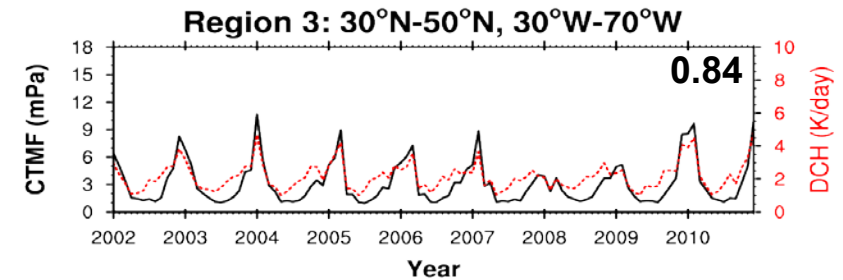
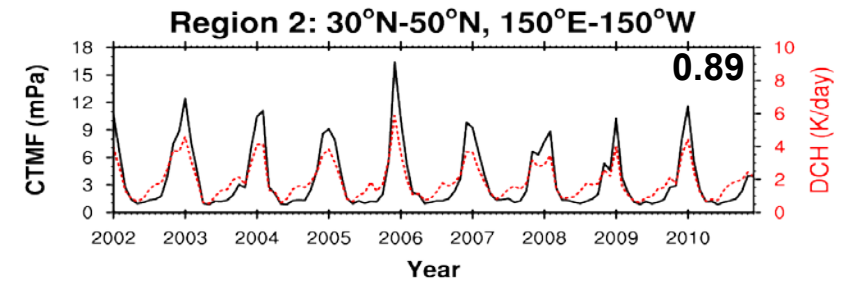
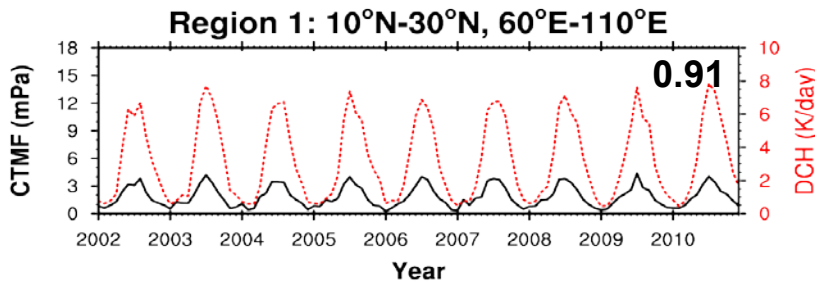
Storm-track region (midlatitudes)

Spatiotemporal variations

Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5). **effect of WFRF**
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.

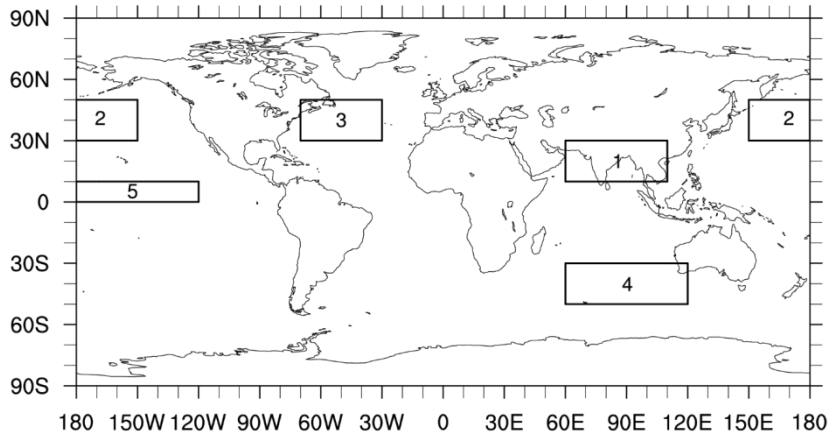


Low latitudes

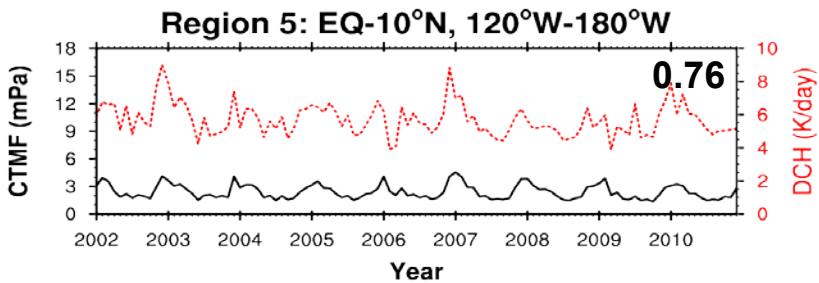
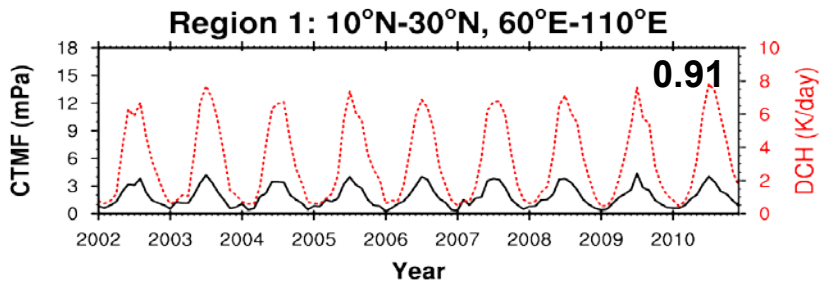
Storm-track region (midlatitudes)

Spatiotemporal variations

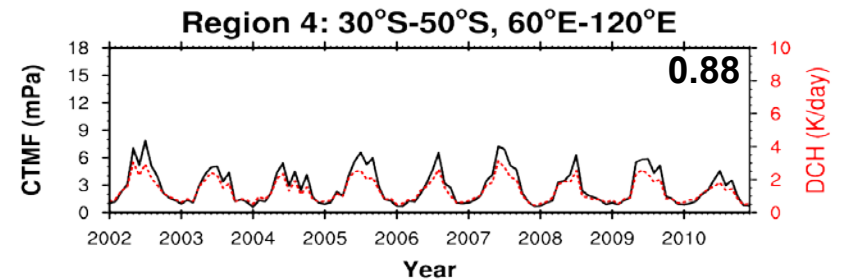
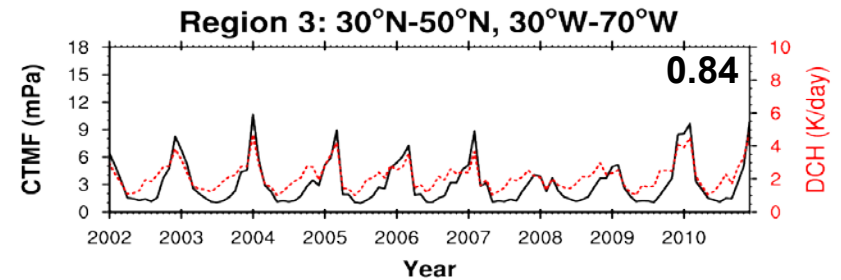
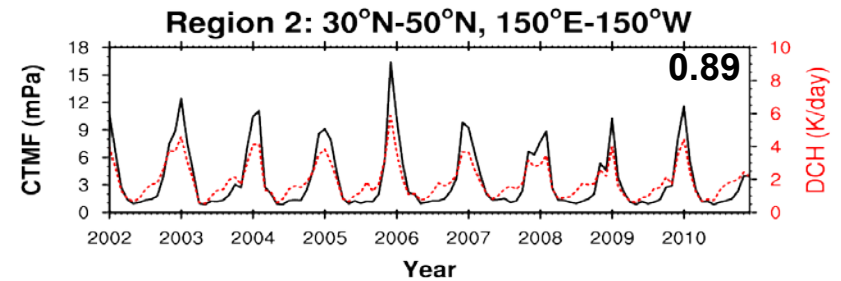
Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5). **effect of WFRF**
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.



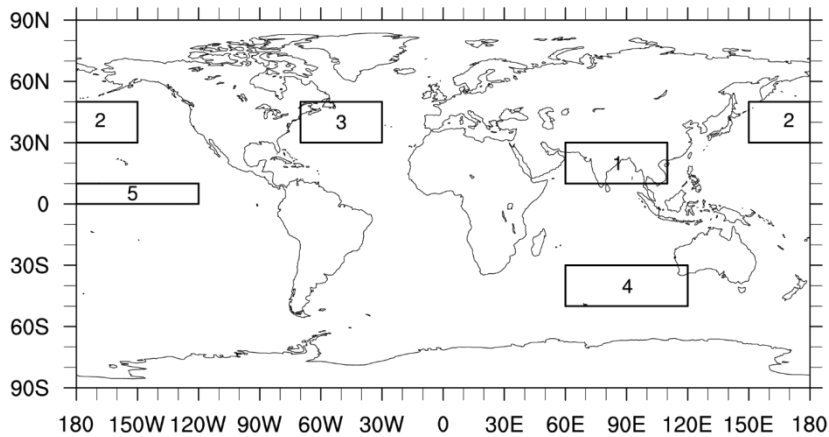
Low latitudes



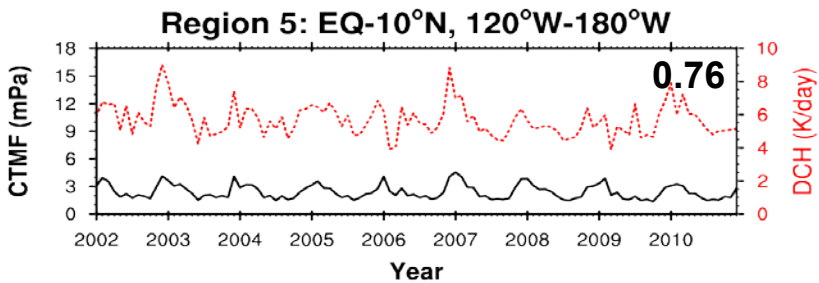
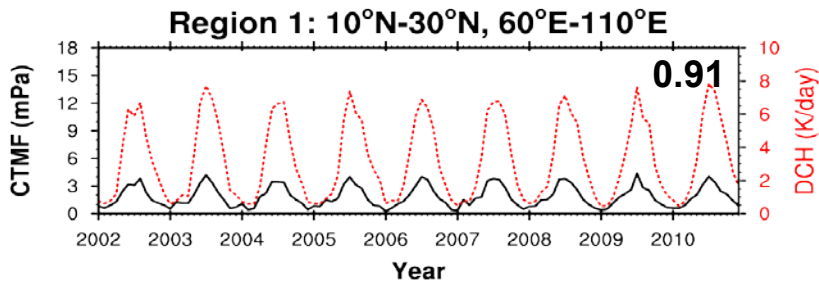
Storm-track region (midlatitudes)

Spatiotemporal variations

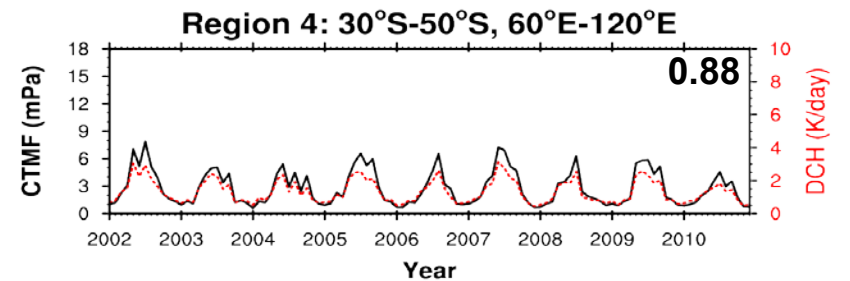
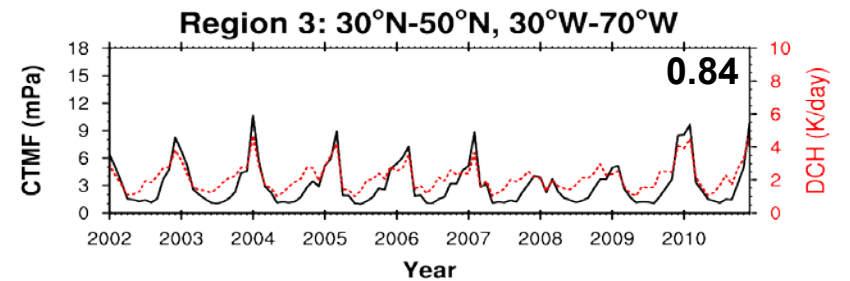
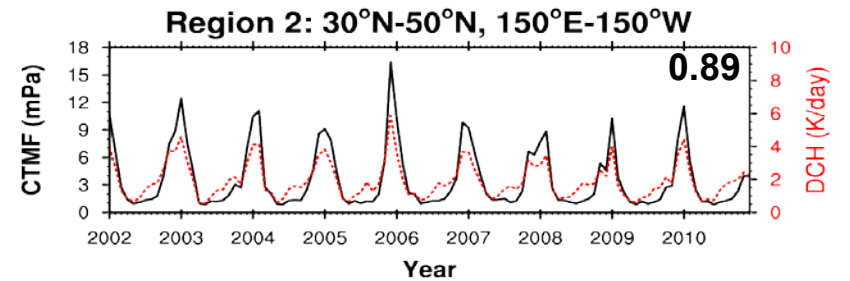
Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5). **effect of WFRF**
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.



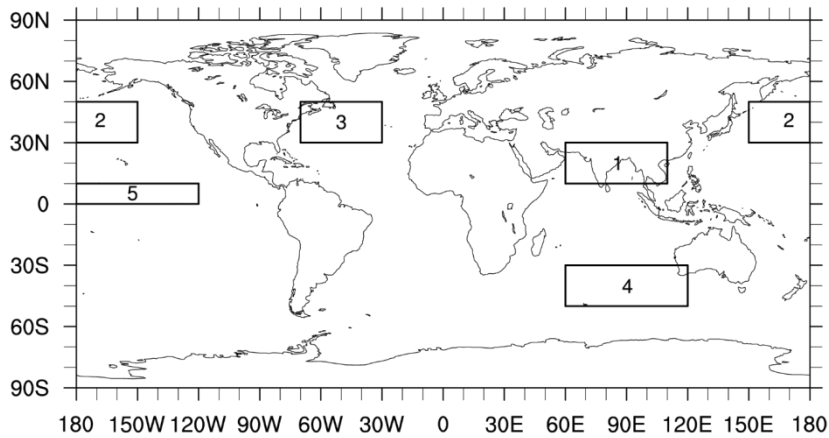
Low latitudes



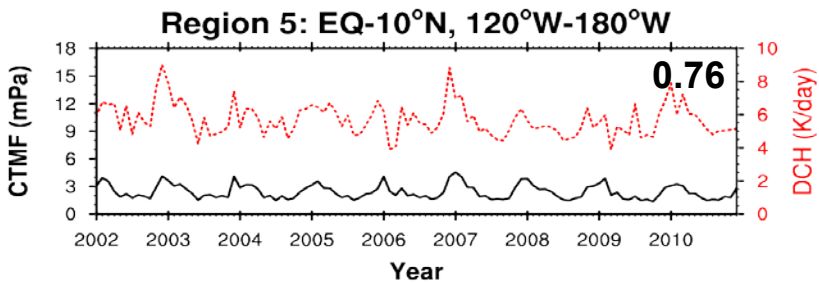
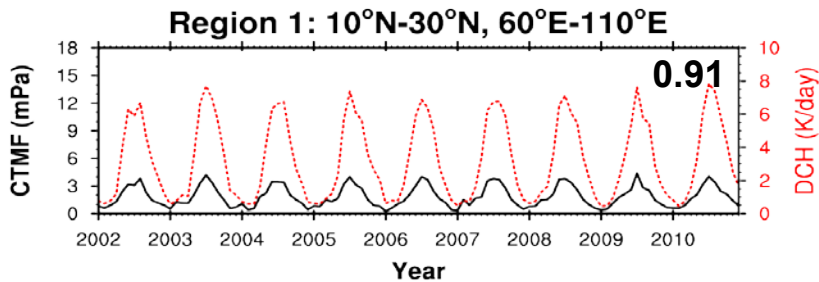
Storm-track region (midlatitudes)

Spatiotemporal variations

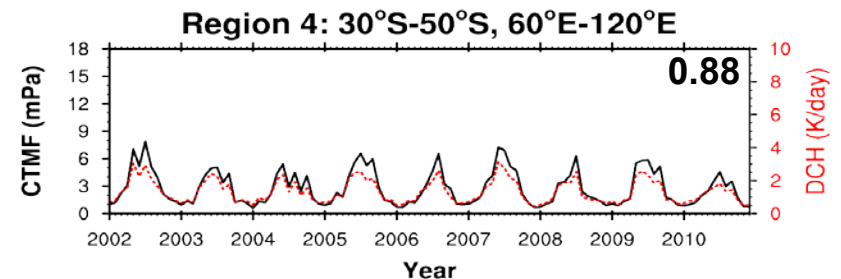
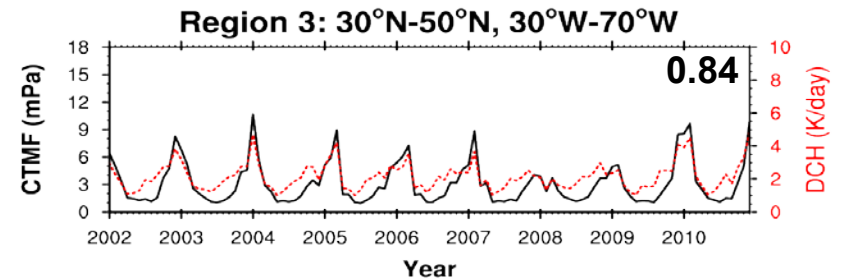
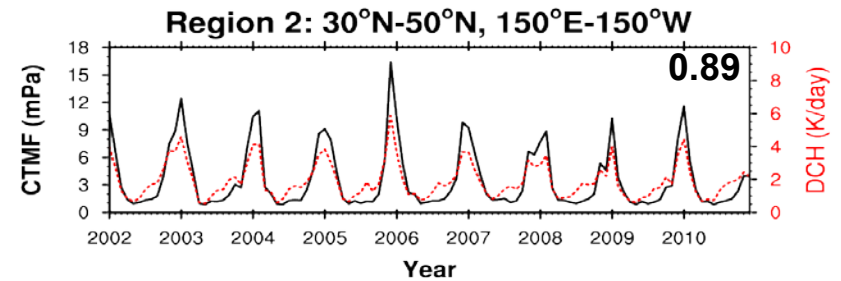
Time series



- **CTMF** is well correlated with **DCH** except in the tropical region (region 5). **effect of WFRF**
- Compared to **DCH**, the magnitude of **CTMF** is relatively reduced in **low latitudes** than mid to high latitudes.

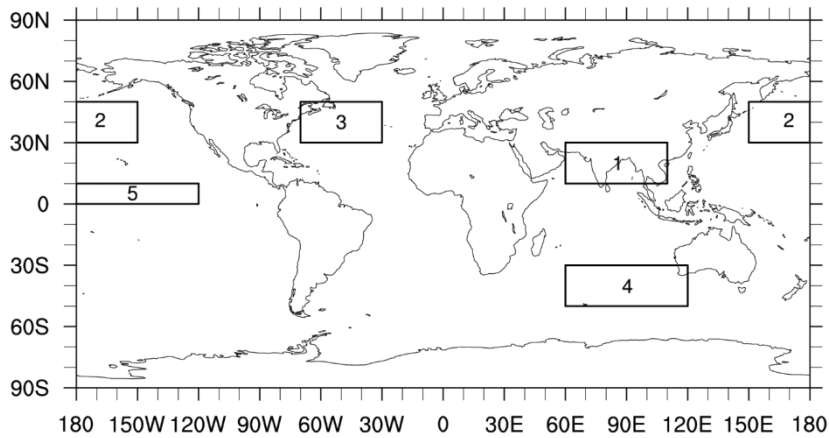


Low latitudes



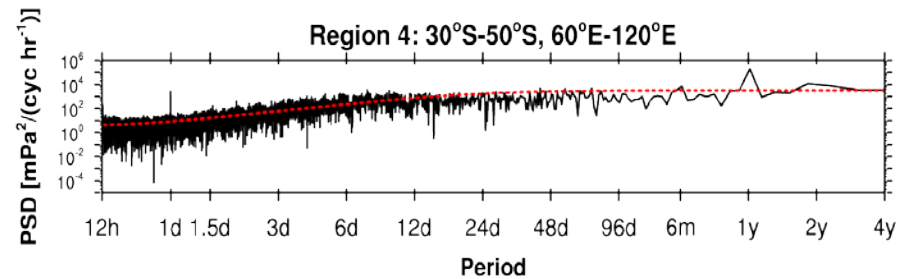
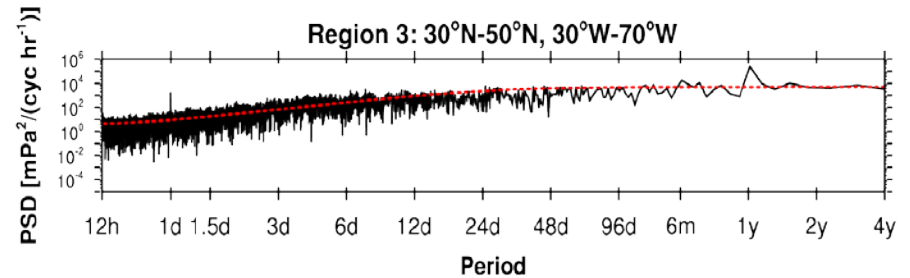
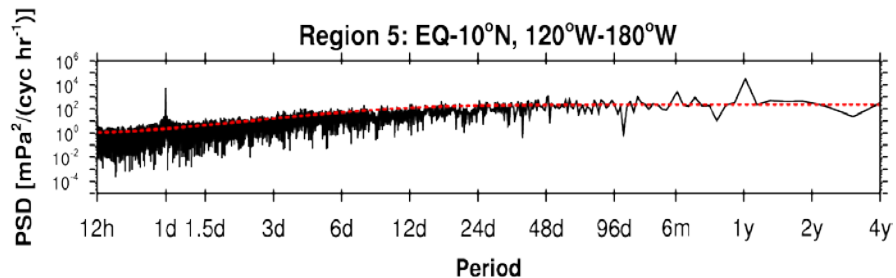
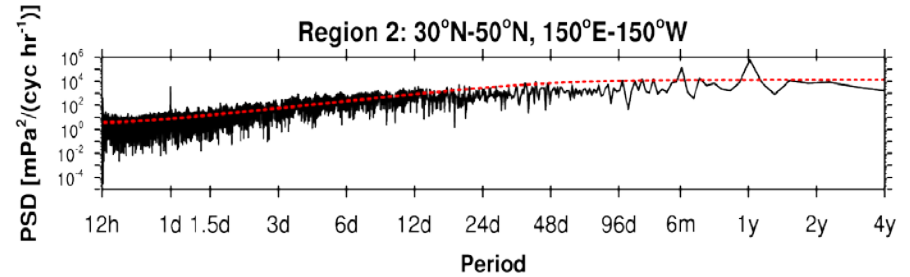
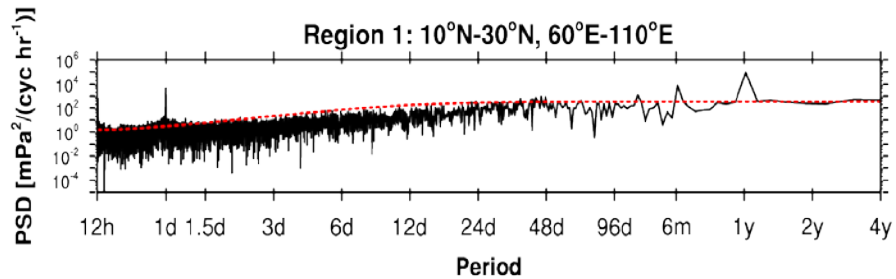
Storm-track region (midlatitudes)

Spatiotemporal variations Power Spectral Density



Black solid line: Power spectral density
 Red dotted line: red noise line at the 95% confidence level

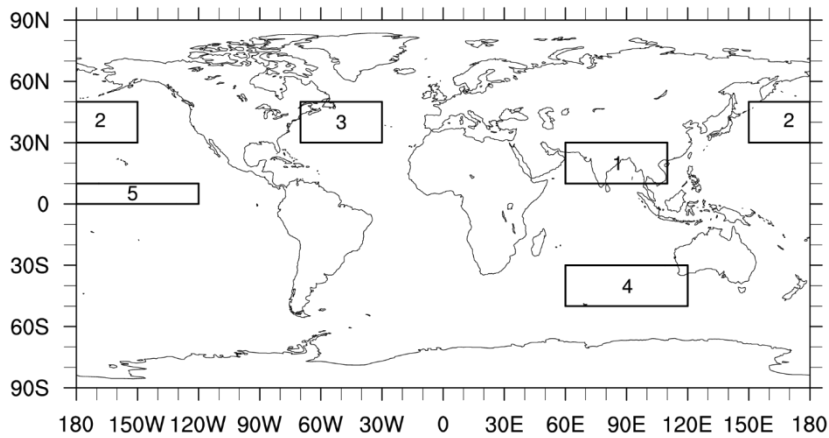
- 1 day, 6 month, 1 year cycle is strongly related to the temporal variation of convection.
- **Interannual variabilities** are also significant.



