

# Investigation of gravity waves in the troposphere and stratosphere based on radiosonde observations at Lauder (45 °S 169 °E) during DEEPWAVE-NZ

1 S. Gisinger, A. Dörnbrack, B. Ehard, B. Kaifler, N. Kaifler,  
1,2 M. Rapp, 2 M. Garhammer  
1,3 M. Bramberger, T. Portele, M. Siller

1 Institut für Physik der Atmosphäre DLR

2 Meteorologisches Institut, Ludwig-Maximilians-Universität

3 Institute of Atmospheric and Cryospheric Sciences, University of Innsbruck



DEEPWAVE Community



Knowledge for Tomorrow



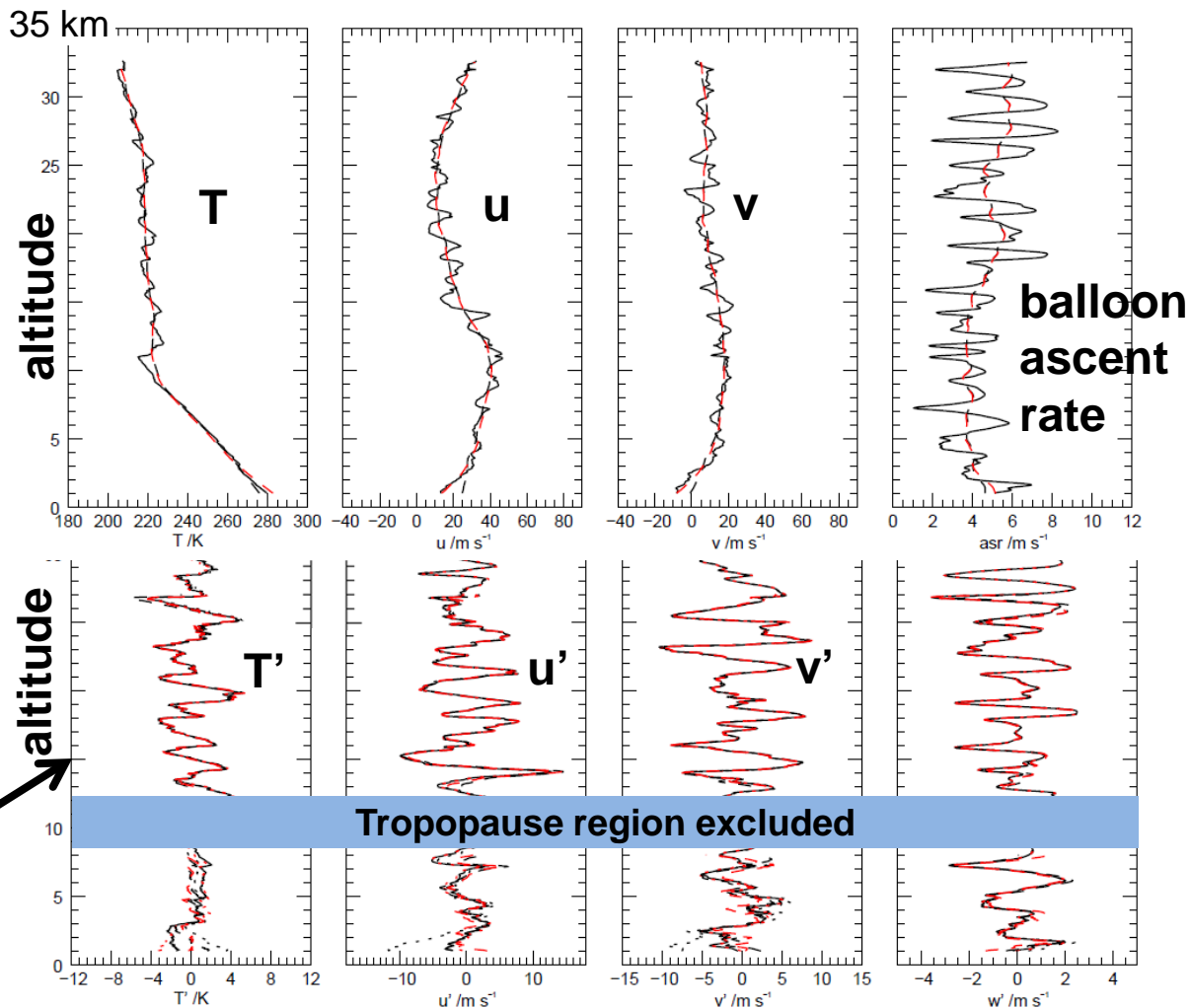
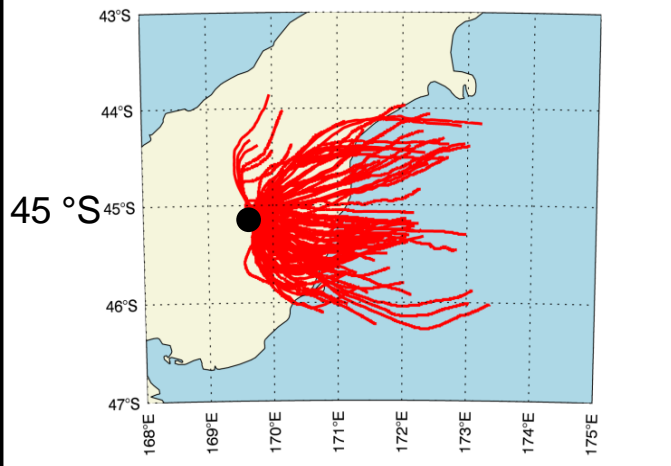
# Analysis of radiosonde data

altitude profiles



## DEEPAVE LAUDER soundings

98 soundings during  
14 intensive observation  
periods (IOPs)