Low latitudes

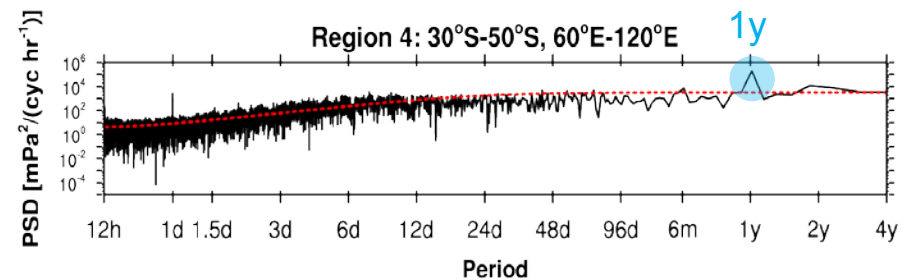
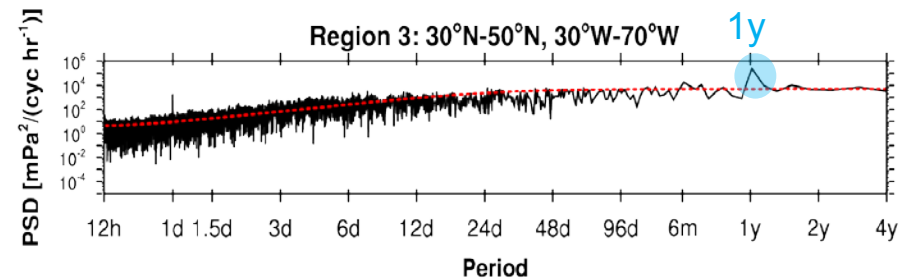
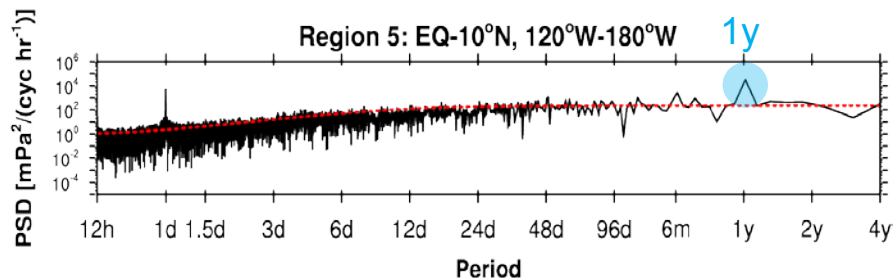
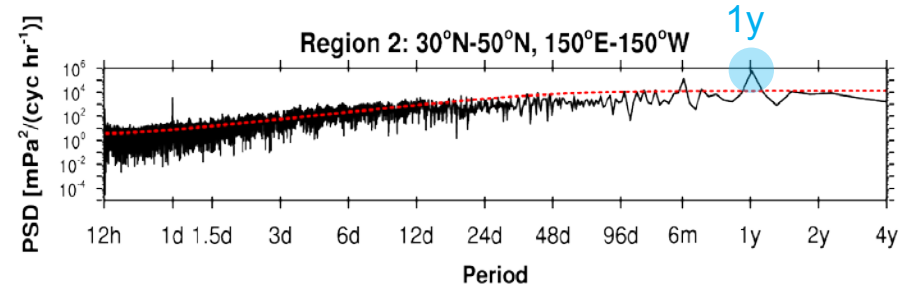
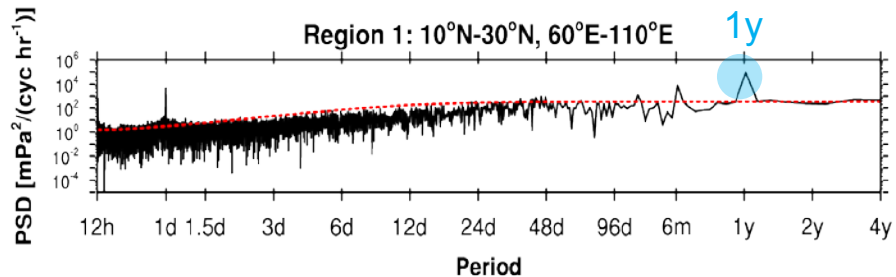
Storm-track region (midlatitudes)

Spatiotemporal variations Power Spectral Density



Black solid line: Power spectral density
 Red dotted line: red noise line at the 95% confidence level

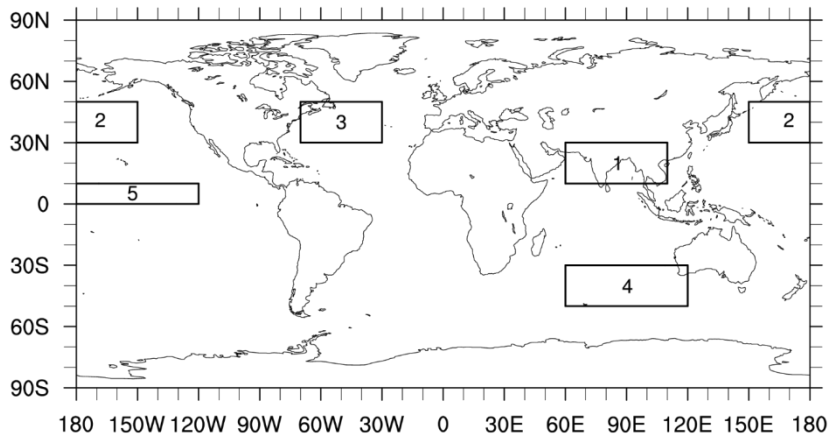
- 1 day, 6 month, 1 year cycle is strongly related to the temporal variation of convection.
- **Interannual variabilities** are also significant.



Low latitudes

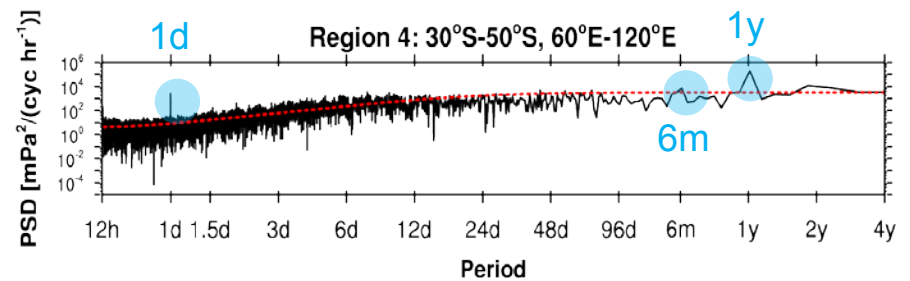
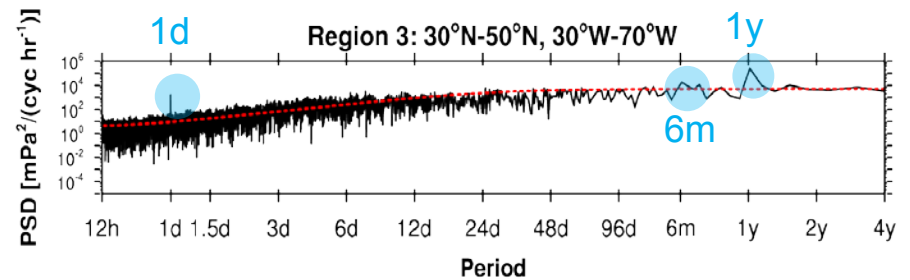
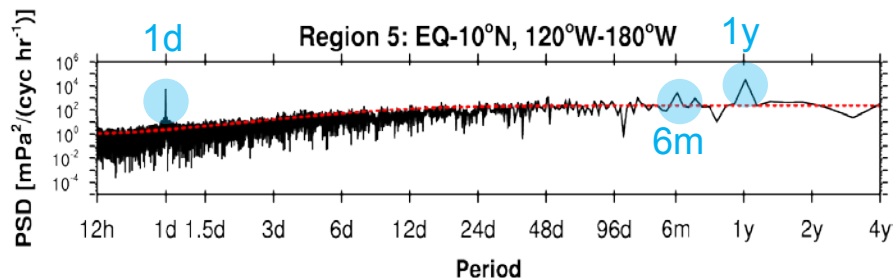
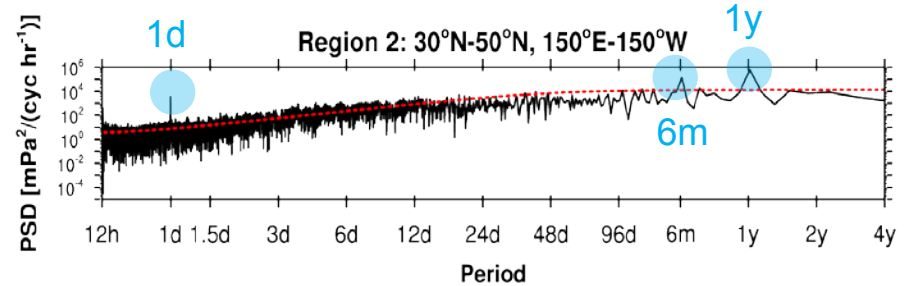
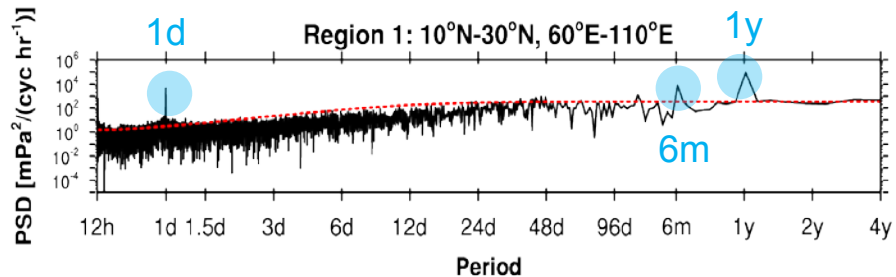
Storm-track region (midlatitudes)

Spatiotemporal variations Power Spectral Density



Black solid line: Power spectral density
 Red dotted line: red noise line at the 95% confidence level

- 1 day, 6 month, 1 year cycle is strongly related to the temporal variation of convection.
- **Interannual variabilities** are also significant.

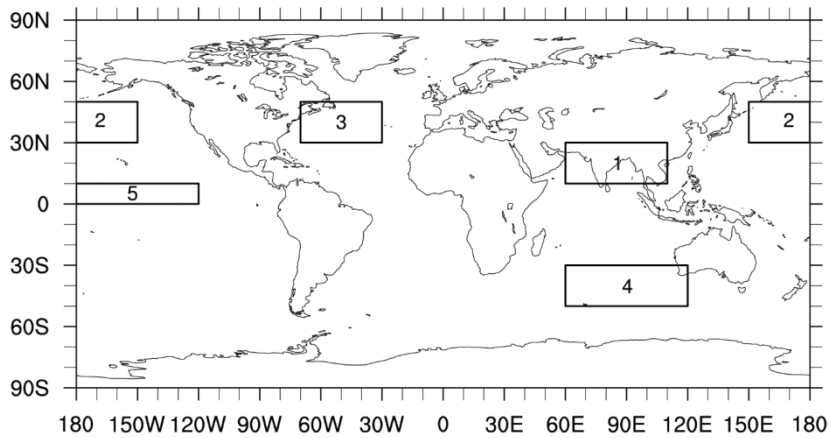


Low latitudes

Storm-track region (midlatitudes)

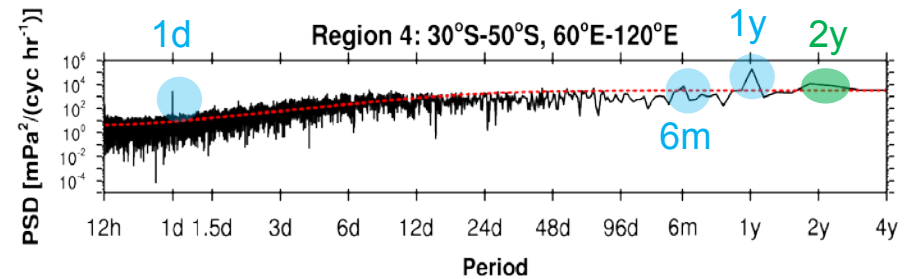
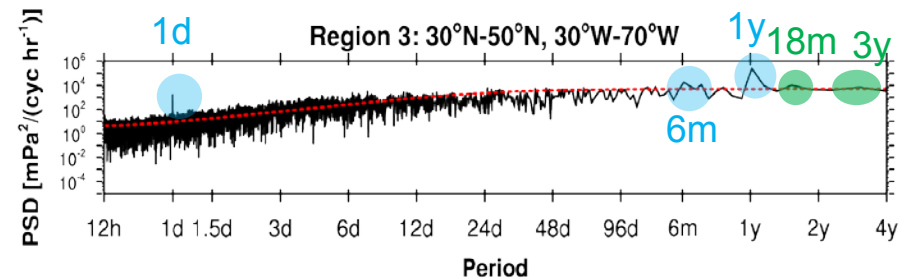
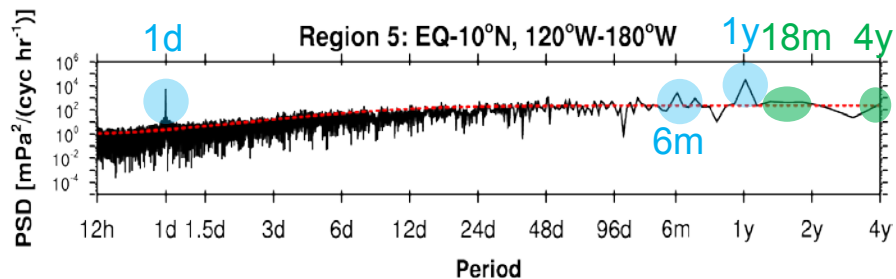
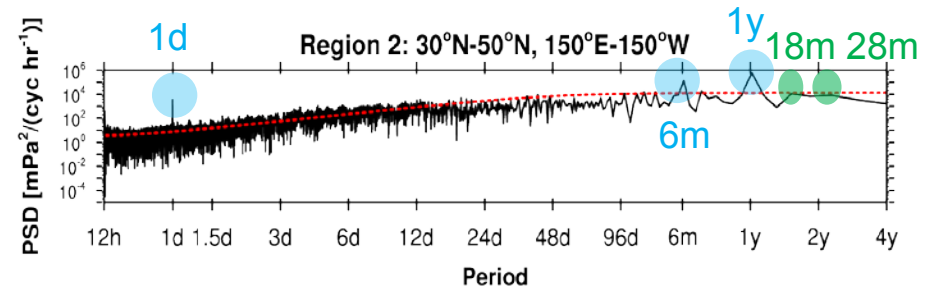
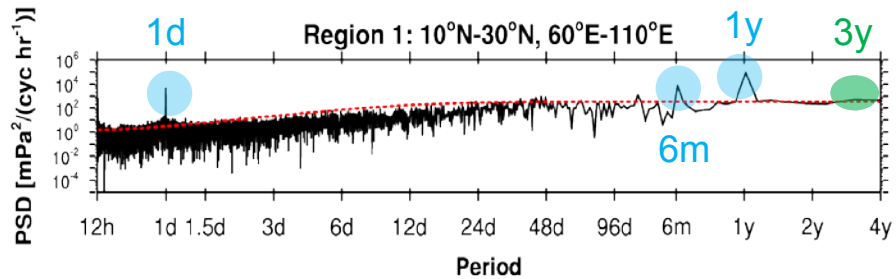
Spatiotemporal variations

Power Spectral Density



Black solid line: Power spectral density
 Red dotted line: red noise line at the 95% confidence level

- 1 day, 6 month, 1 year cycle is strongly related to the temporal variation of convection.
- **Interannual variabilities** are also significant.

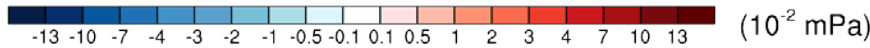
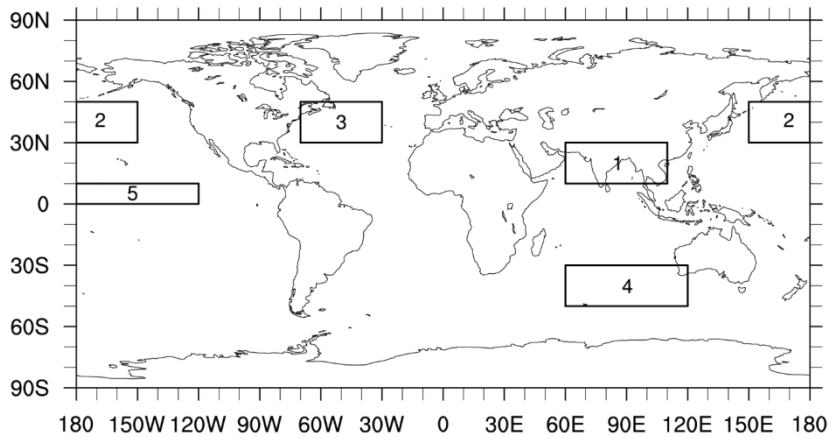


Low latitudes

Storm-track region (midlatitudes)

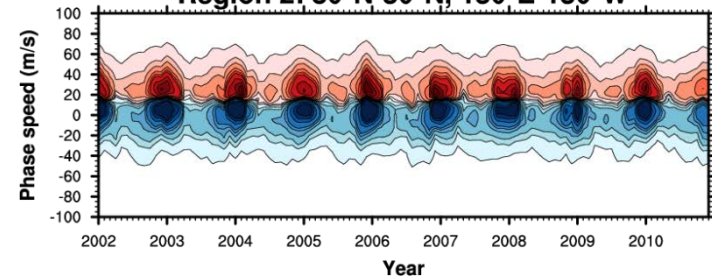
Spatiotemporal variations

Zonal CTMF spectrum

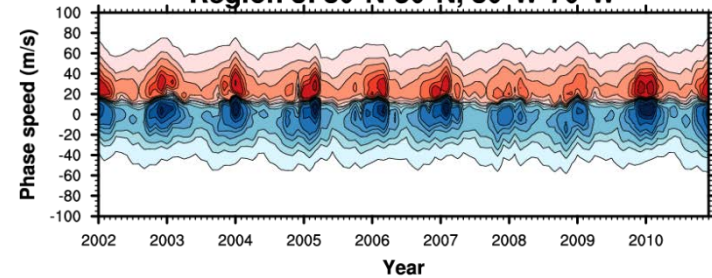


- **Annual variation** is large except in region 5.
- The **width** of the CTMF spectrum is large in the **low latitudes** (region 1 & region 5).

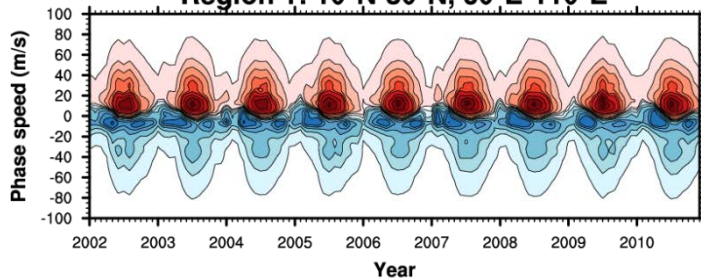
Region 2: 30°N-50°N, 150°E-150°W



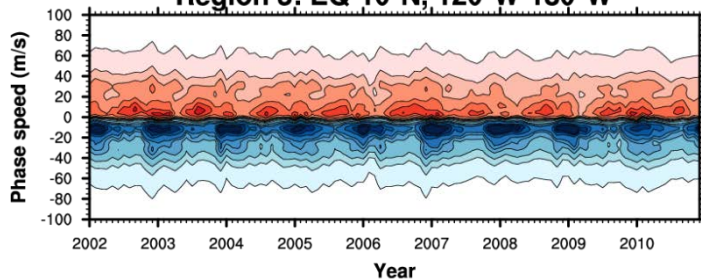
Region 3: 30°N-50°N, 30°W-70°W



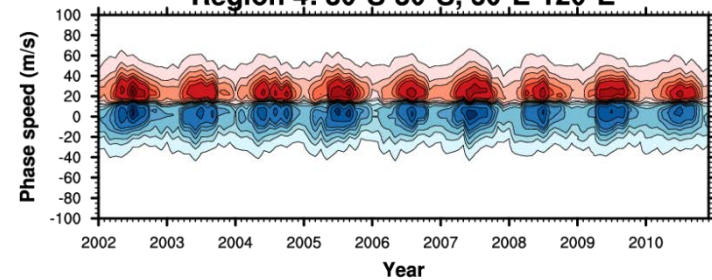
Region 1: 10°N-30°N, 60°E-110°E



Region 5: EQ-10°N, 120°W-180°W



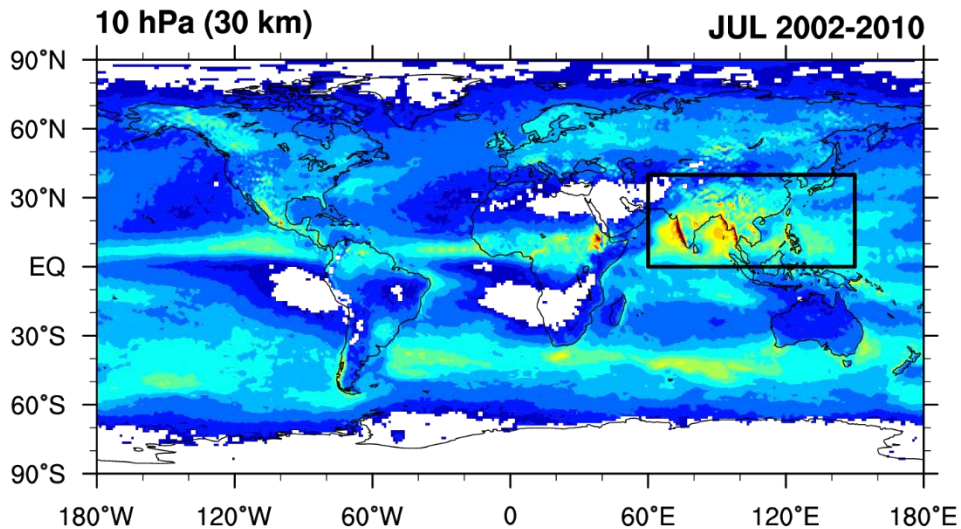
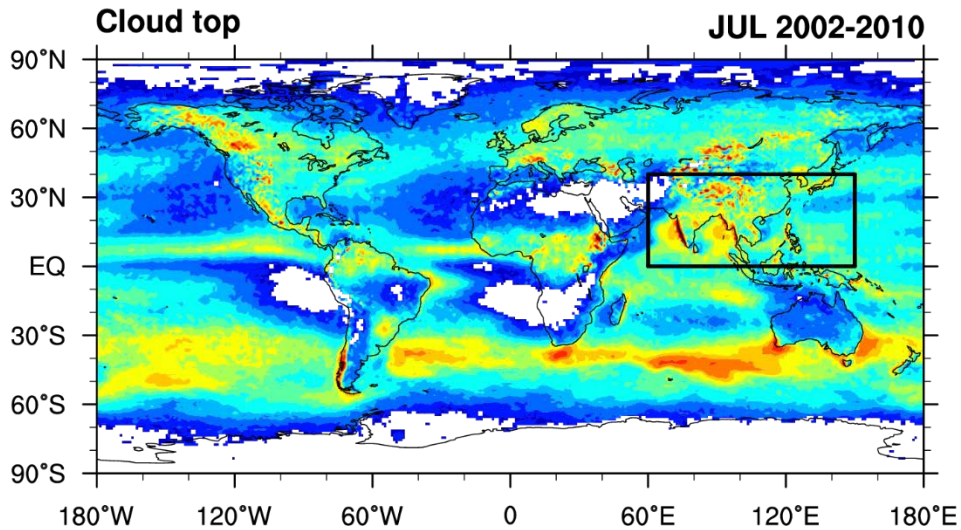
Region 4: 30°S-50°S, 60°E-120°E



Low latitudes

Storm-track region (midlatitudes)

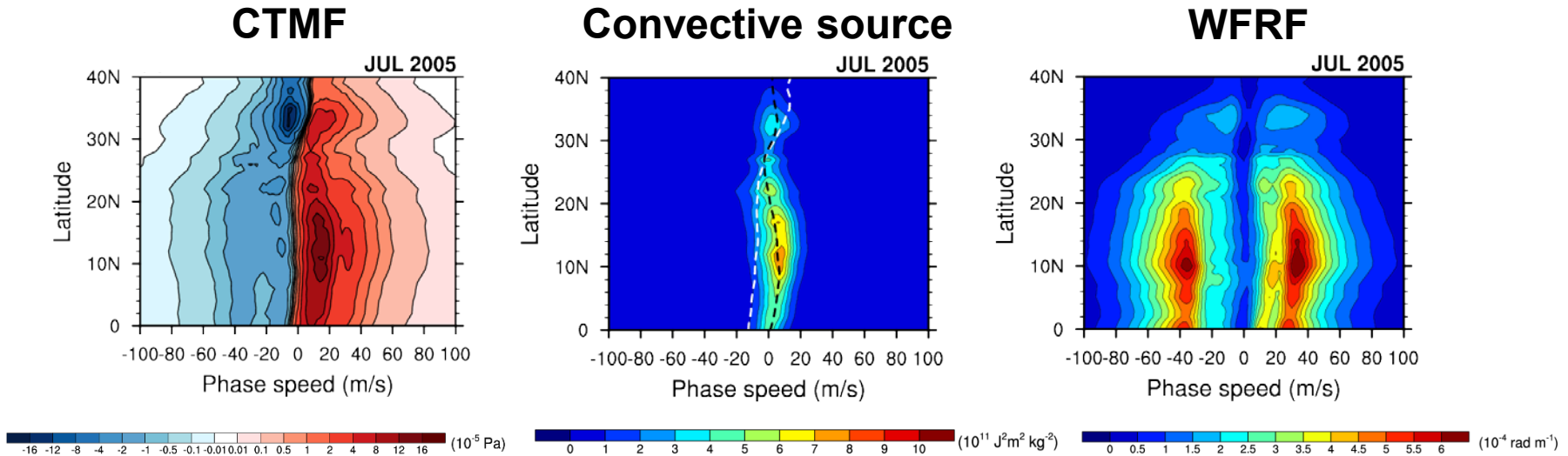
CGW momentum flux Asian summer monsoon region



Large convective gravity wave momentum flux at the cloud top and the stratosphere (10 hPa)

CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$



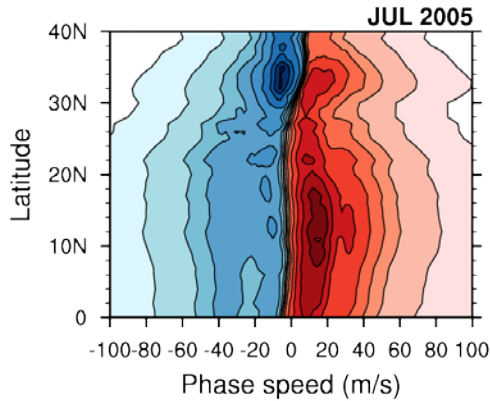
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian summer monsoon region

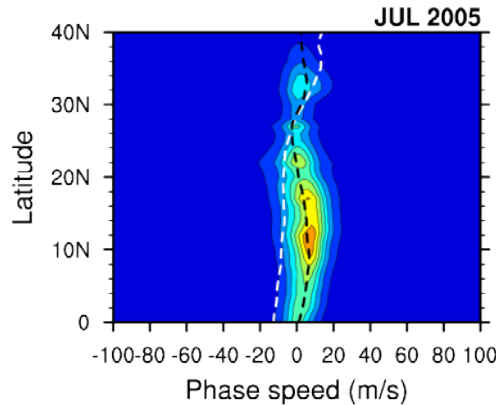
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WFRF
Convective source

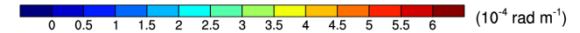
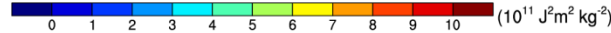
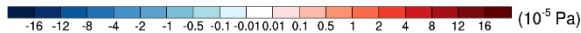
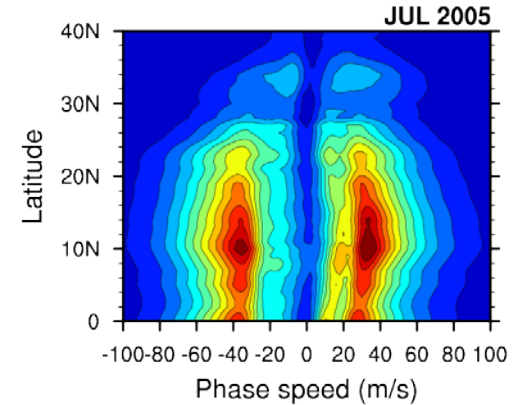
CTMF



Convective source



WFRF



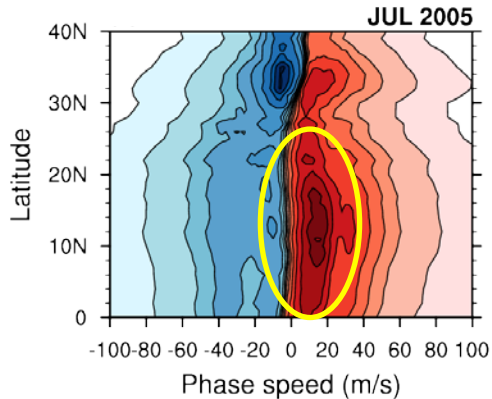
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian summer monsoon region

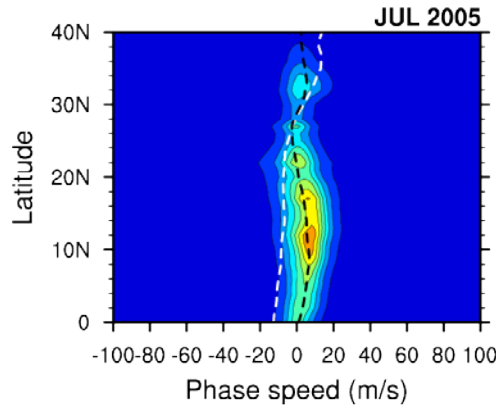
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WFRF
Convective source

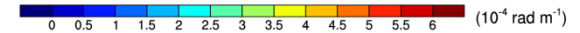
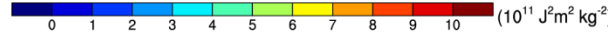
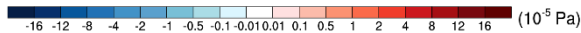
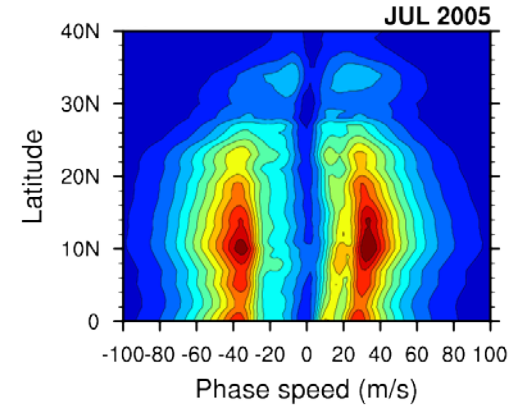
CTMF



Convective source



WFRF

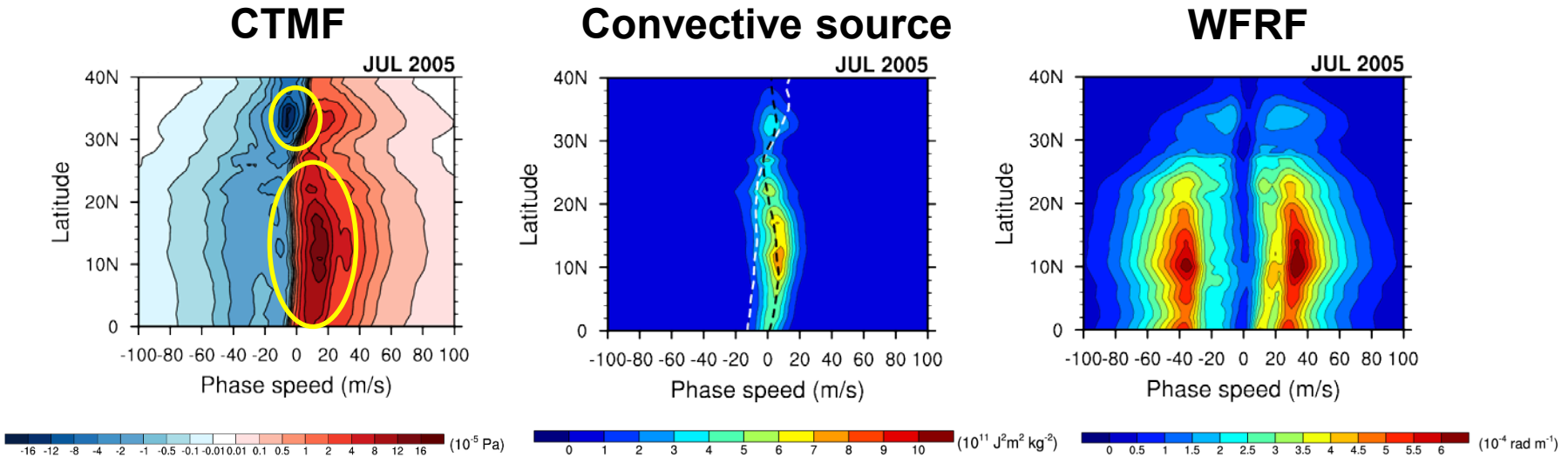


- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WFRF
Convective source

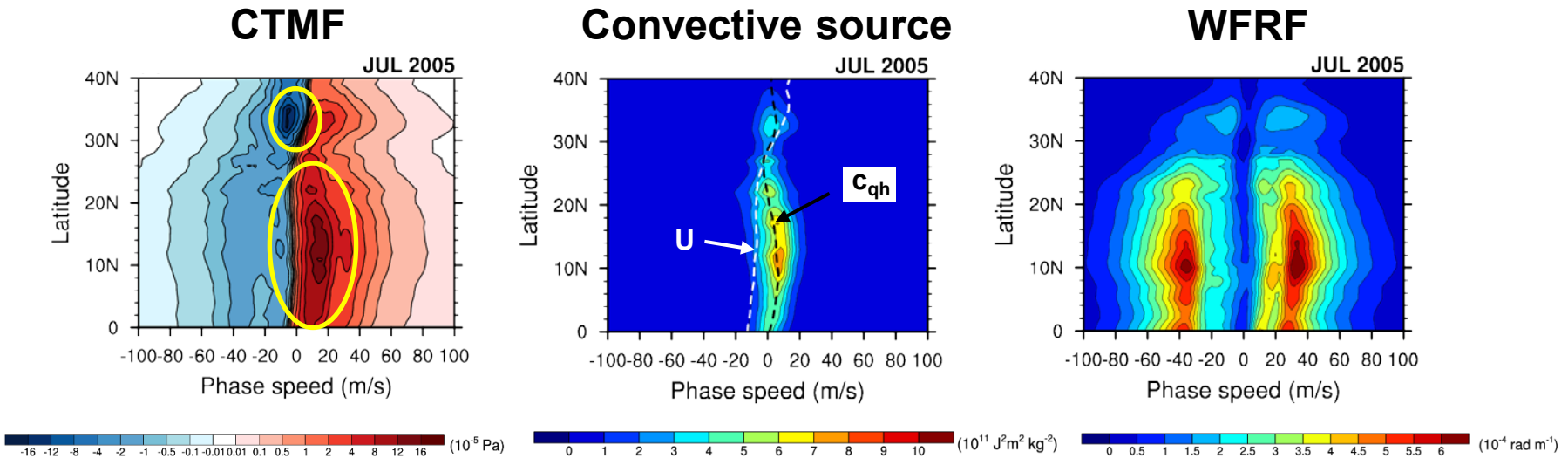


- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WFRF
Convective source



- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

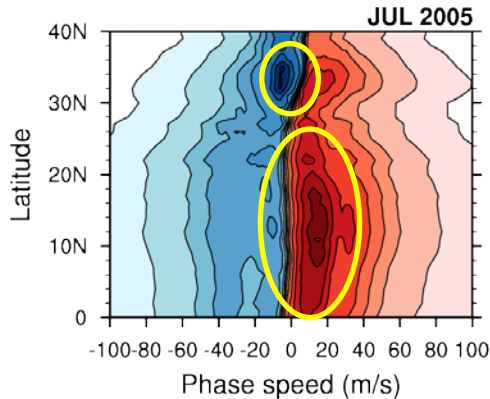
CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

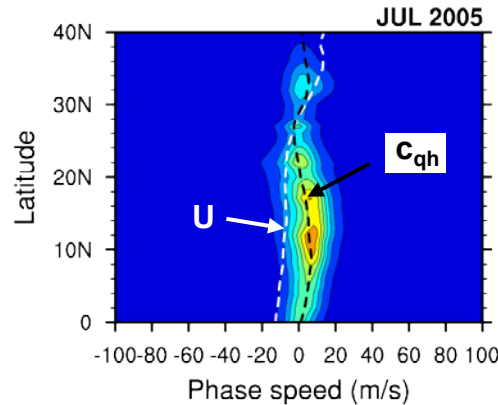
CTMF
WFRF
Convective source
Convective source
Moving speed of convection

$$\Theta(c, \varphi) = q_0^2 \left(\frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{1 + [c - c_{qh}(\varphi)]^2 / c_0^2}$$

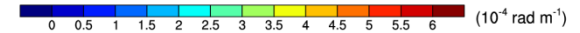
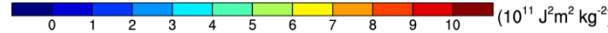
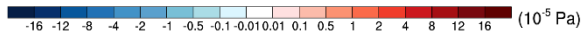
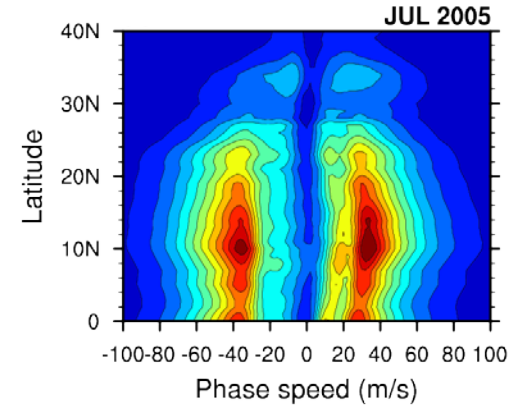
CTMF



Convective source



WFRF



- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

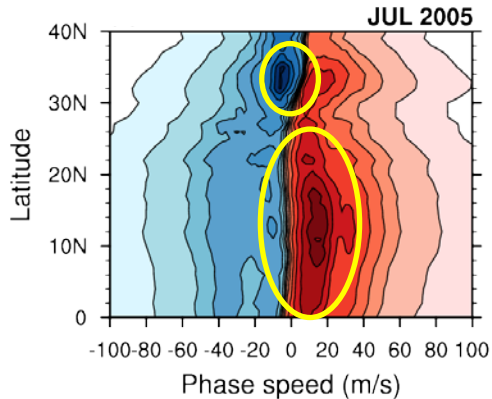
CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

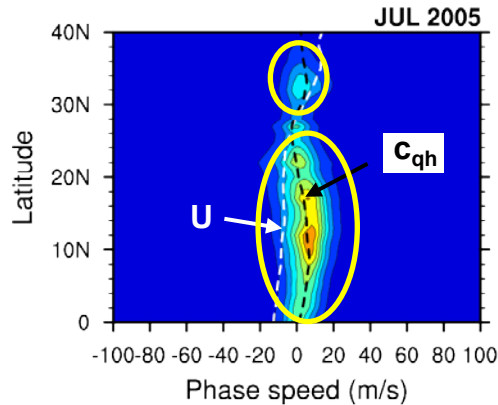
CTMF
WFRF
Convective source
Convective source
Moving speed of convection

$$\Theta(c, \varphi) = q_0^2 \left(\frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{1 + [c - c_{qh}(\varphi)]^2 / c_0^2}$$

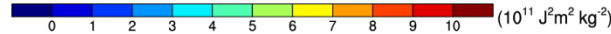
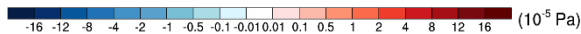
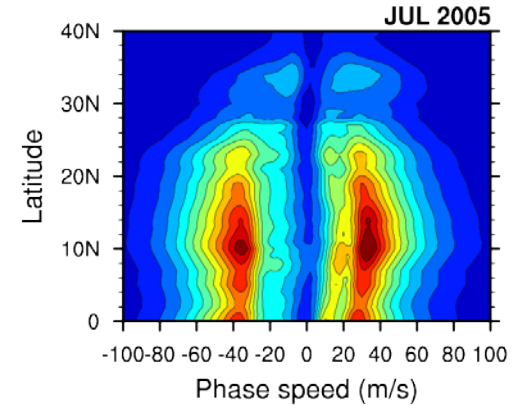
CTMF



Convective source



WFRF



- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

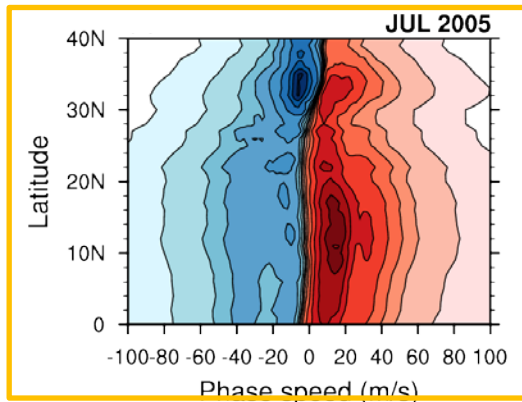
CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

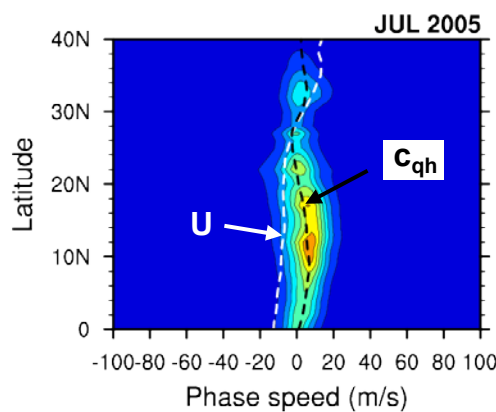
CTMF
WFRF
Convective source
Convective source
Moving speed of convection

$$\Theta(c, \varphi) = q_0^2 \left(\frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{1 + [c - c_{qh}(\varphi)]^2 / c_0^2}$$

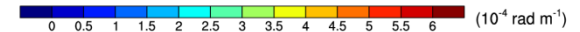
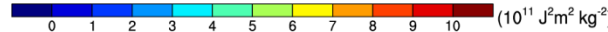
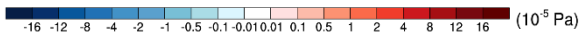
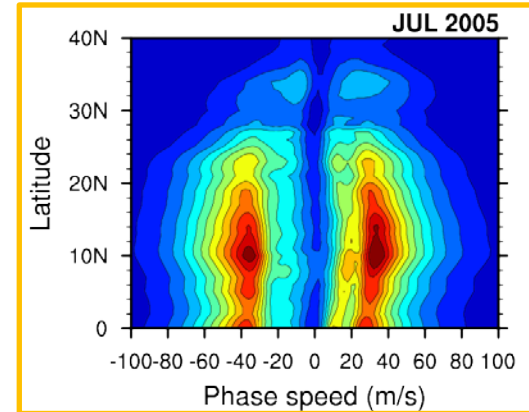
CTMF



Convective source



WFRF



- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

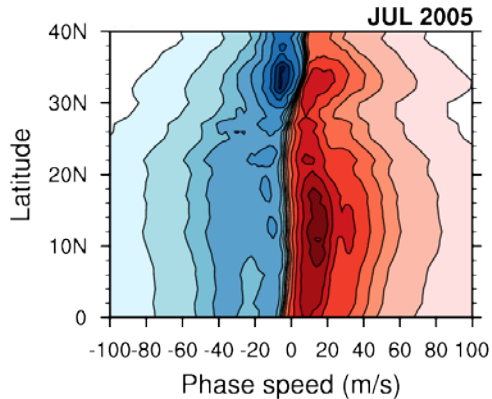
CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

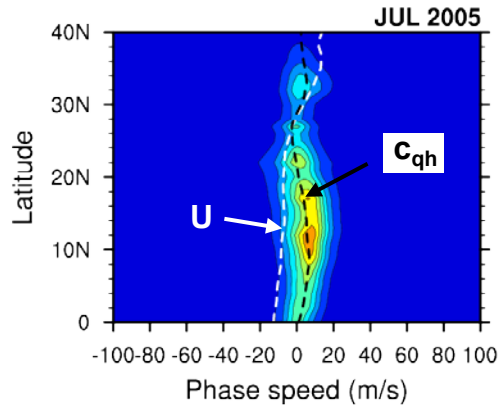
CTMF
WFRF
Convective source
Convective source
Moving speed of convection

$$\Theta(c, \varphi) = q_0^2 \left(\frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{1 + [c - c_{qh}(\varphi)]^2 / c_0^2}$$

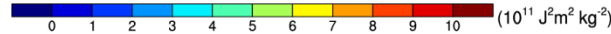
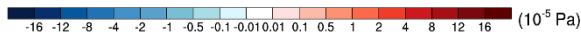
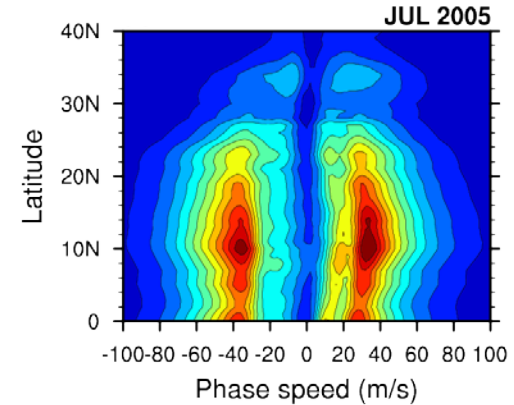
CTMF



Convective source



WFRF



- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

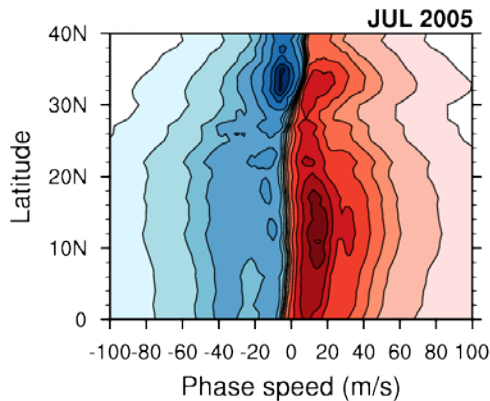
CTMF spectrum Asian summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

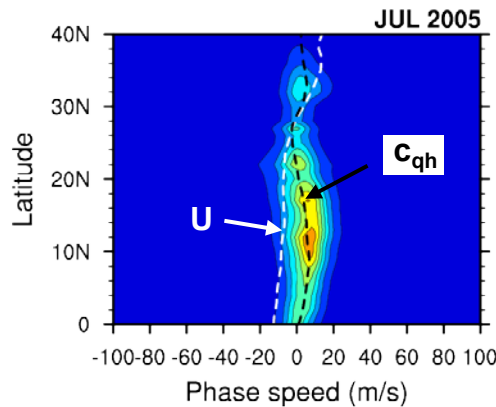
CTMF
WFRF
Convective source
Convective source
Moving speed of convection

$$\Theta(c, \varphi) = q_0^2 \left(\frac{\delta_h \delta_t}{32\pi^{3/2}} \right)^2 \frac{1}{1 + [c - c_{qh}(\varphi)]^2 / c_0^2}$$

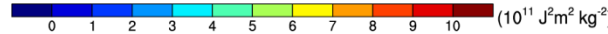
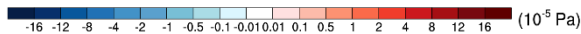
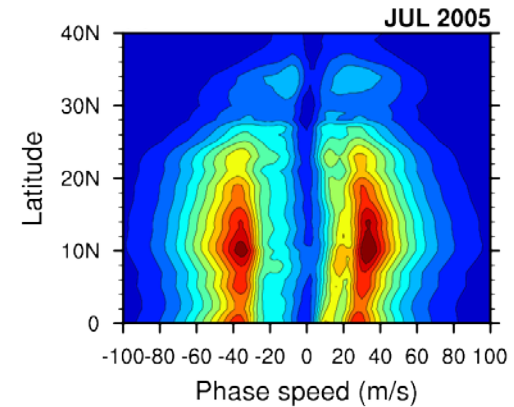
CTMF



Convective source



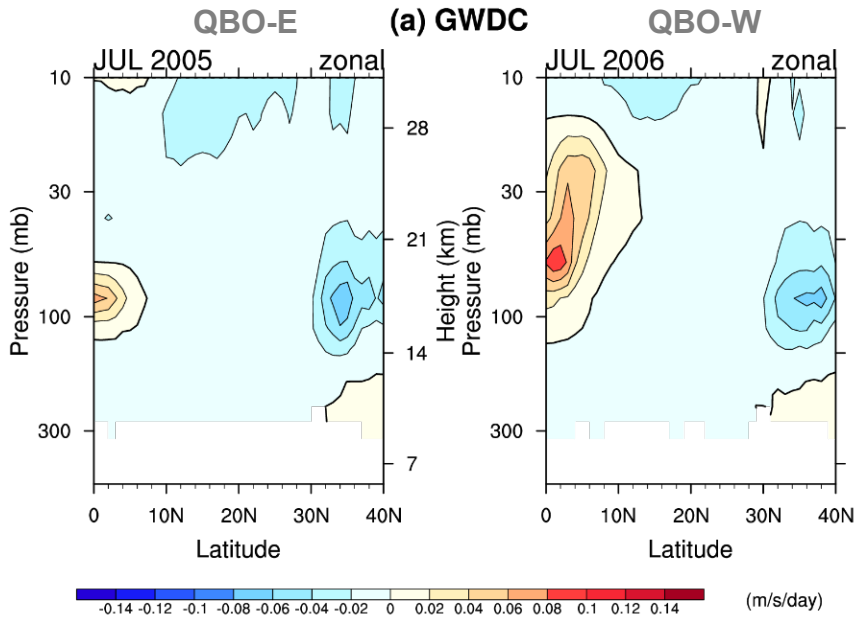
WFRF



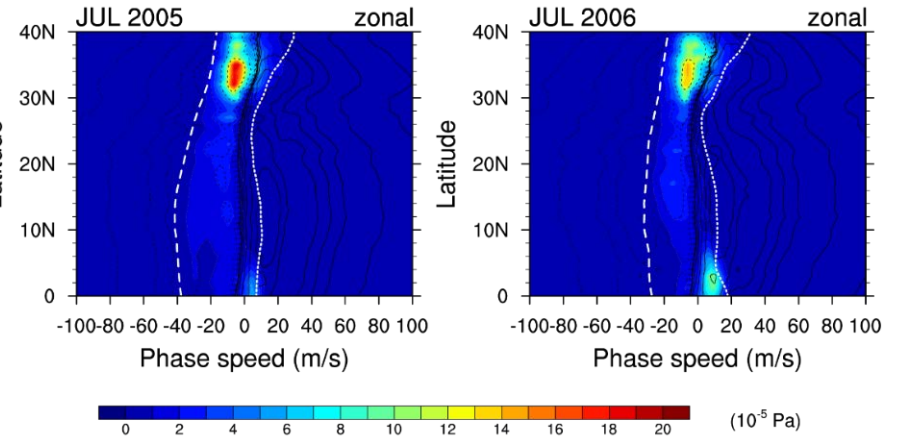
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

How this shape of the CTMF spectrum can affect GWDC?

CTMF spectrum → GWDC Asian summer monsoon region

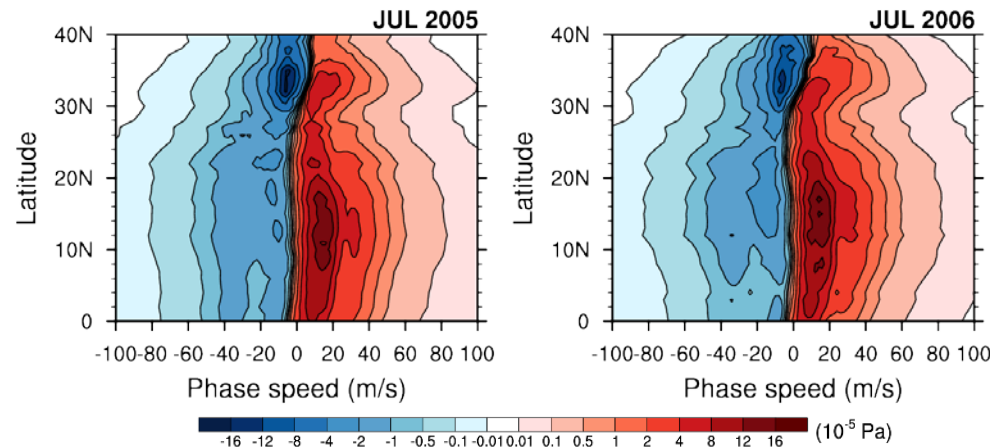


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

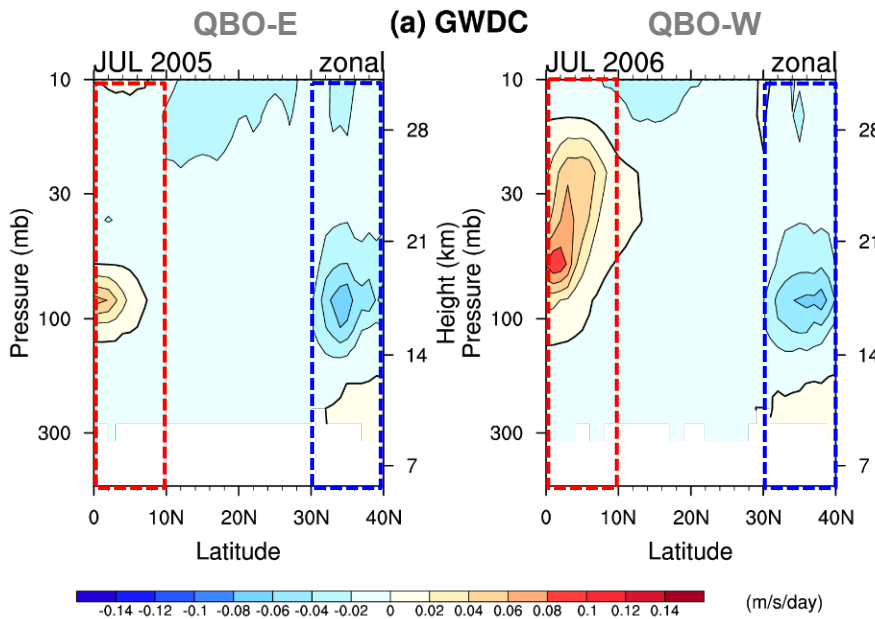


Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

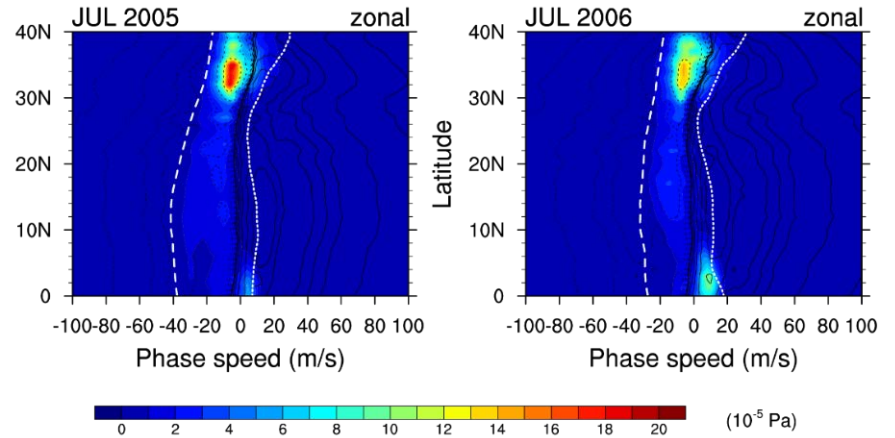
CTMF spectrum



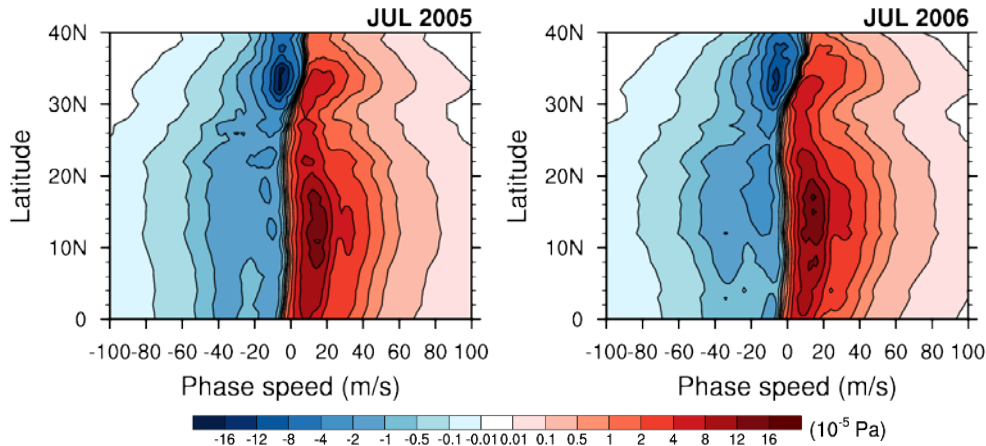
CTMF spectrum → GWDC Asian summer monsoon region



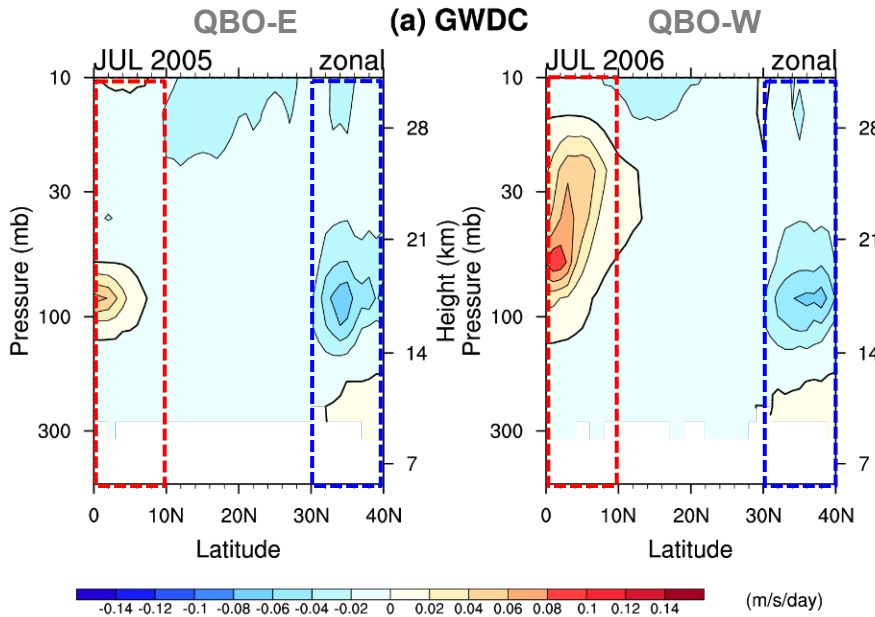
Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



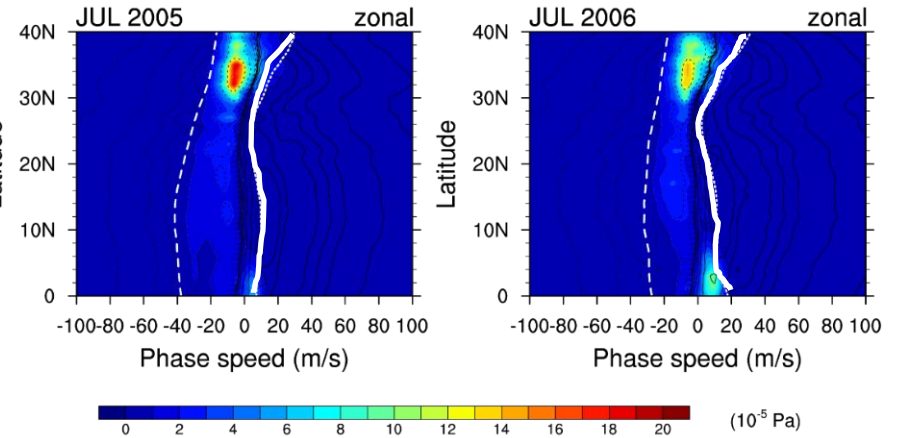
CTMF spectrum



CTMF spectrum → GWDC Asian summer monsoon region

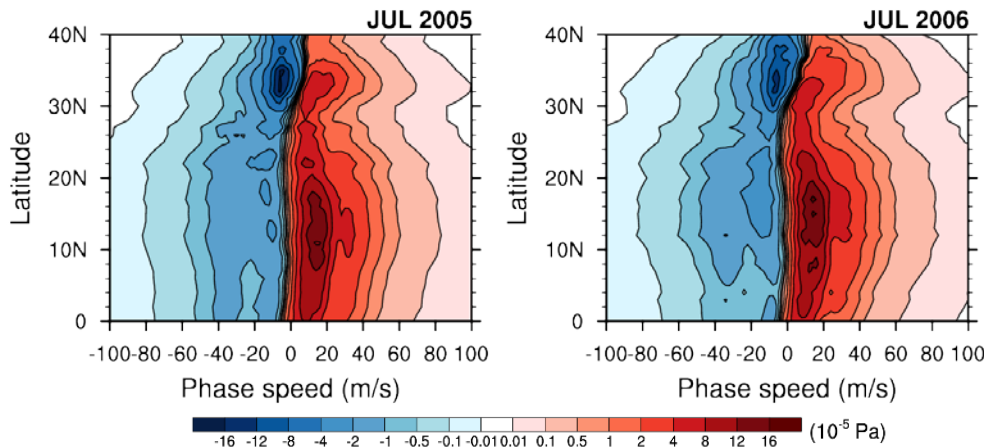


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

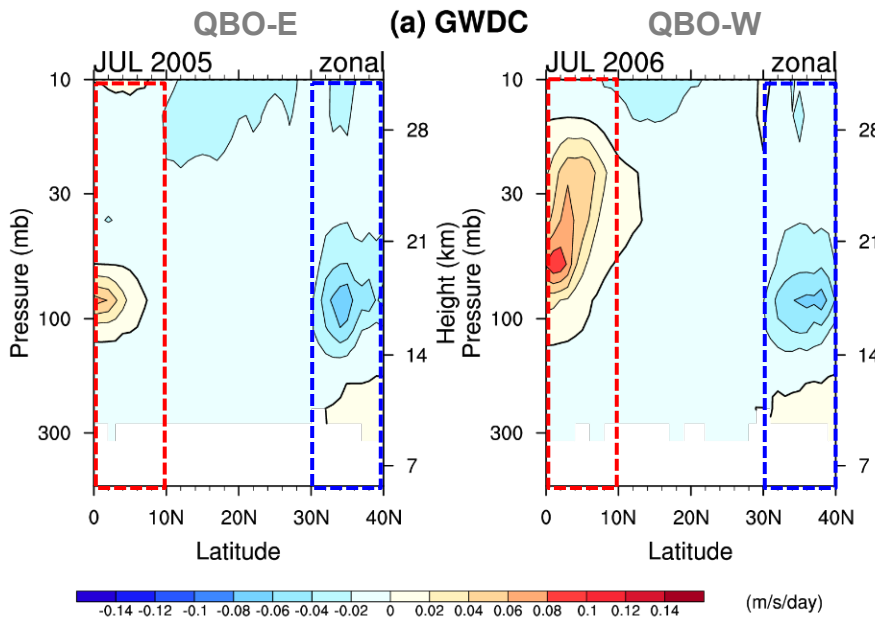


Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

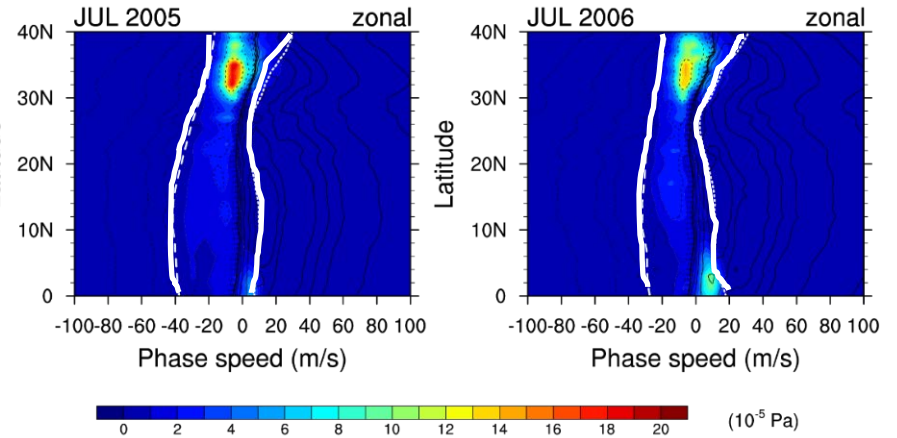
CTMF spectrum



CTMF spectrum → GWDC Asian summer monsoon region

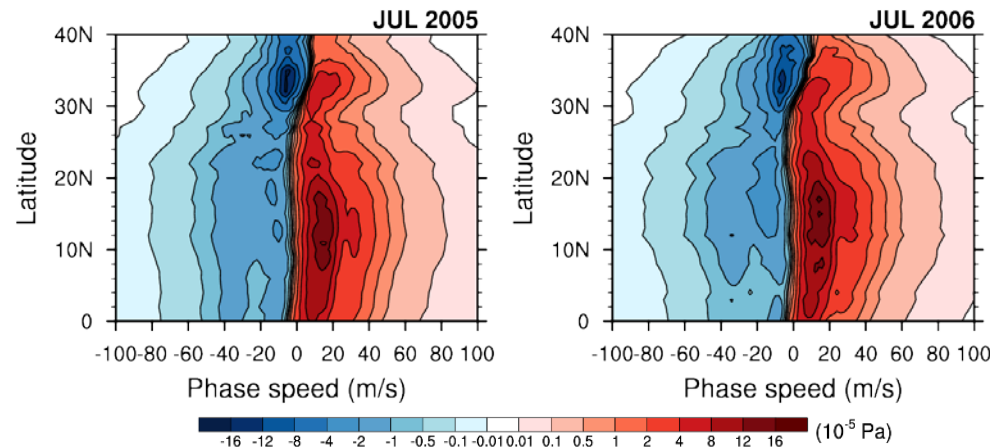


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

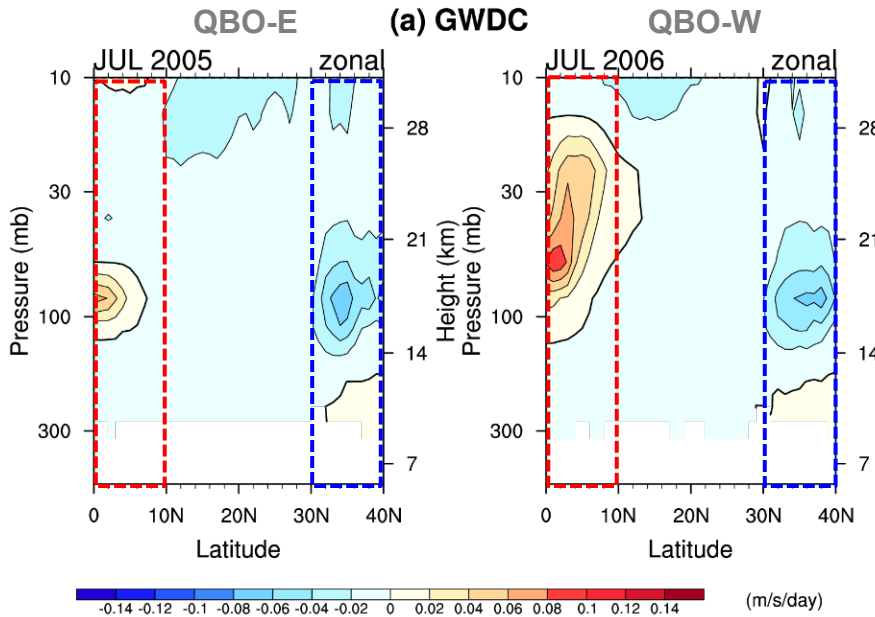


Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

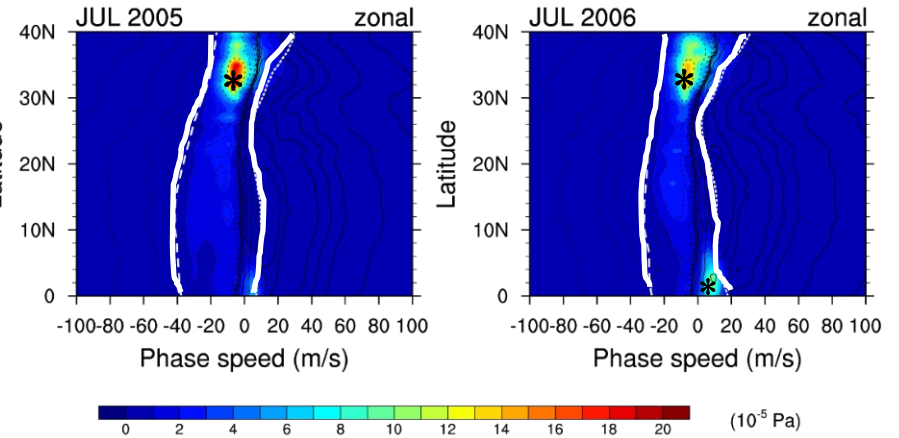
CTMF spectrum



CTMF spectrum → GWDC Asian summer monsoon region

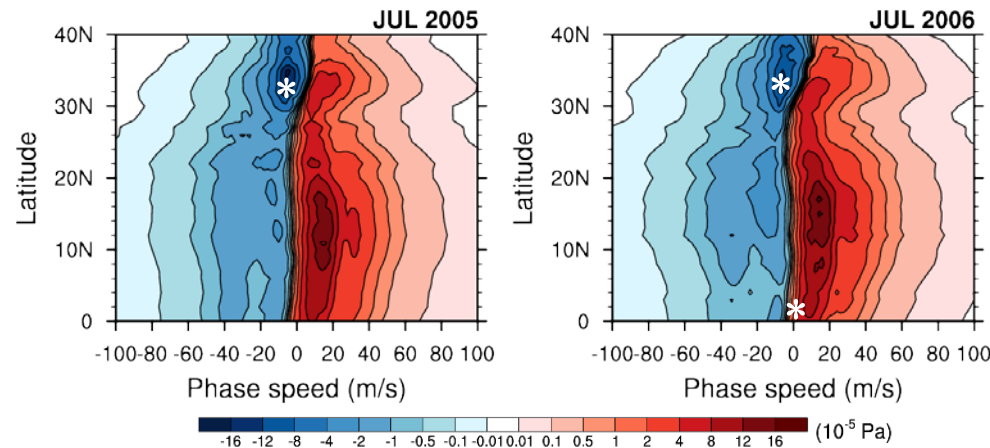


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

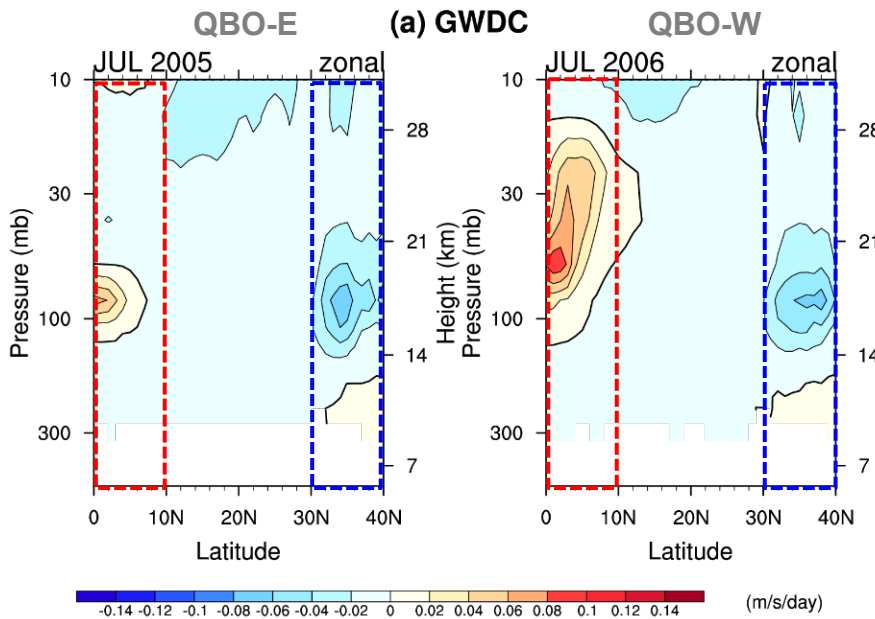


Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

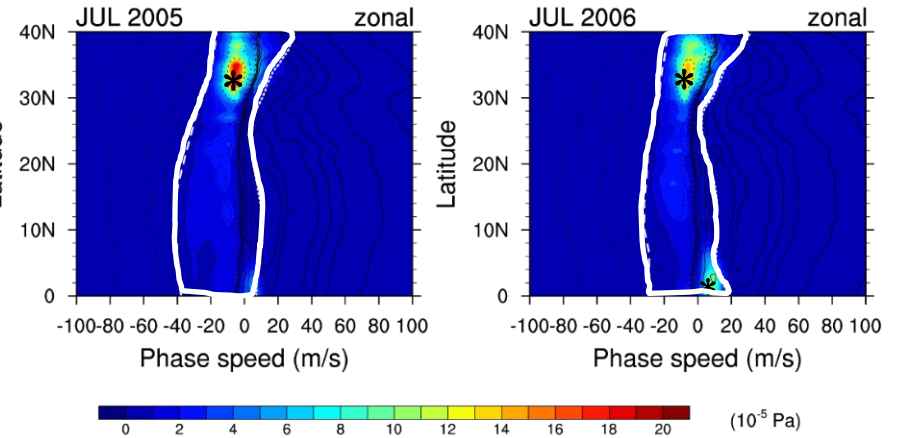
CTMF spectrum



CTMF spectrum → GWDC Asian summer monsoon region

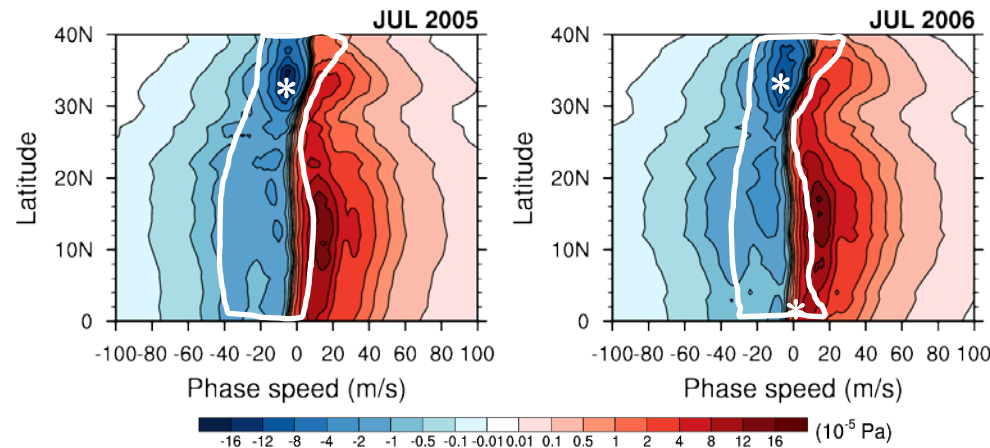


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

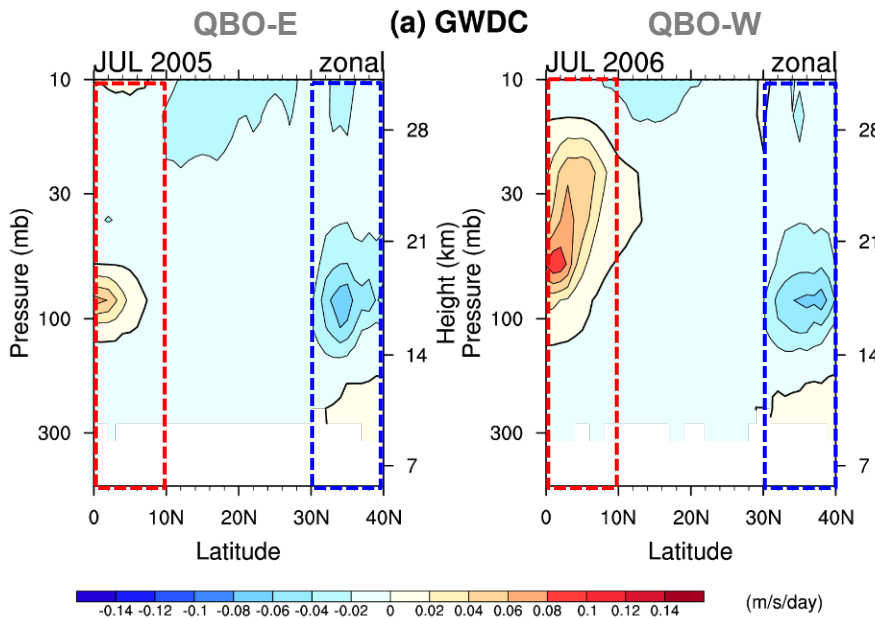


Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

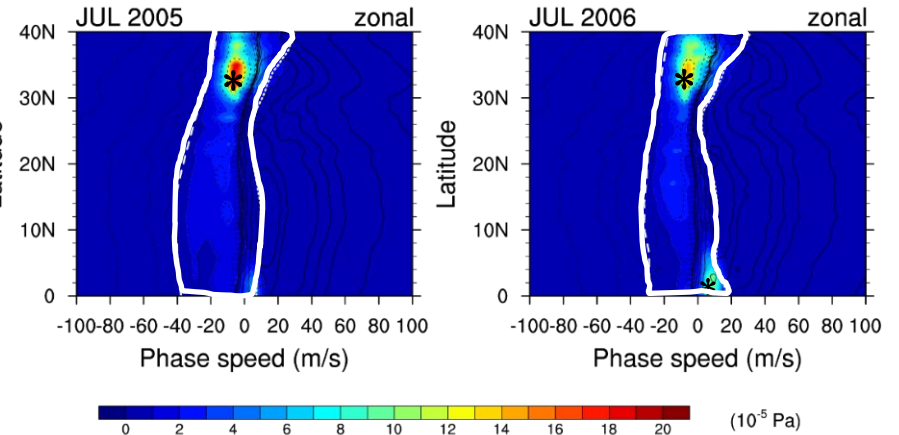
CTMF spectrum



CTMF spectrum → GWDC Asian summer monsoon region

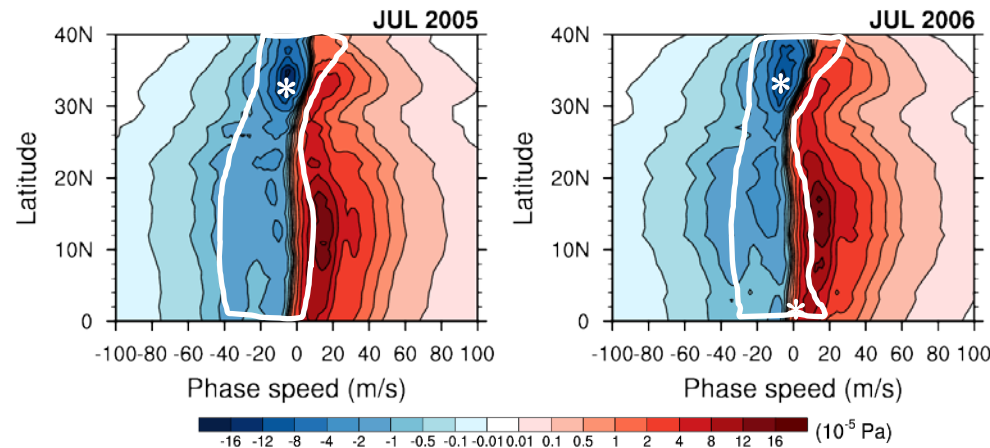


Difference in GWMF spectrum between cloud top and 10 hPa (=MF_{ct} - MF_{10 hPa})



Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

CTMF spectrum

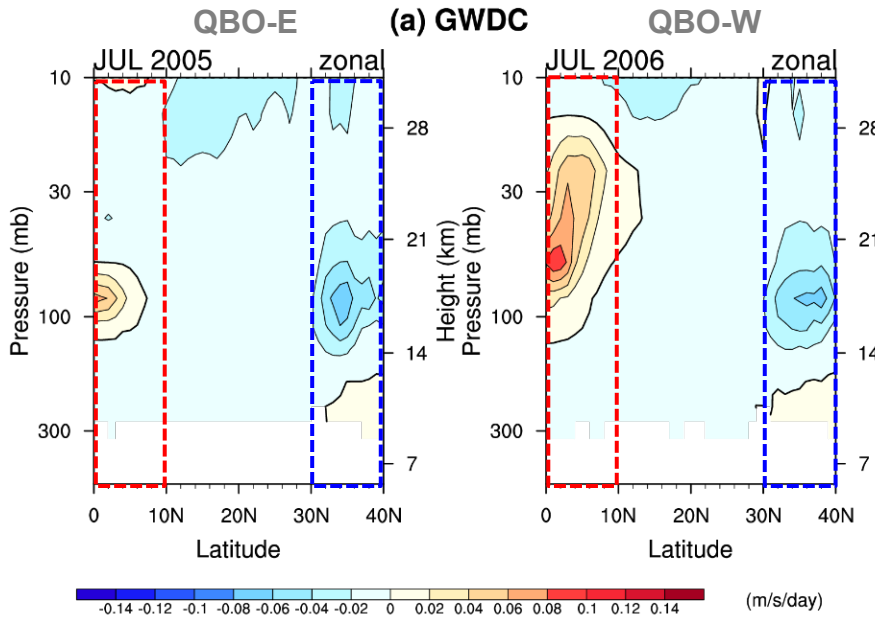


If peak of the CTMF is located within the wind filtering region

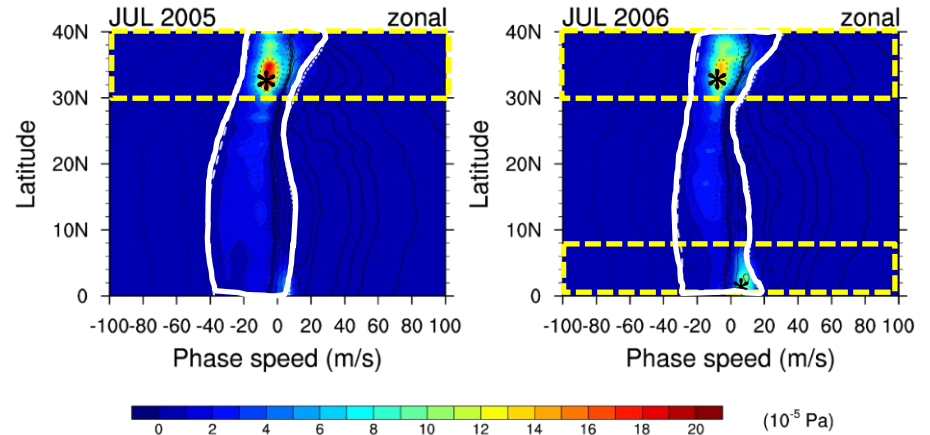
Large dissipation

Large GWDC

CTMF spectrum → GWDC Asian summer monsoon region

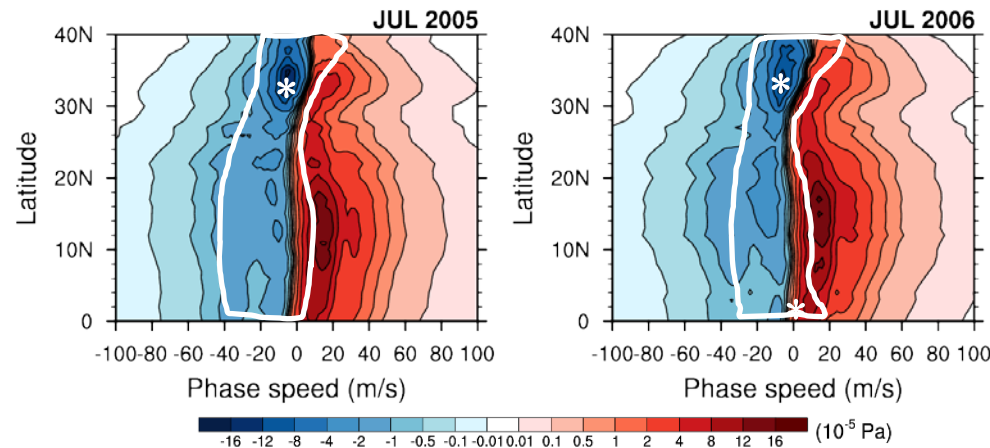


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

CTMF spectrum

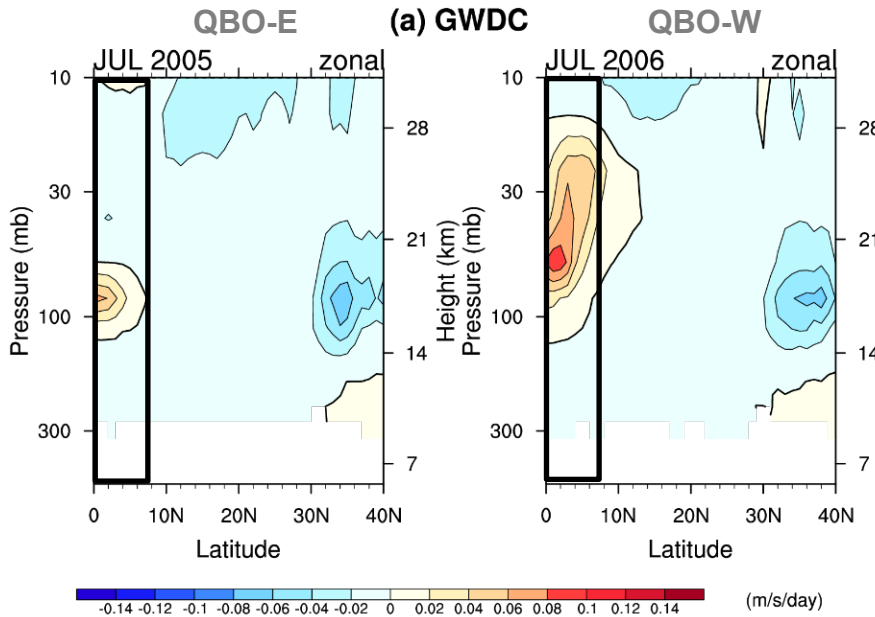


If peak of the CTMF is located within the wind filtering region

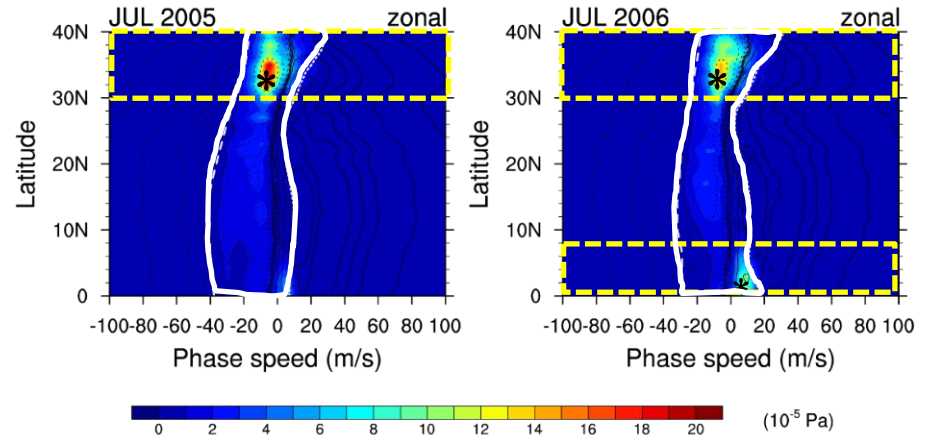
Large dissipation

Large GWDC

CTMF spectrum \rightarrow GWDC Asian summer monsoon region

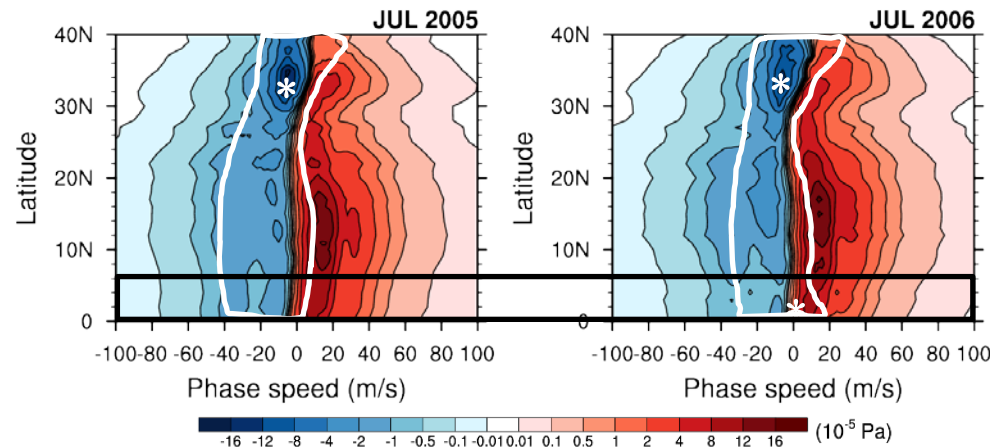


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



Dotted line: maximum zonal wind
Dashed line: minimum zonal wind

CTMF spectrum



If peak of the CTMF is located within the wind filtering region

Large dissipation

Large GWDC

The positive peak can cause large difference in GWDC between two QBO phases

Summary and conclusion

Spatiotemporal variations in CTMF

- CTMF is determined not only by magnitude of convective heating but also by wave-filtering and resonance factor, several conditions within convection, and wave nonlinearity.
- CTMF spectrum is highly fluctuate with both time and space in terms of its shape and magnitude.

CTMF spectrum and GWDC in Asian summer monsoon region

- The magnitude of GWDC is largely influenced by the CTMF spectrum.
 - Maximum drag in the stratosphere occurs where spectral peak of CTMF is located within the critical-level filtering region.

→ Physically and mathematically consistent source spectrum (CTMF) of CGWs is required for realistic spatiotemporal variabilities in GWDC of the stratosphere.



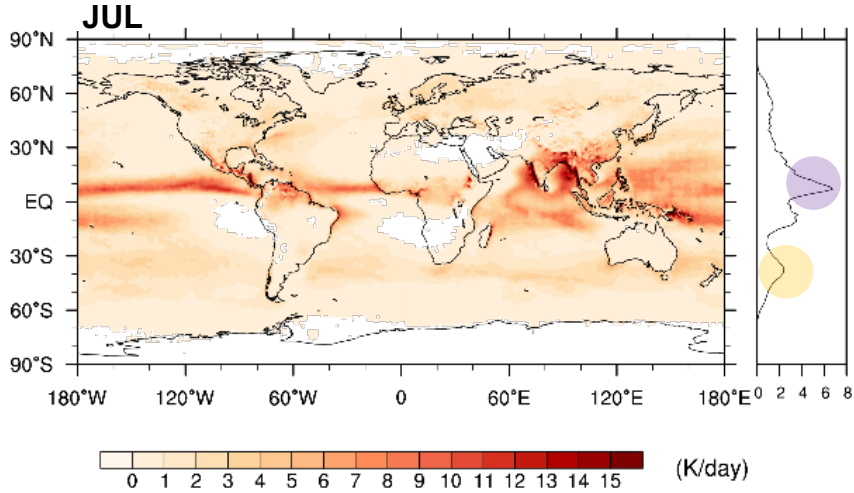
Thank you for your attention.

Spatial variability

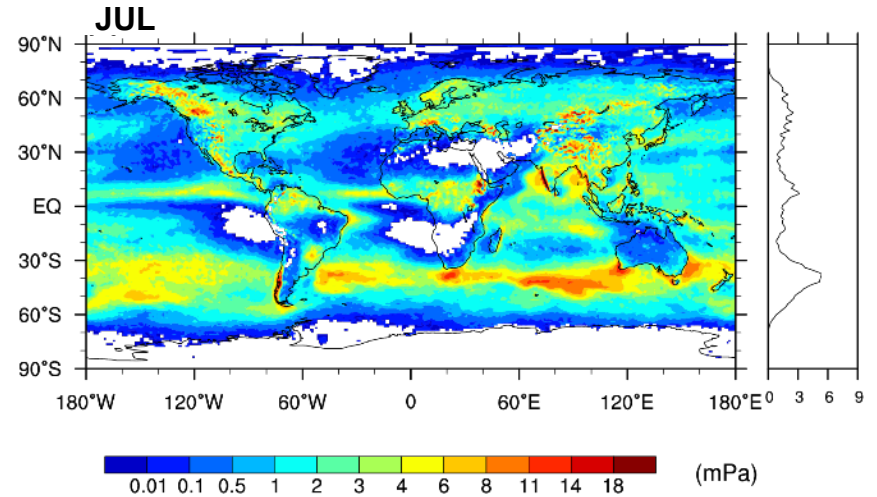
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WFRF
Convective source \propto DCH

DCH (CFRS)

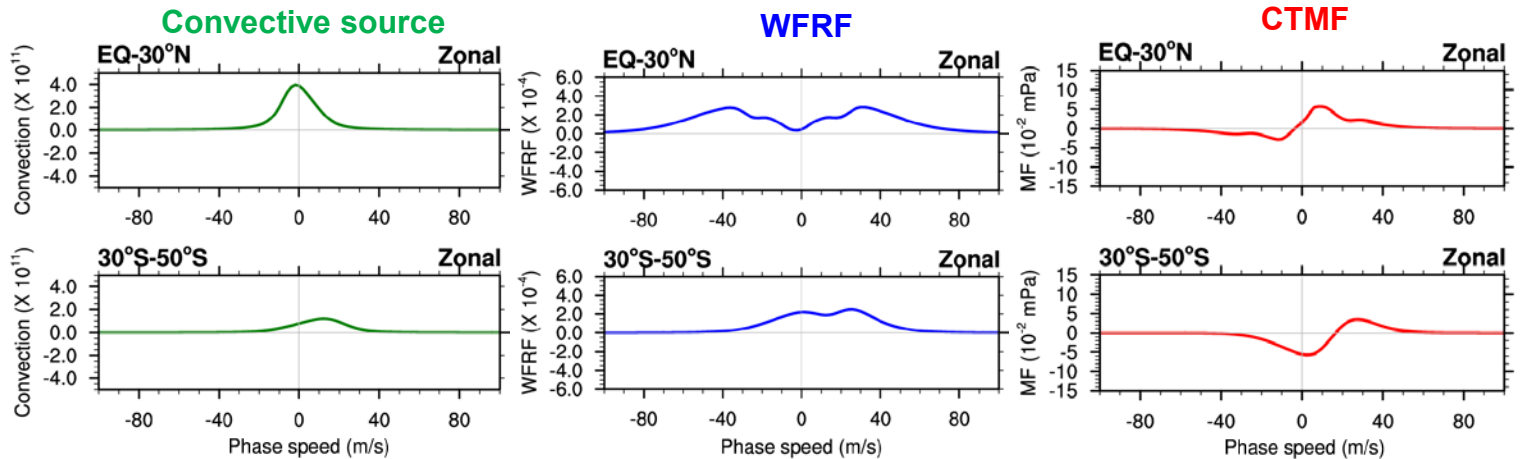


CTMF (CFRS)



Summer hemisphere subtropic

Winter hemisphere storm-track

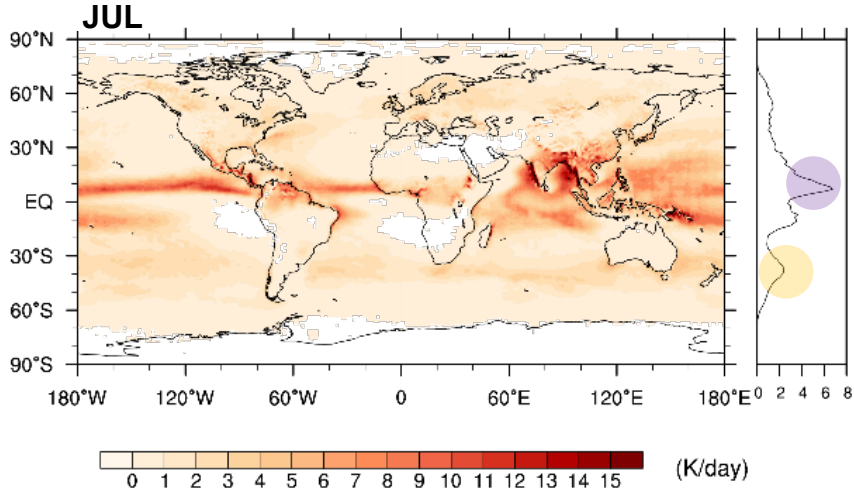


Spatial variability

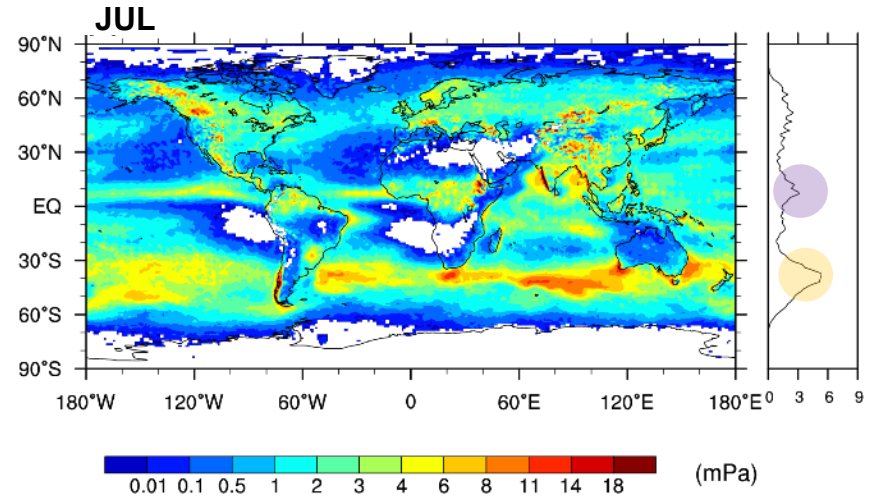
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

CTMF
WRF
Convective source \propto DCH

DCH (CFRS)

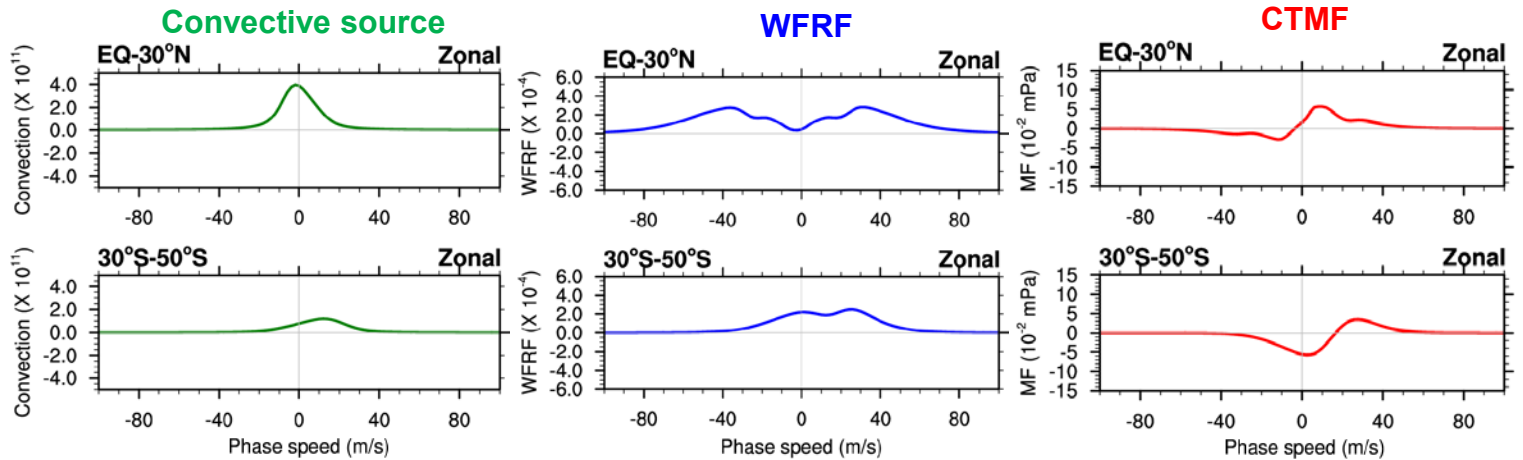


CTMF (CFRS)



Summer hemisphere subtropic

Winter hemisphere storm-track



CTMF formulation

Cloud-Top Momentum Flux spectrum

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U'_{ict}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

$F(\mu) = 1 / (1 + a\mu^b)$
 $a = 0.48792$ $b = 1.64896$

$$\mu = \frac{g Q_0 L}{c_p T_0 N_c U_c^2}$$

Nonlinearity

WFRF Convective source Nonlinear forcing effect

WFRF (wave-filtering and resonance factor)

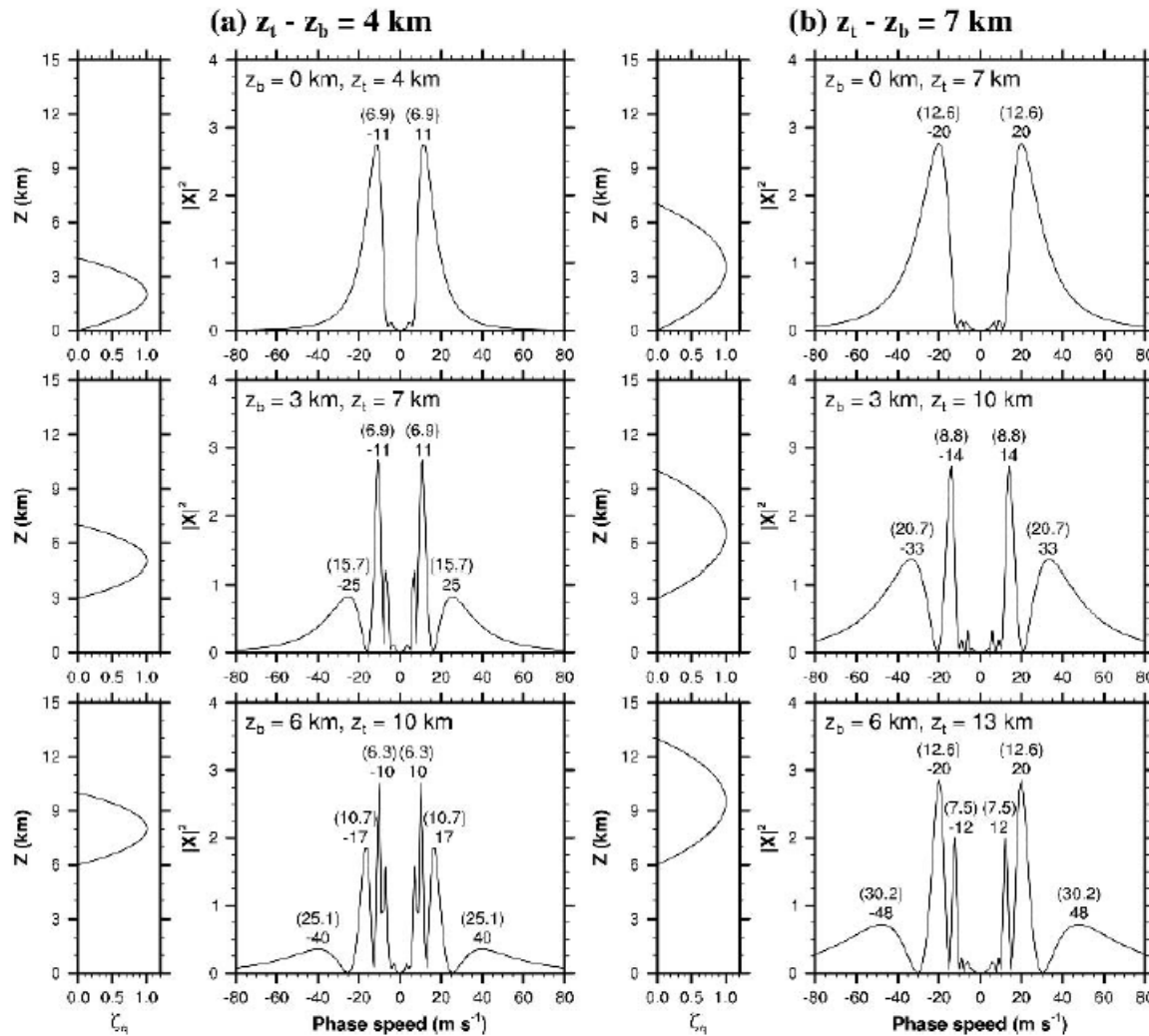
basic-state wind

stability

vertical configuration of heating profile

$$X = \begin{cases} \frac{X_{u1} X_{u2} (2Y_{u1} - \bar{X}_{u2} \bar{Y}_{u1}) + \bar{X}_{u1} \bar{X}_{u2} (2\bar{Y}_{u1} - X_{u2} Y_{u1})}{2(X_- X_{u1} X_{u2} + X_+ \bar{X}_{u1} \bar{X}_{u2})} & \text{for } U_0 = U_t, \\ \frac{X_{s4} \bar{Y}_{s3} (X_{s2} - X_{s3} X_{s0}) + \bar{X}_{s4} Y_{s3} (\bar{X}_{s3} - \bar{X}_{s2} X_{s0}) + X_{s5}}{X_- X_{s4} (X_{s2} - X_{s3} X_{s0}) + X_+ \bar{X}_{s4} (\bar{X}_{s3} - \bar{X}_{s2} X_{s0})} & \text{for } U_0 \neq U_t, \end{cases}$$

Wave-filtering and resonance factor



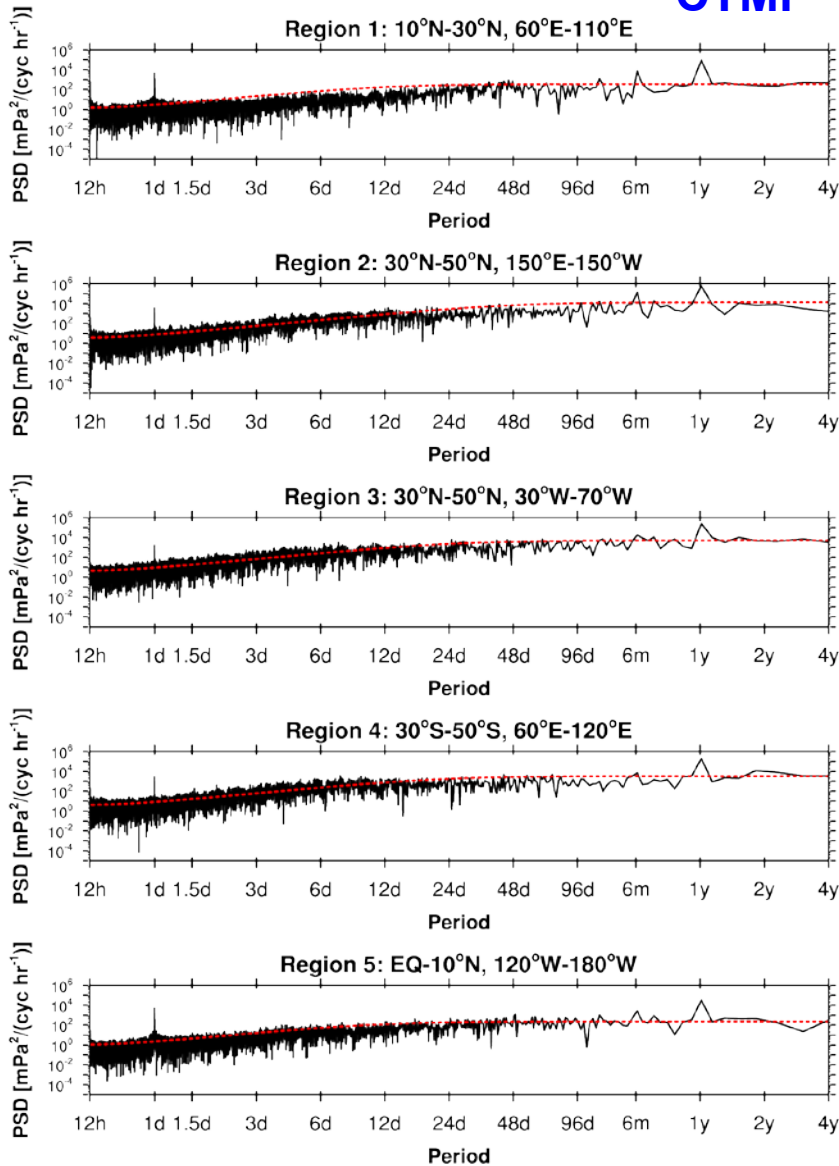
$$\lambda_z = 2\pi \frac{|U_t - c|}{N_2}$$

FIG. 4. The $|X|^2$ values for diabatic forcings with two different depths ($z_t - z_b$) of (a) 4 and (b) 7 km and their dependency on the center height $[(z_t + z_b)/2]$ of forcing under the vertically uniform basic-state wind ($U_0 = U_t = 0$ m s⁻¹) and stability ($N_1 = N_2 = 0.01$ rad s⁻¹) condition. Peak phase speeds are numbered over peaks, and numbers in parentheses are vertical wavelengths corresponding to the peak phase speeds.

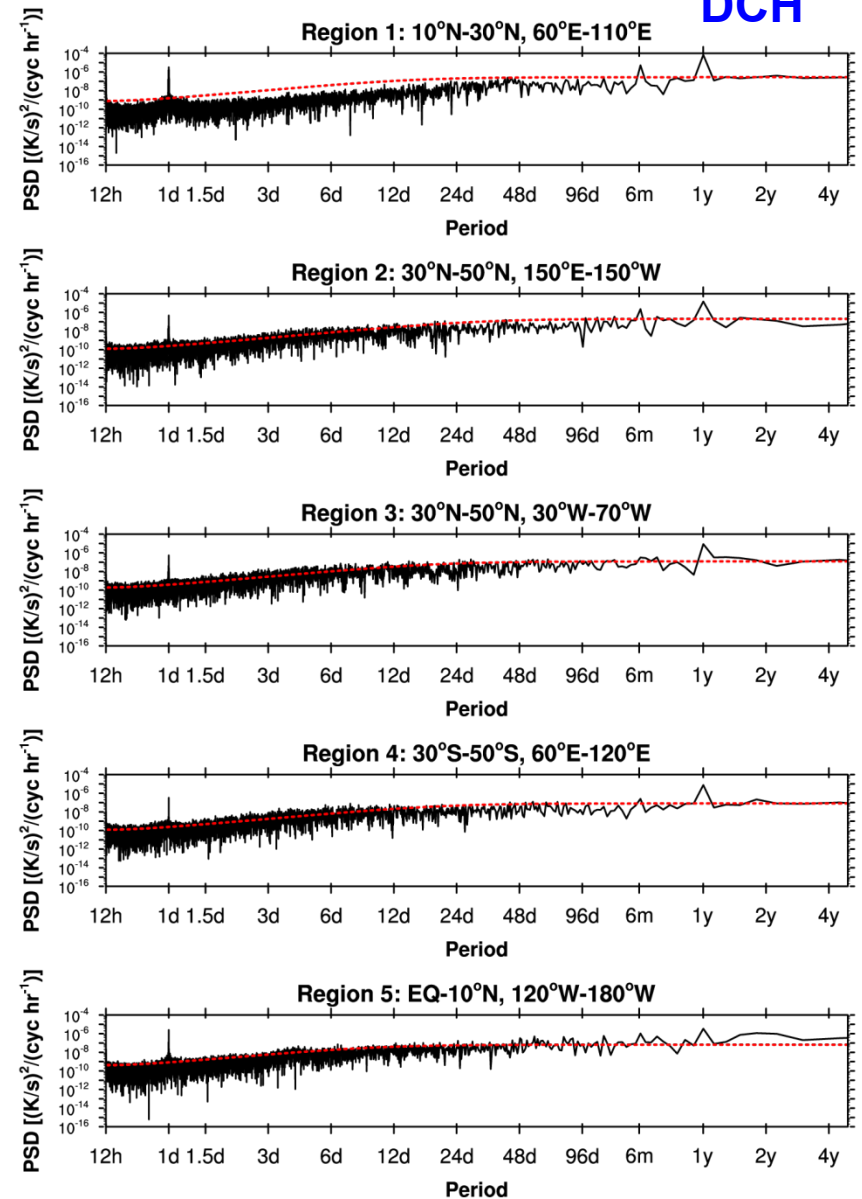
Spatiotemporal variations

Power Spectral Density

CTMF



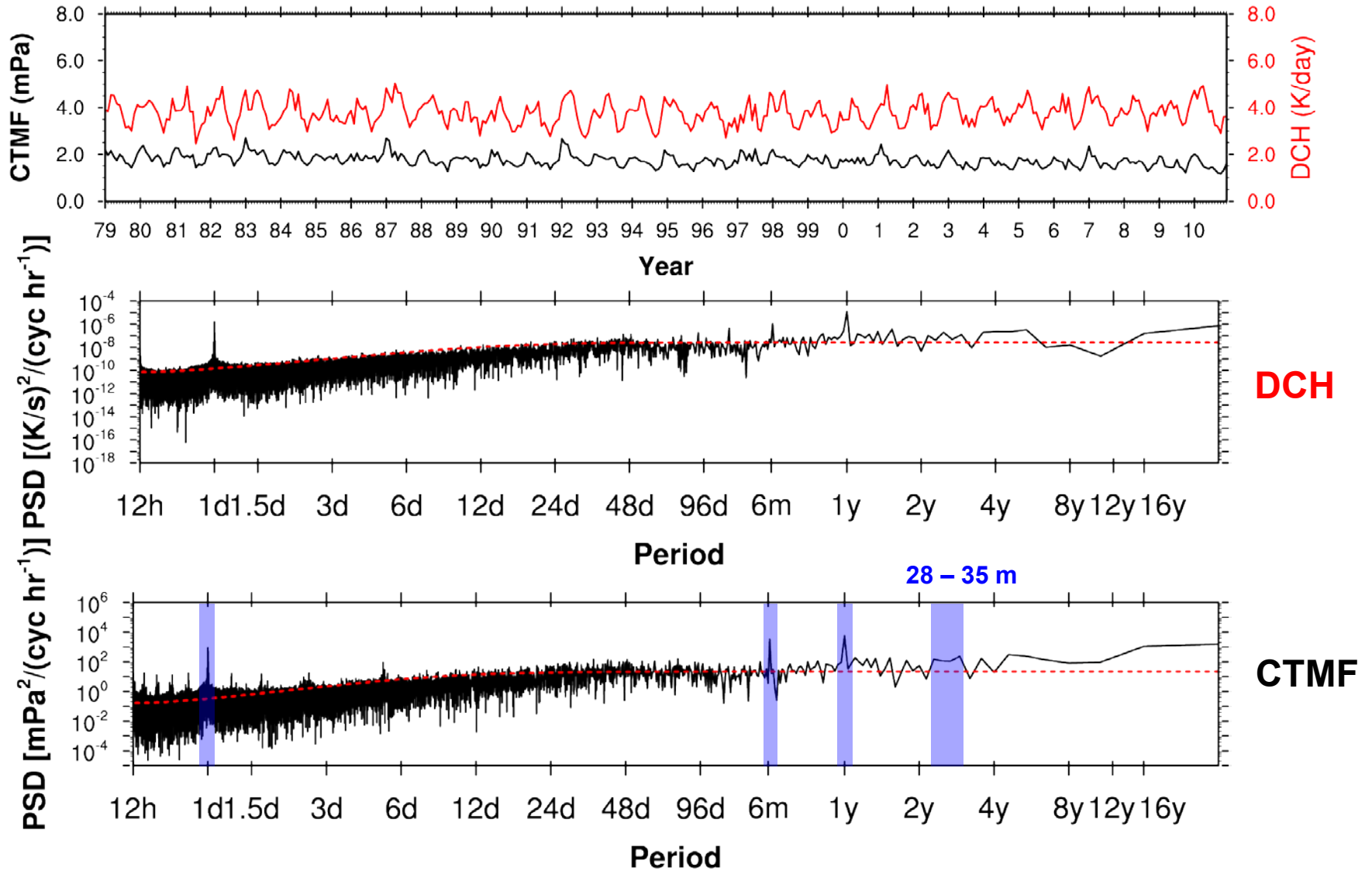
DCH



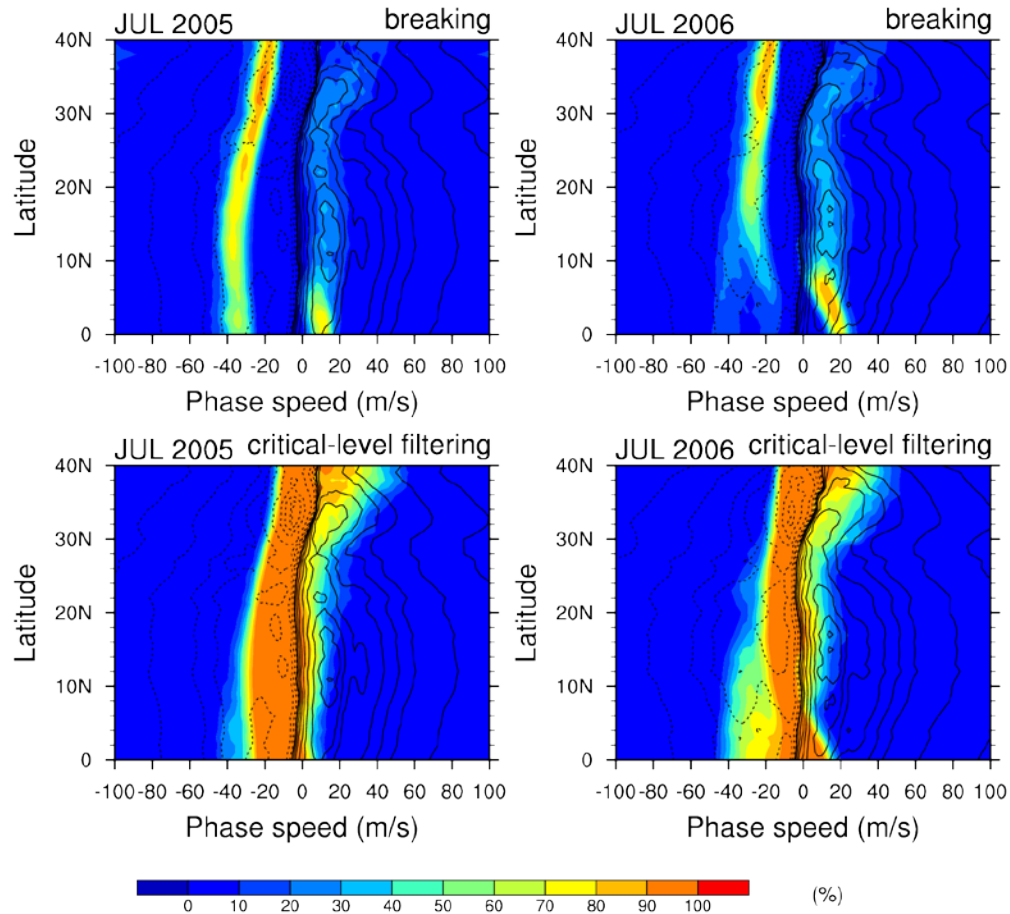
32 year time series & PSD of CTMF

5°S - 5°N

Correlation = 0.59
(maximum correlation at lag 0)

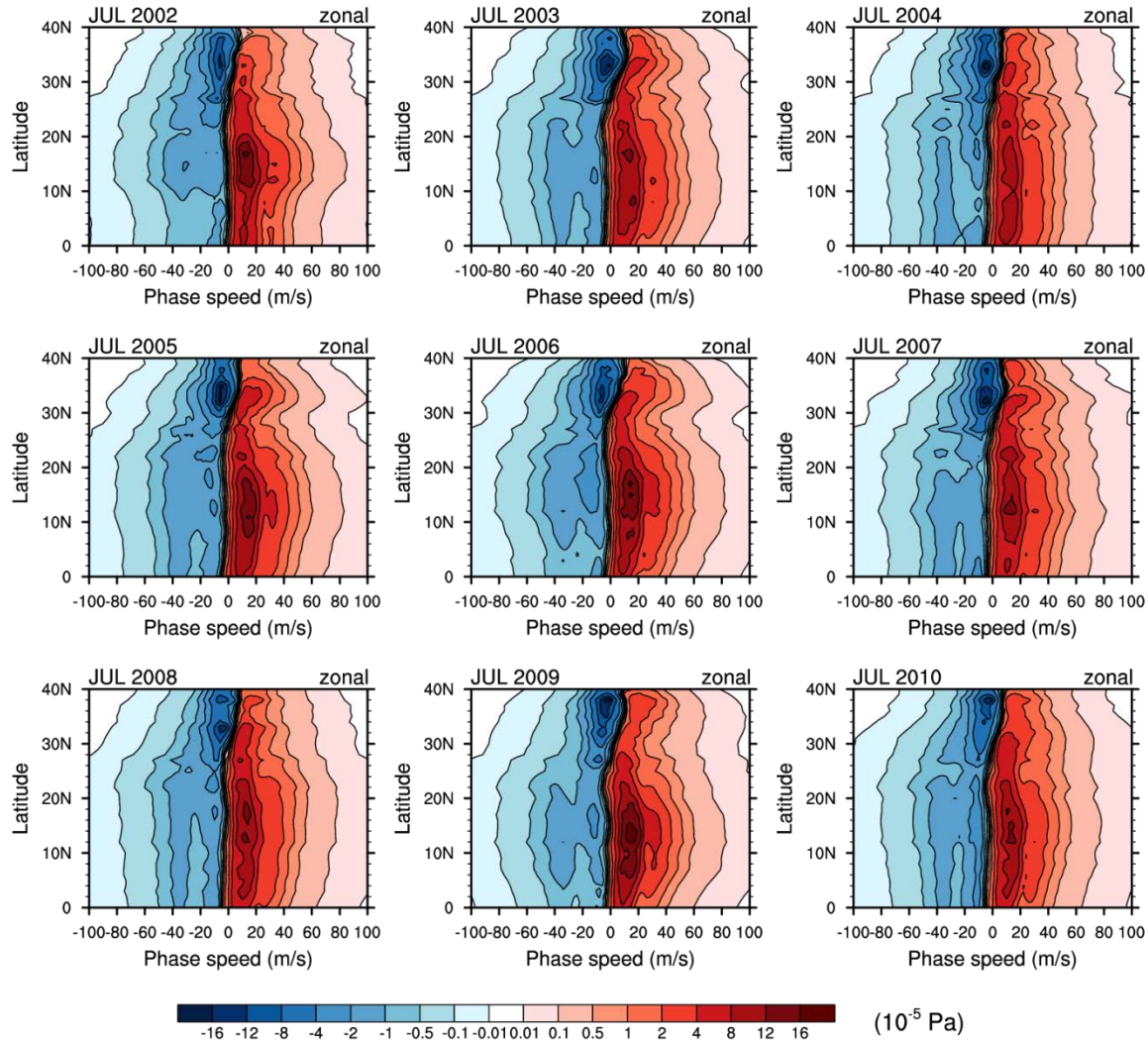


Percentage of each dissipation mechanism

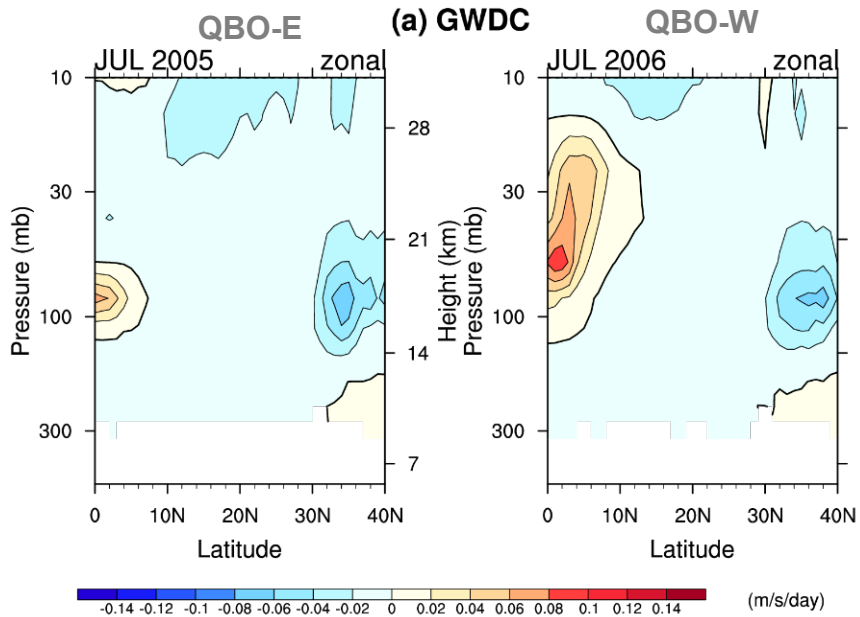


CTMF spectrum in ASM (2002-2010)

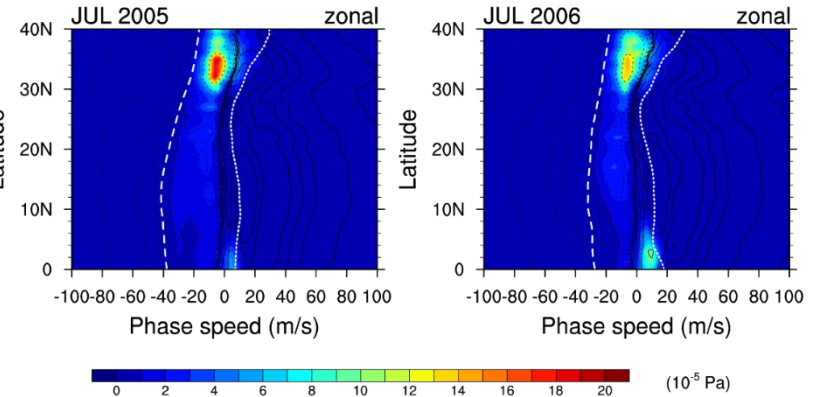
CTMF spectrum in ASM



CTMF spectrum ↔ GWDC

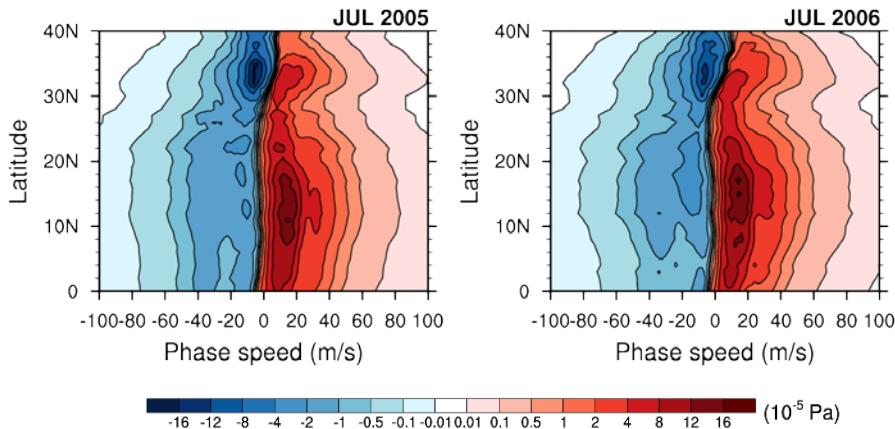


Difference in GWMF spectrum between cloud top and 10 hPa (=MF_{ct} - MF_{10 hPa})



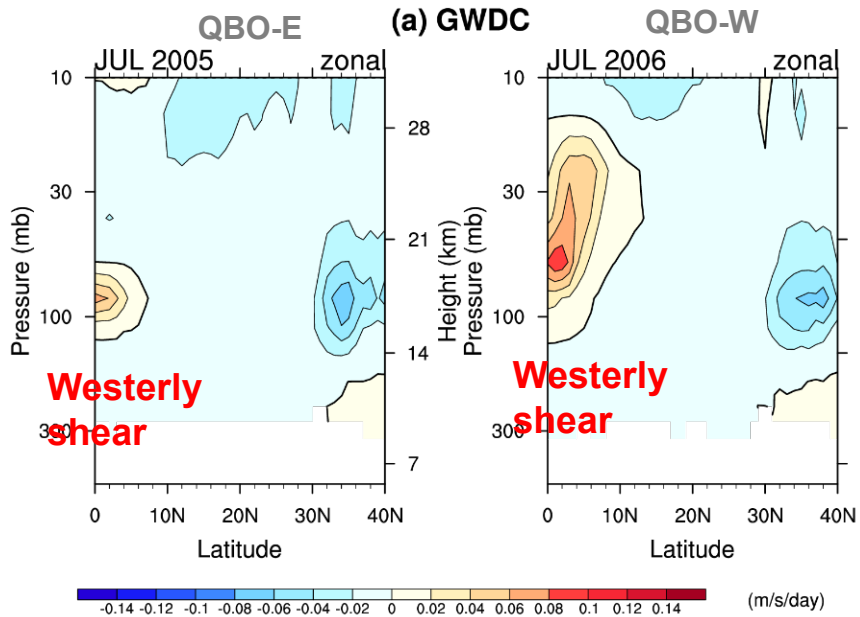
Dotted line: maximum wind
Dashed line: minimum wind

CTMF spectrum

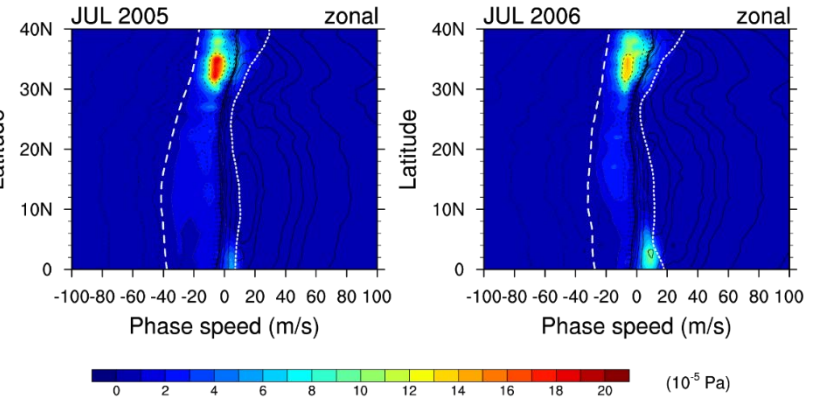


- Q.** Why is there strong drag in EQ-10°N & 30°N-40°N?
- A.** Within the filtering region, spectral peaks are located.

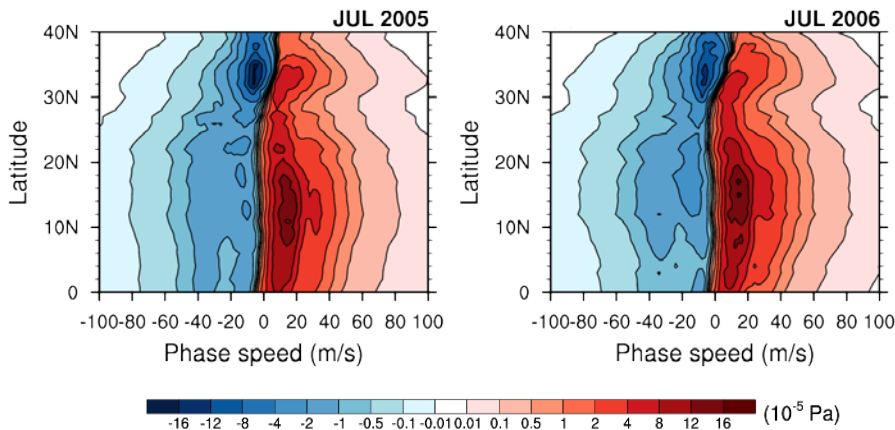
CTMF spectrum ↔ GWDC



Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

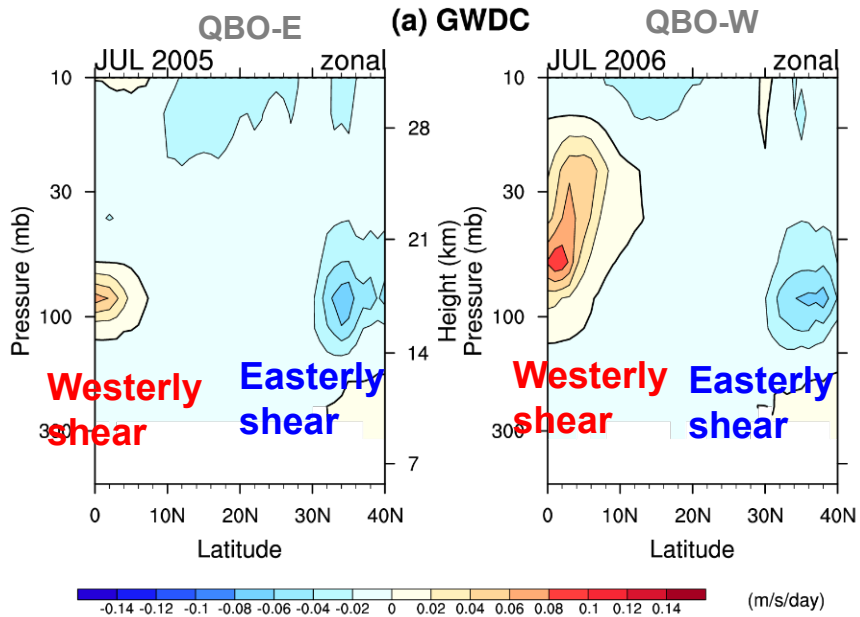


CTMF spectrum

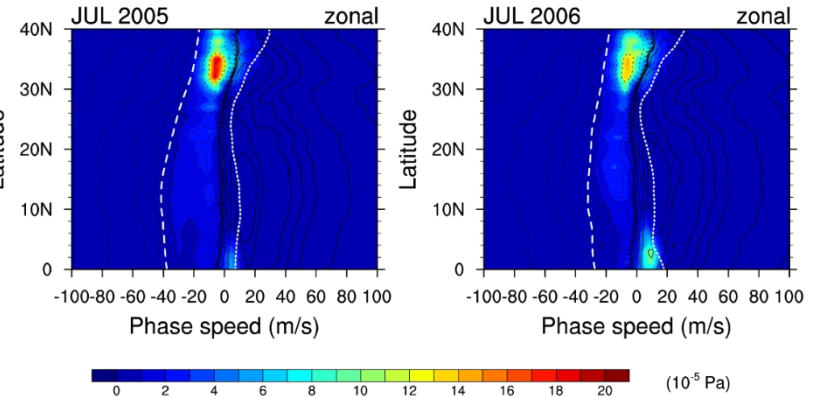


- Q. Why is there strong drag in EQ-10°N & 30°N-40°N?
- A. Within the filtering region, spectral peaks are located.

CTMF spectrum ↔ GWDC

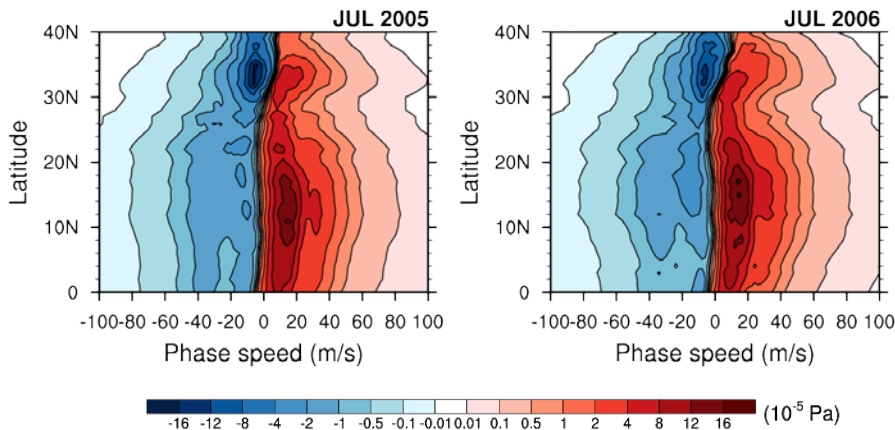


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



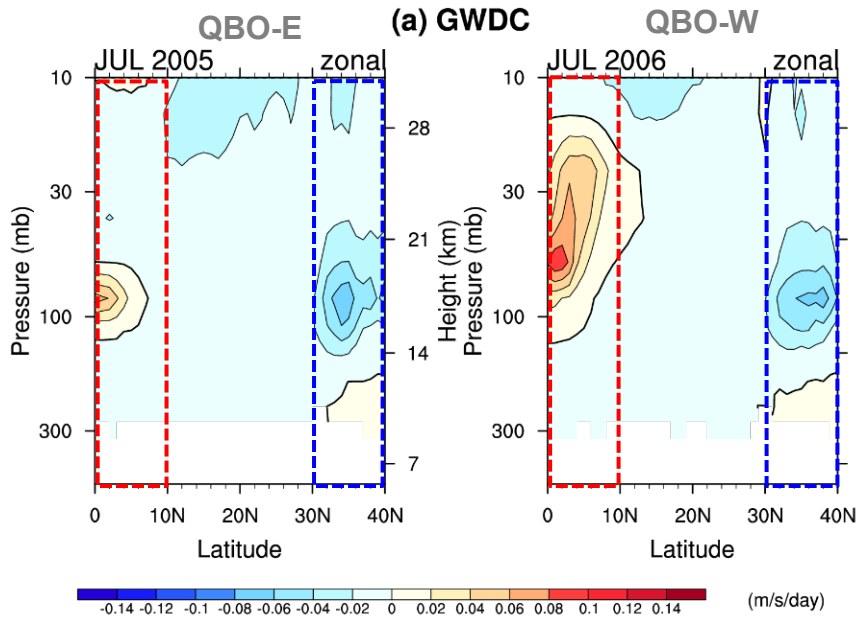
Dotted line: maximum wind
Dashed line: minimum wind

CTMF spectrum

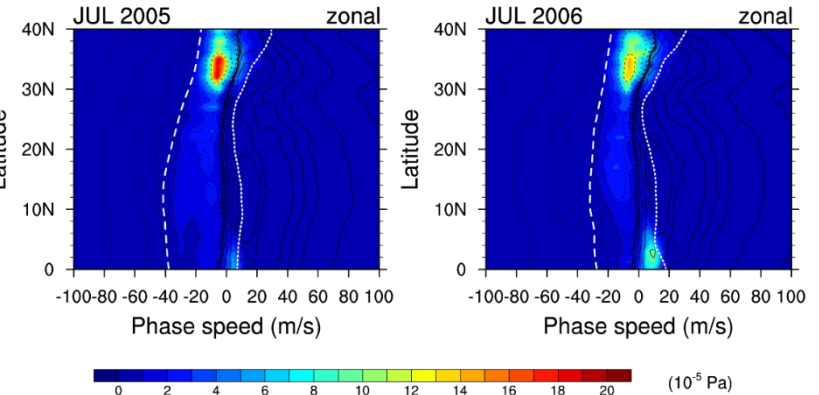


- Q.** Why is there strong drag in EQ-10°N & 30°N-40°N?
- A.** Within the filtering region, spectral peaks are located.

CTMF spectrum ↔ GWDC

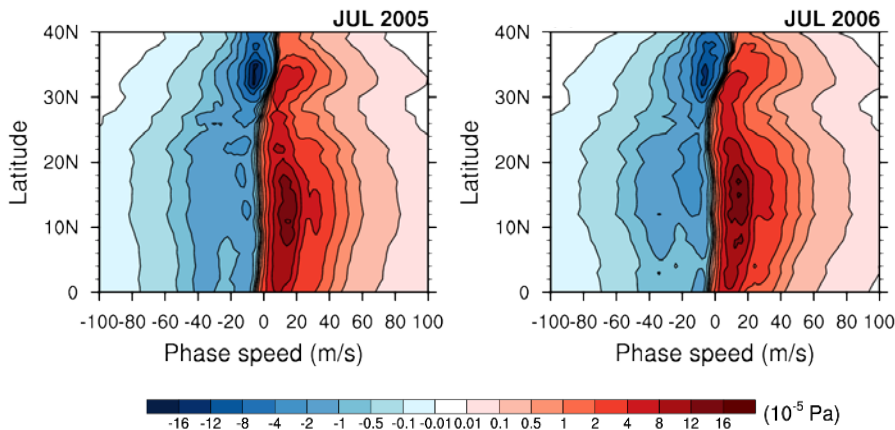


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



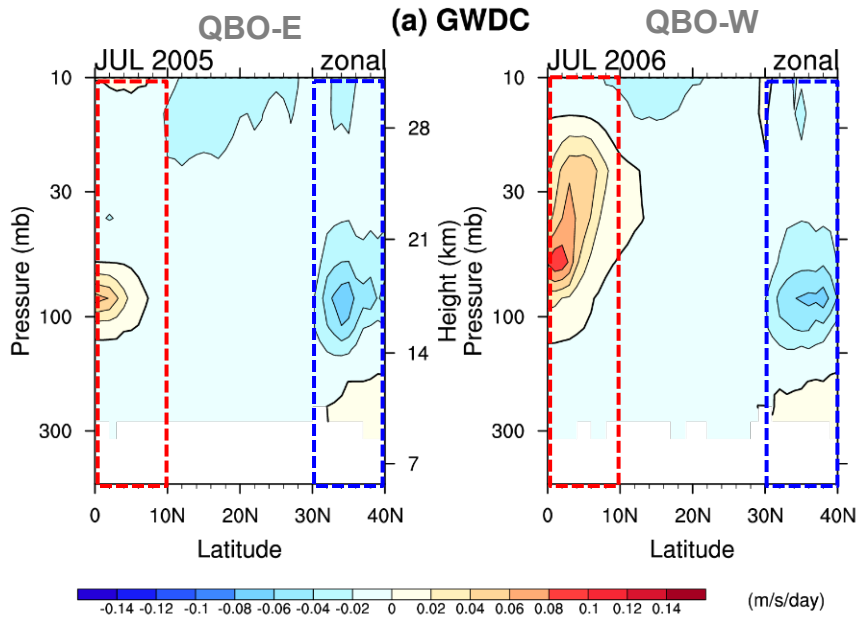
Dotted line: maximum wind
Dashed line: minimum wind

CTMF spectrum

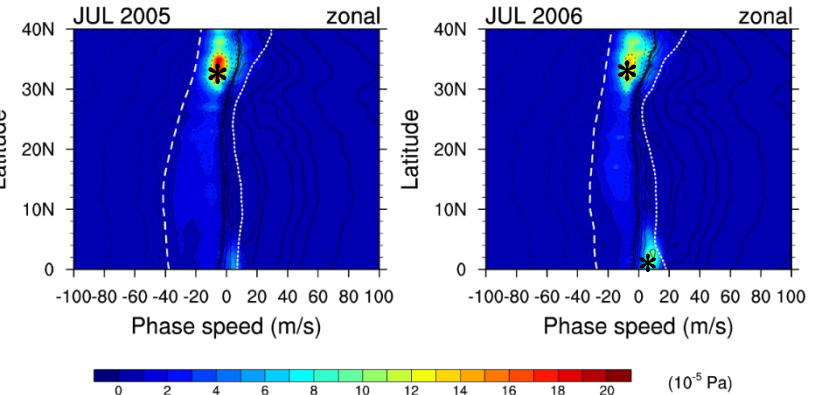


- Q.** Why is there strong drag in EQ-10°N & 30°N-40°N?
- A.** Within the filtering region, spectral peaks are located.

CTMF spectrum ↔ GWDC

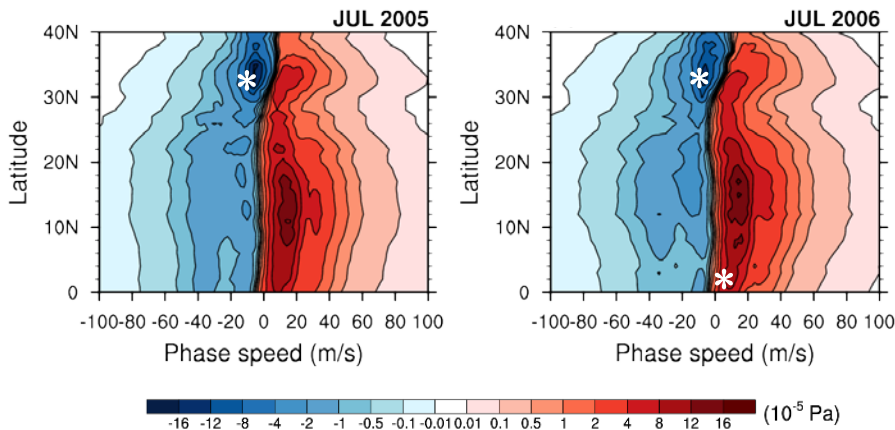


Difference in GWMF spectrum between cloud top and 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



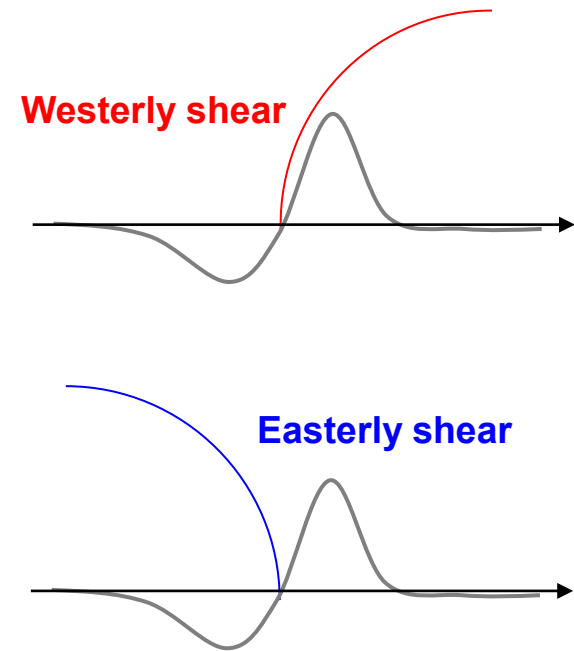
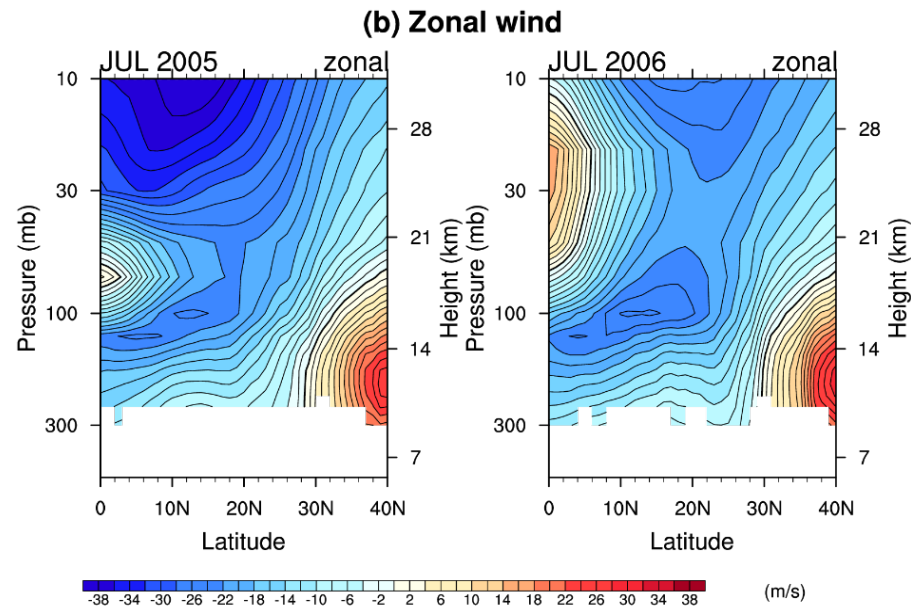
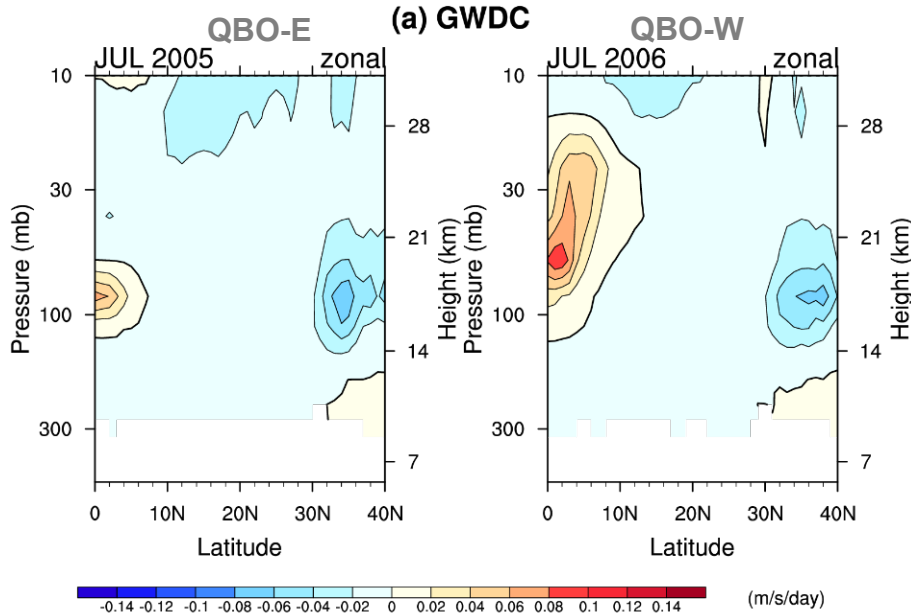
Dotted line: maximum wind
Dashed line: minimum wind

CTMF spectrum



- Q.** Why is there strong drag in EQ-10°N & 30°N-40°N?
- A.** Within the filtering region, spectral peaks are located.

CTMF spectrum \leftrightarrow GWDC

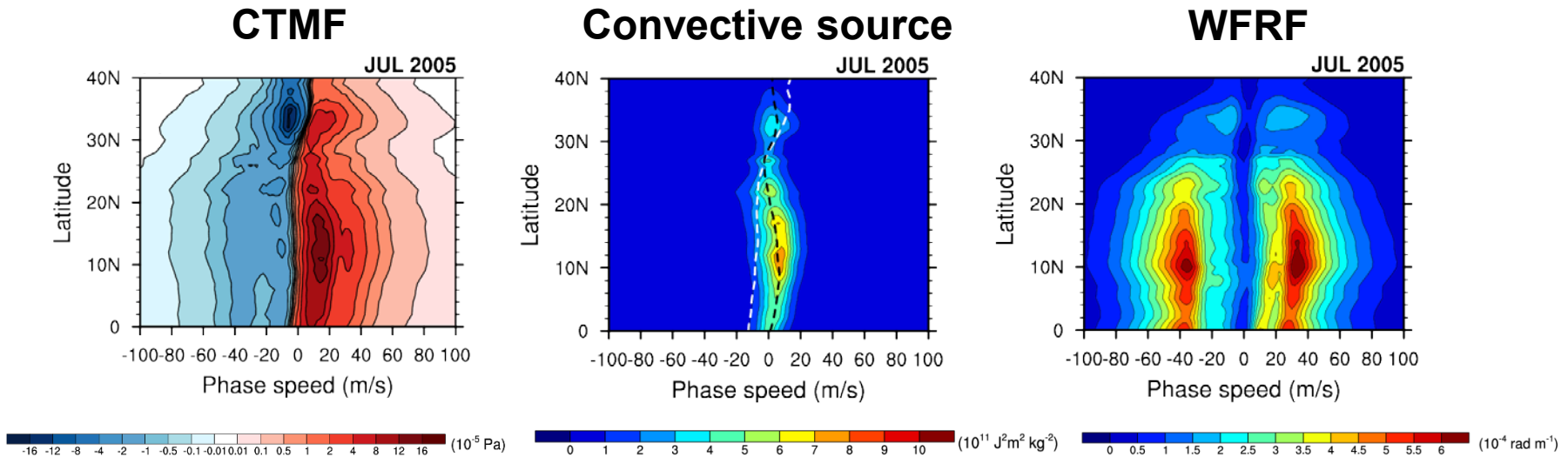


Q. What determines the sign of drag ?

A. Sign of the vertical wind shear (mainly due to the critical-level filtering)

CTMF spectrum Asian Summer monsoon region

$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$



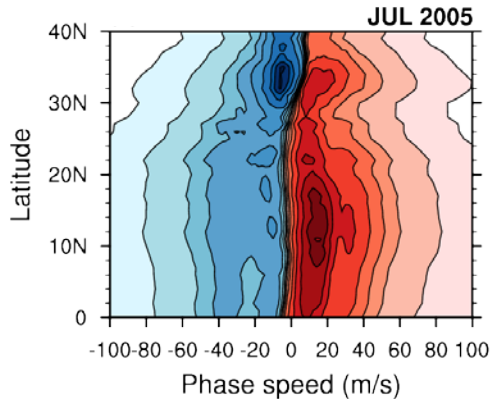
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

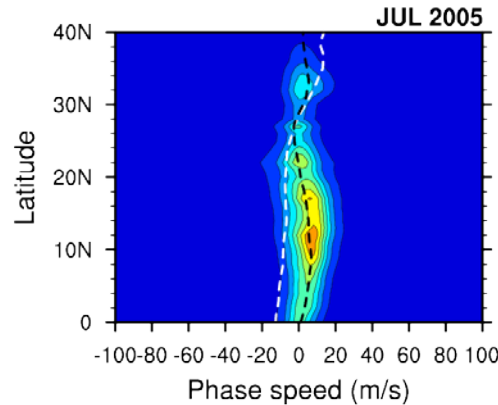
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

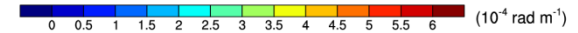
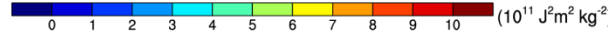
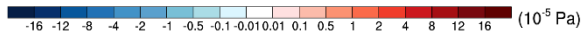
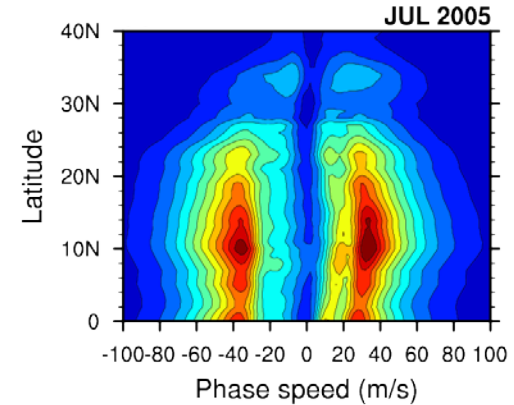
CTMF



Convective source



WFRF



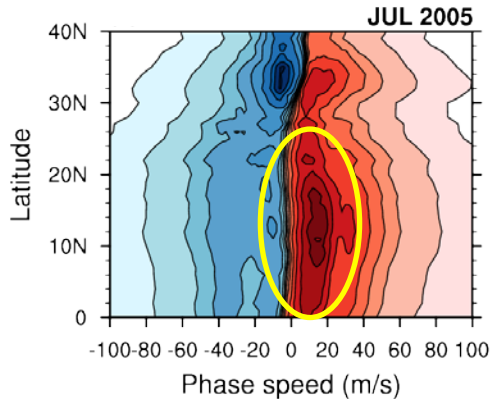
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

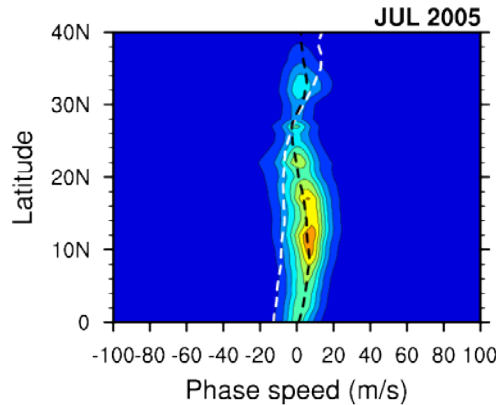
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

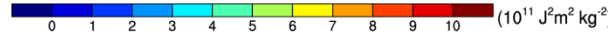
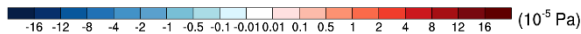
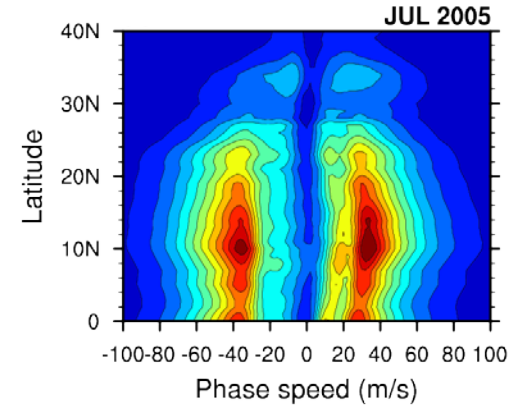
CTMF



Convective source



WFRF



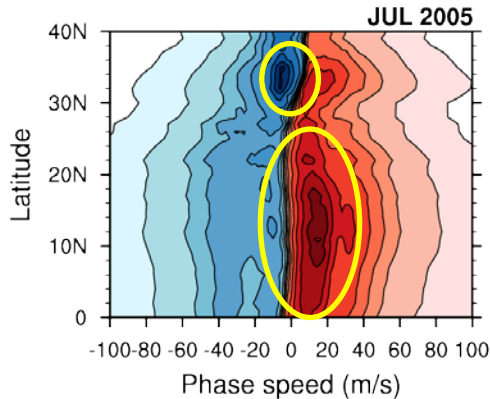
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

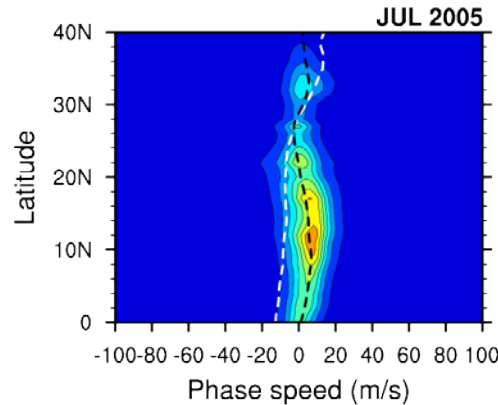
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

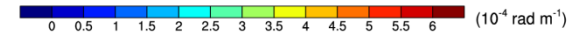
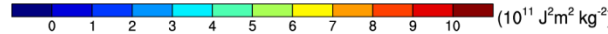
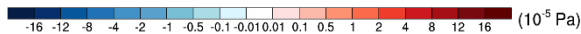
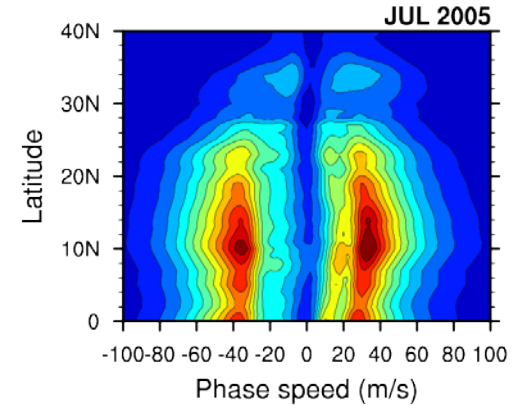
CTMF



Convective source



WFRF



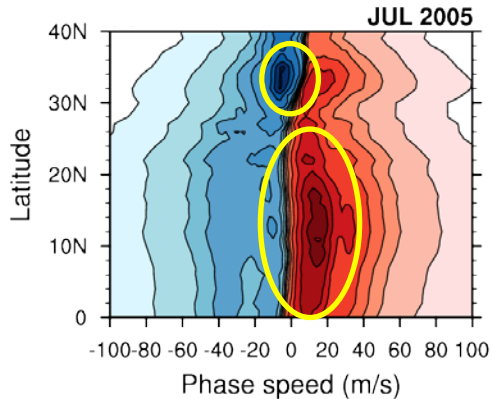
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

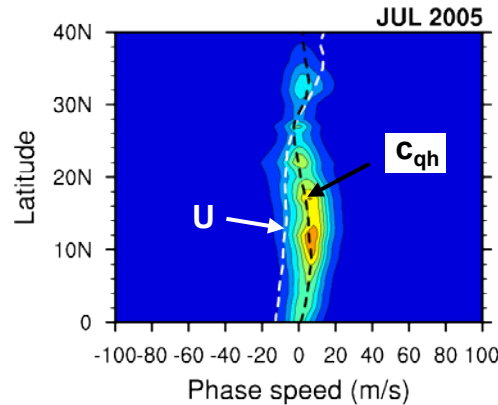
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

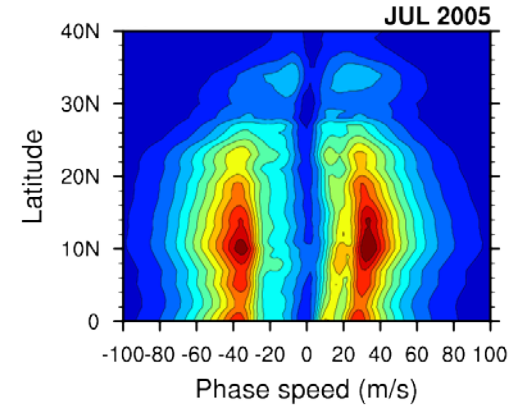
CTMF



Convective source



WFRF



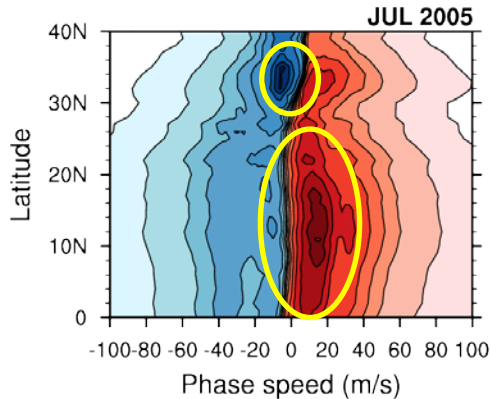
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

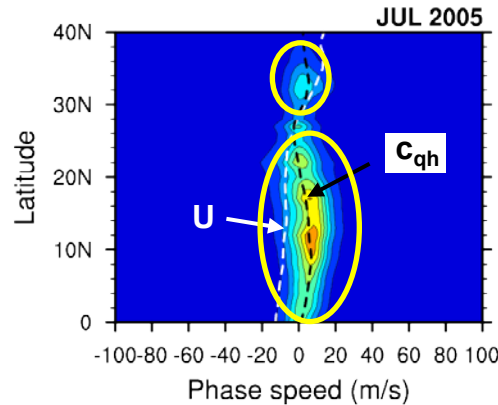
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

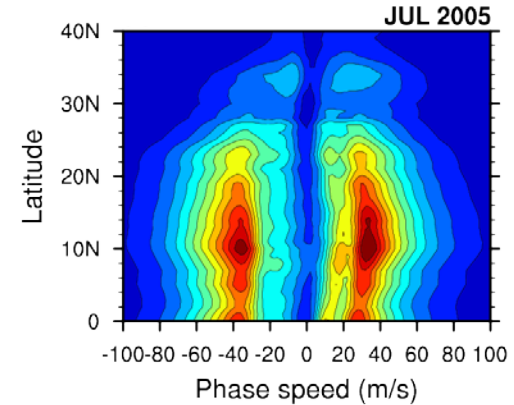
CTMF



Convective source



WFRF



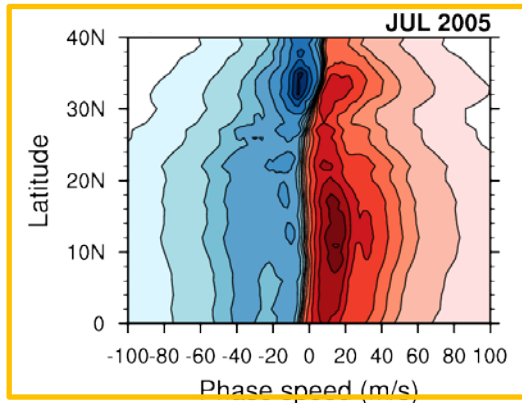
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

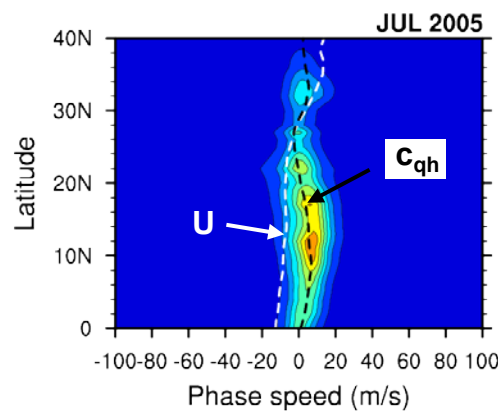
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

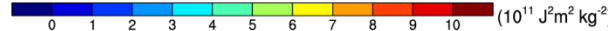
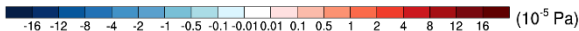
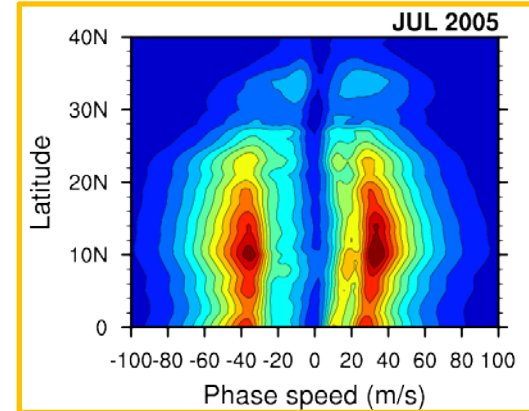
CTMF



Convective source



WFRF



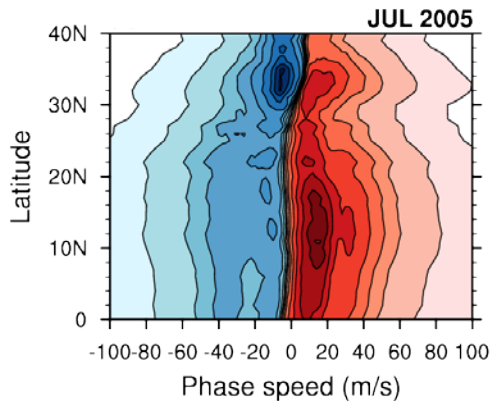
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

CTMF spectrum Asian Summer monsoon region

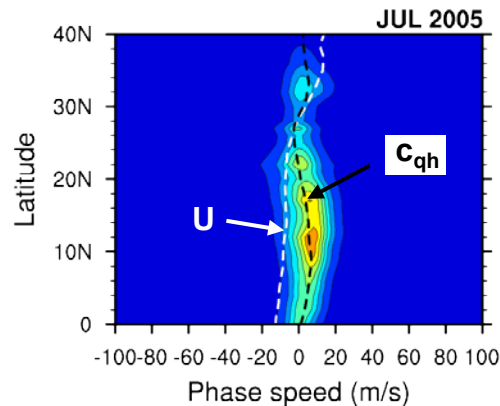
$$CTMF(c, \varphi) = \text{sgn}[c - U_{ct}(\varphi)] \rho_{ct} \frac{2(2\pi)^3}{A_h L_t} \left(\frac{g}{c_p T_q N_q^2} \right)^2 \times \frac{N_{ct} |X|^2}{|c - U_{ct}(\varphi)|} \Theta(c, \varphi) \times F(\mu)$$

WFRF Convective source

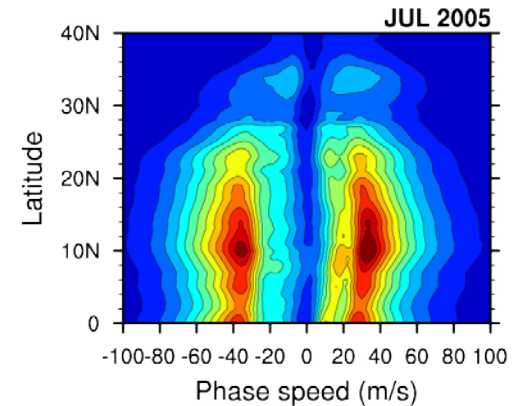
CTMF



Convective source



WFRF



Color scale for CTMF: (10^5 Pa)

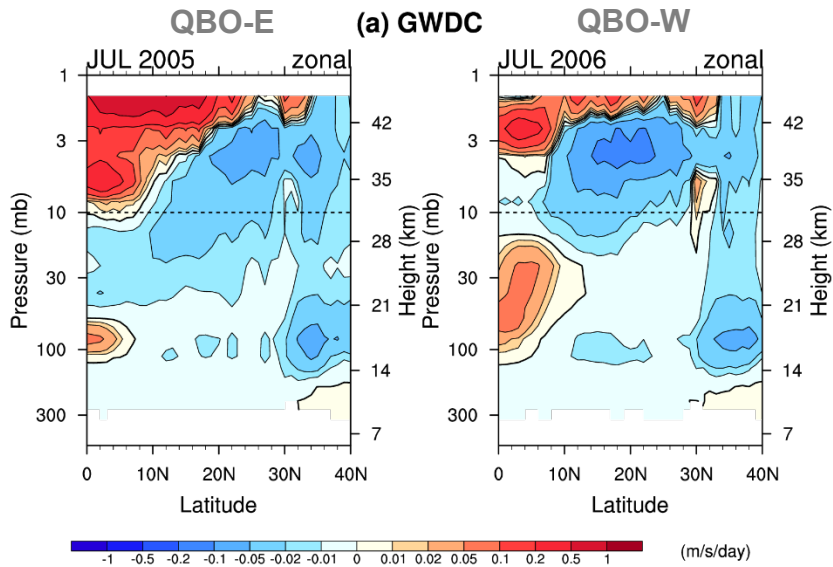
Color scale for Convective source: $(10^{11} \text{ J}^2 \text{ m}^2 \text{ kg}^{-2})$

Color scale for WFRF: $(10^4 \text{ rad m}^{-1})$

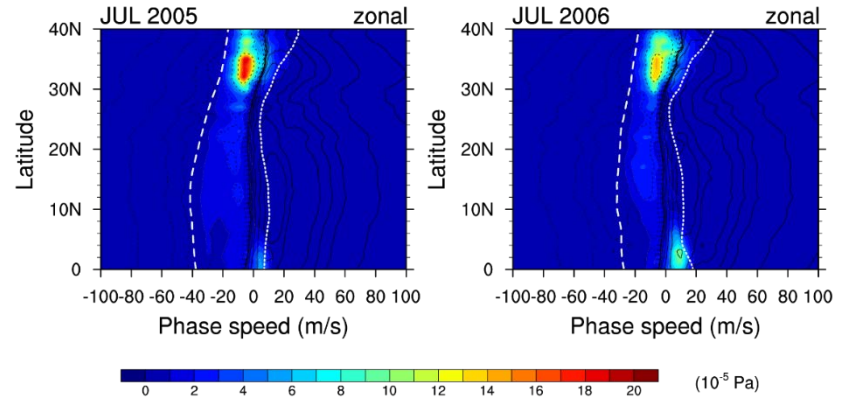
- **CTMF** spectrum is amplified at the phase speed corresponding to the **moving speed of convection (c_{qh})**
- The **width** of the CTMF is following **WFRF** (wave-filtering and resonance factor)
- Spectral combination of **convective source** and **WFRF** is important.

How this shape of the CTMF spectrum are linked to the GWDC?

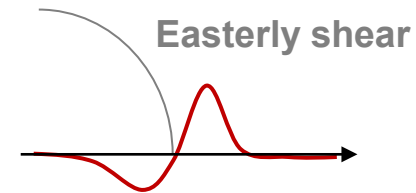
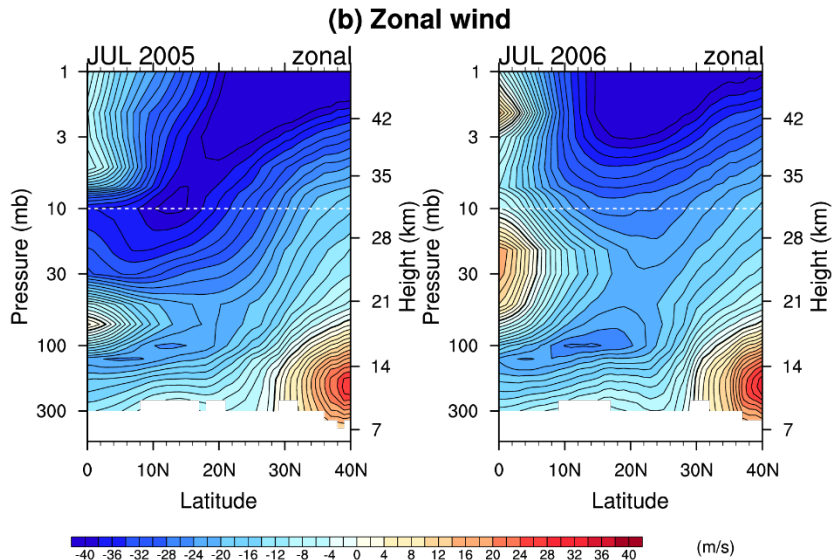
CTMF spectrum → GWDC



Difference in GWMF spectrum from cloud top to 10 hPa (=MF_{ct} - MF_{10 hPa})

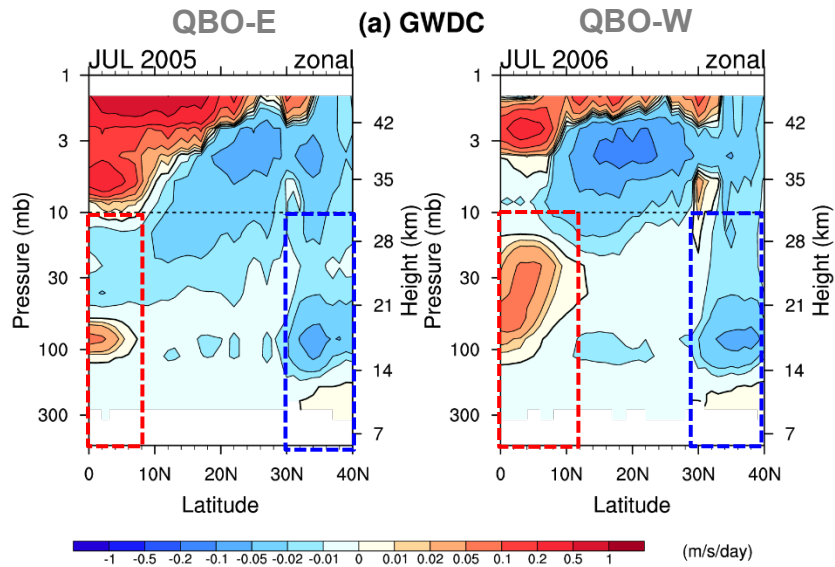


Solid line: maximum wind
Dashed line: minimum wind

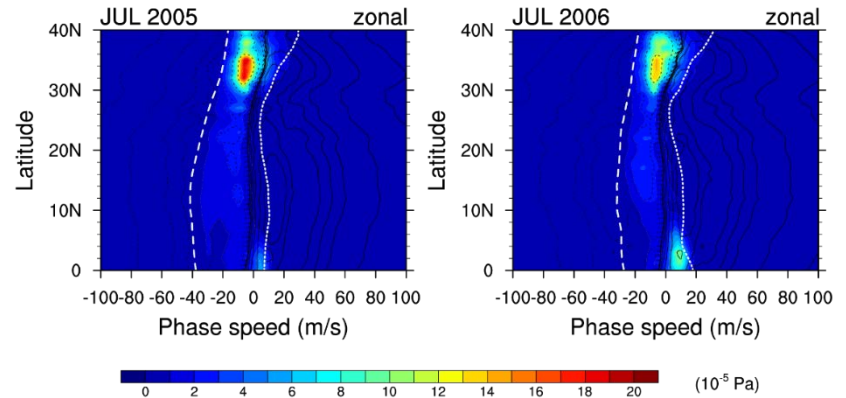


- Q.** What determines the sign of drag ?
- A.** Sign of the vertical wind shear (mainly due to the critical-level filtering)

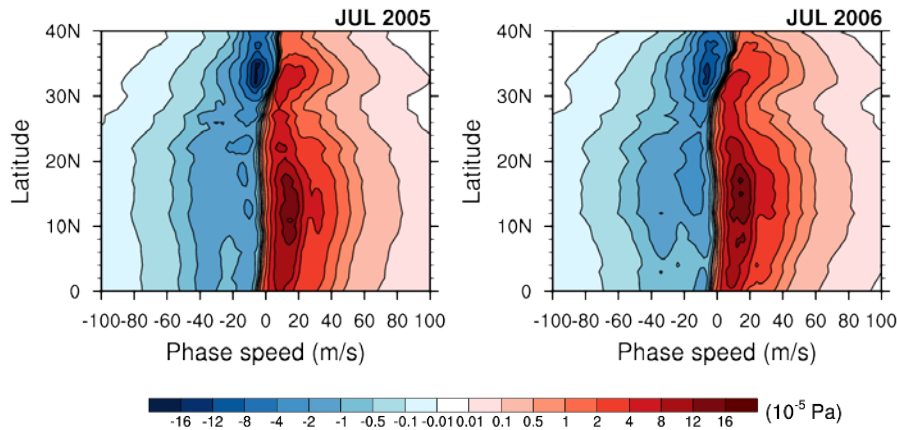
CTMF spectrum → GWDC



Difference in GWMF spectrum from cloud top to 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)

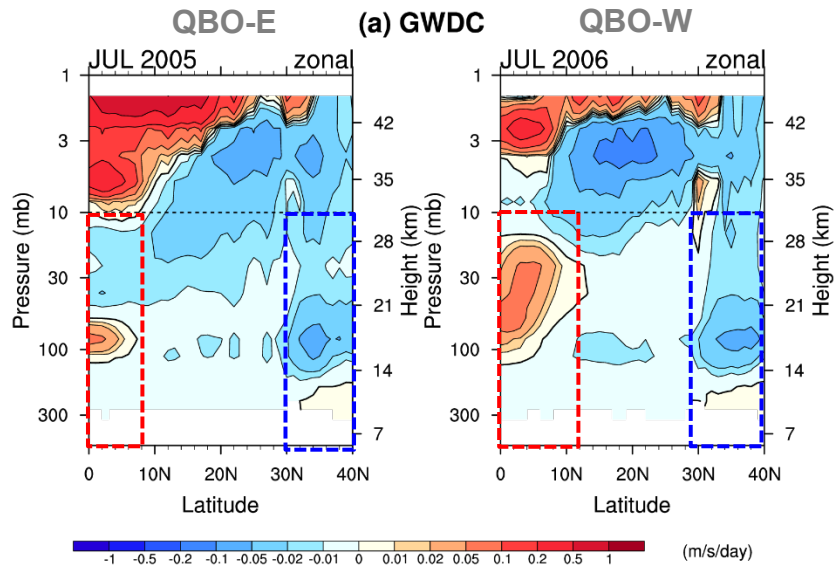


Solid line: maximum wind
Dashed line: minimum wind

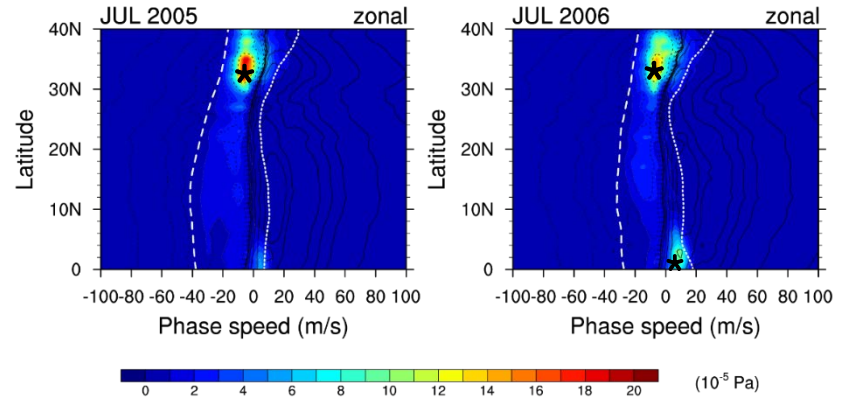


- Q. Why is there strong drag in **EQ-10°N** & **30°N-40°N**?
- A. **spectral peaks** are located.

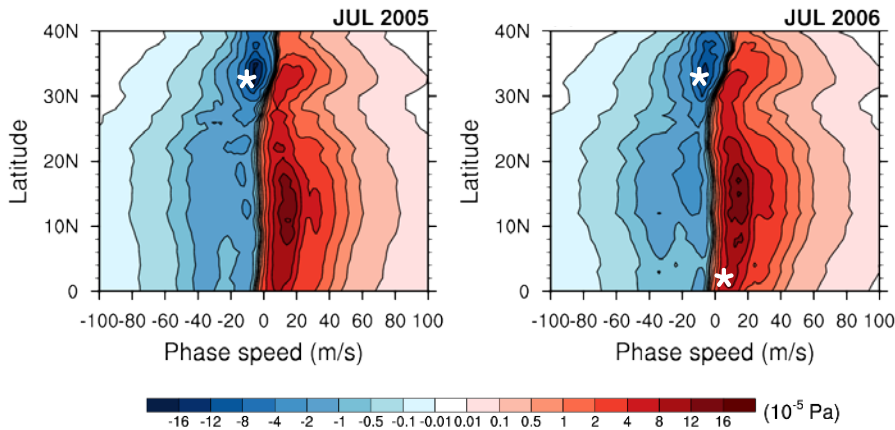
CTMF spectrum → GWDC



Difference in GWMF spectrum from cloud top to 10 hPa (=MF_{ct} - MF_{10 hPa})

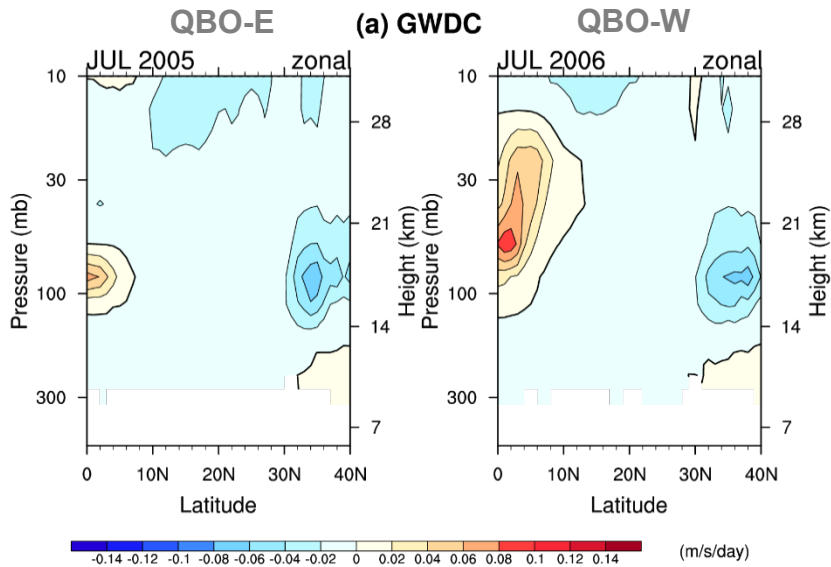


Solid line: maximum wind
Dashed line: minimum wind

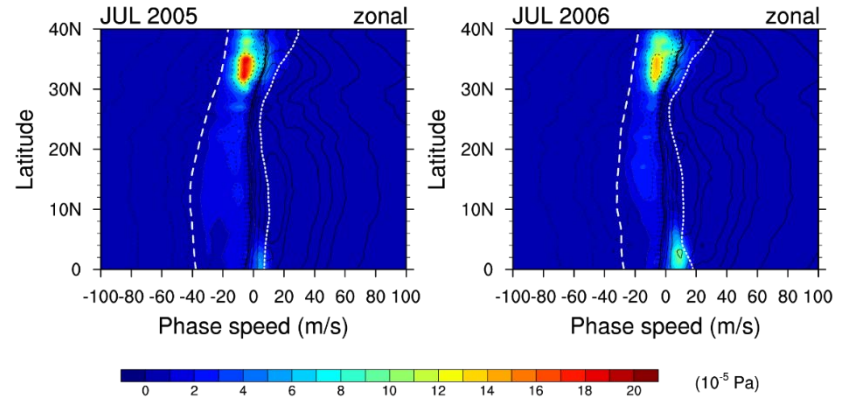


- Q. Why is there strong drag in **EQ-10°N** & **30°N-40°N**?
- A. **spectral peaks** are located.

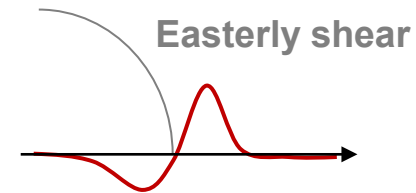
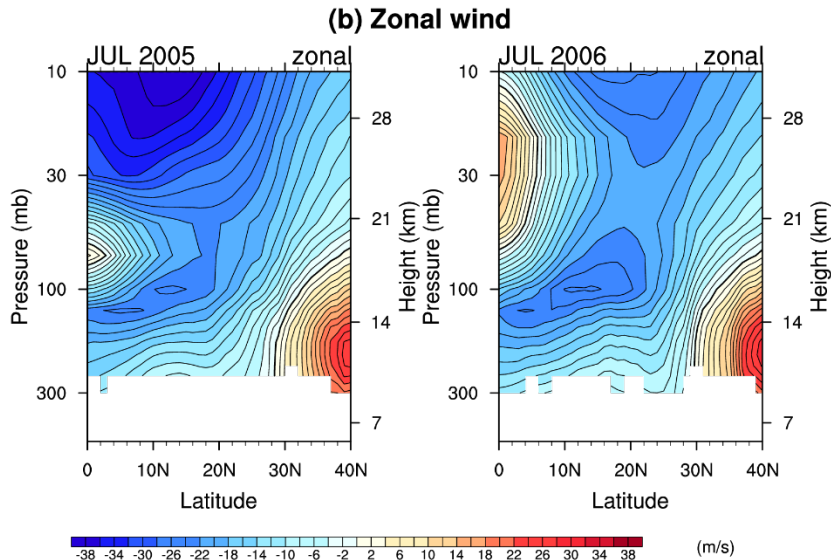
CTMF spectrum ↔ GWDC



Difference in GWMF spectrum from cloud top to 10 hPa ($=MF_{ct} - MF_{10\text{ hPa}}$)



Solid line: maximum wind
 Dashed line: minimum wind



- Q.** What determines the sign of drag ?
- A.** Sign of the vertical wind shear (mainly due to the critical-level filtering)

Motivation

- Parameterizations of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) showed that momentum flux of CGWs at the source-level is determined not only from **convective source** but also from wave-filtering and resonance factor (**WFRF**).
- Choi and Chun (2011) **updated** and **validated** Song and Chun (2005) by comparing source-level (cloud-top) gravity wave momentum flux (**CTMF**) spectra with those from **3-D mesoscale simulation**.
- Implementation of this parameterization to global climate model (**GCM**) reproduced quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013).
- In this study, we focus on understanding CTMF spectrum and its **variation** through the **long-term off-line** calculation of Choi and Chun (2011). Also we find connection between CTMF spectrum and the gravity-wave drag (GWDC).

Motivation

- Parameterizations of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) showed that momentum flux of CGWs at the source-level is determined not only from **convective source** but also from wave-filtering and resonance factor (**WFRF**).
- Choi and Chun (2011) **updated** and **validated** Song and Chun (2005) by comparing source-level (cloud-top) gravity wave momentum flux (**CTMF**) spectra with those from **3-D mesoscale simulation**.
- Implementation of this parameterization to global climate model (**GCM**) reproduced quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013). → **On-line test**
- In this study, we focus on understanding CTMF spectrum and its **variation** through the **long-term off-line** calculation of Choi and Chun (2011). Also we find connection between CTMF spectrum and the gravity-wave drag (GWDC).

Motivation

- Parameterizations of convectively induced gravity waves (**CGWs**) have been developed based on **analytical formulation** of gravity wave momentum flux at the **source-level** (Beres et al. 2004; Song and Chun 2005).
- Song and Chun (2005) is **updated** and **validated** by comparing source-level (cloud-top) gravity wave momentum flux (**CTMF**) spectra with those from **3-D mesoscale simulation** (Choi and Chun 2011).
- Implementation of this parameterization to global climate model (**GCM**) yields well-simulated quasi-biennial oscillation (**QBO**) (Kim et al. 2013) and reduced excessively strong **polar night jet** in the southern hemisphere (Choi and Chun 2013).

Summary and conclusion

Spatiotemporal variations in CTMF

- CTMF is determined not only by magnitude of heating but also by vertical shape of the heating, wave propagation condition, wave nonlinearity.
- CTMF spectrum is highly fluctuate with both time and space in terms of its shape and magnitude.

CTMF spectrum and GWDC in Asian summer monsoon region

- The sign of GWDC is determined by the background wind.
 - There exists westerly (easterly) drag in the westerly (easterly) shear region.
- The magnitude of GWDC is largely influenced by the CTMF spectrum.
 - Maximum drag is located in the region where wave dissipation is occurred at the spectral peak of CTMF spectrum.

→ Physically and mathematically consistent source spectrum (CTMF) of CGWs is required for realistic spatiotemporal variabilities in GWDC of the stratosphere.