## perturbation profiles

measured profile minus background fit  
(2<sup>nd</sup>-polynomial-fit with  
additional 5-km running mean)

Assumption: perturbations are caused by GWs



# Analysis of radiosonde data

- perturbations of **different variables** are **sensitive to different parts of the GW spectrum** (Lane et al 2000, Lane et al 2003, Geller and Gong 2010)

$$\frac{m^2}{k^2+l^2} = \frac{N^2-\Omega^2}{\Omega^2-f^2}$$

**amplitude horizontal wind**

$$A_u = \frac{-lA_v + mA_w}{k}$$

**amplitude vertical wind**

$$A_w = \frac{-kA_u + lA_v}{m}$$



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➤  $\Omega \rightarrow f: m \uparrow, k \downarrow, |A_u| \uparrow$

→ measurements of **hz. wind** emphasize **low frequency waves** (inertia-GWs)

- Gravity wave **energies** (Geller and Gong 2010)

– **kinetic energy:**  $\langle KE_{mass} \rangle = \frac{1}{2} [\langle u'^2 + v'^2 \rangle]$  low frequency/inertia-GWs



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– **potential energy:**  $\langle PE_{mass} \rangle = \frac{1}{2} \frac{g^2}{N^2} \langle \frac{T'^2}{T_b^2} \rangle$  mixed

– **vertical energy:**  $\langle VE_{mass} \rangle = \frac{1}{2} \langle w'^2 \rangle$  high frequency GWs



# When can soundings be treated as vertical profiles?

- drift of the balloon is small enough compared to wave scales
- ascent of the balloon is fast enough compared to wave scales and wave frequency

$$\left| \frac{kU + lV}{m\overline{W}_B} \right| \ll 1$$

$$\frac{\omega}{m\overline{W}_B} \ll 1$$

$k, l, m$  ... wavenumbers

$U, V$  ... hz. background wind

$\overline{W}_B$  ... mean balloon ascent rate

$\omega$  ... frequency

(Gardener and Gardener  
1993, Reeder et al. 1999,  
Lane et al. 2003)

- ✓ **low frequency/inertia-GWs**, e.g. when **horizontal velocity** perturbations are analyzed
- ✗ for **medium and high frequency GWs**, e.g. when **vertical velocity**/balloon ascent rate is analyzed (horizontal projection method, Shutts et al 1988, Lane et al 2000, Reeder et al 1999)



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**this talk**

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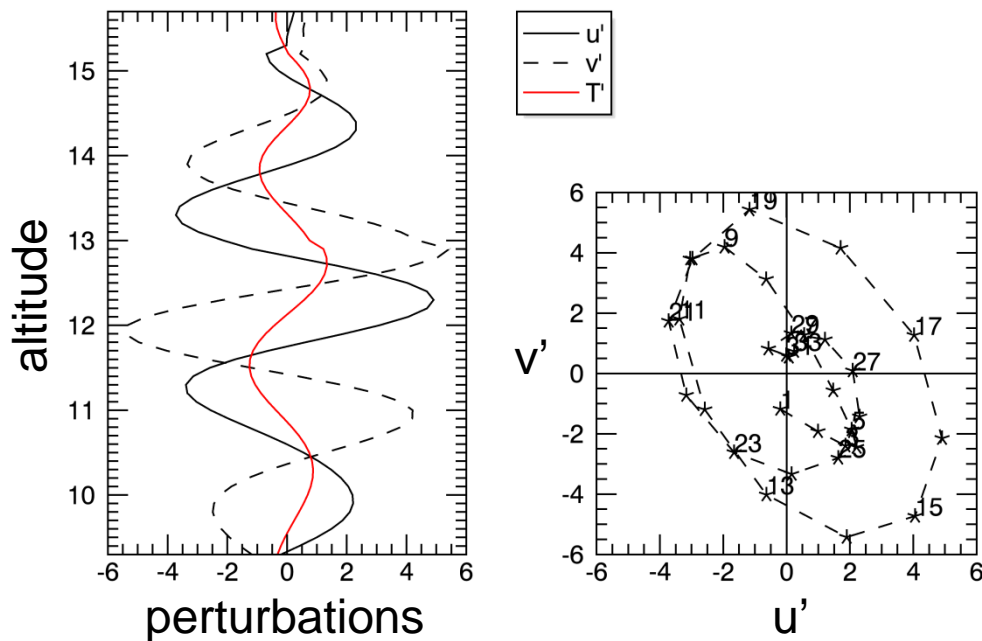


# Inertia-GWs

## horizontal velocity perturbations

- treat sounding as vertical profile
- **derive wave properties** (e.g., Allen and Vincent 1995, Vincent et al. 1997, Murphy et al 2014)

2014-06-13T23:40:00Z WP#3  $\lambda_z = 2.1$  km



basic idea based on relationship of  **$u'$**  and  **$v'$**  (e.g. hodograph)

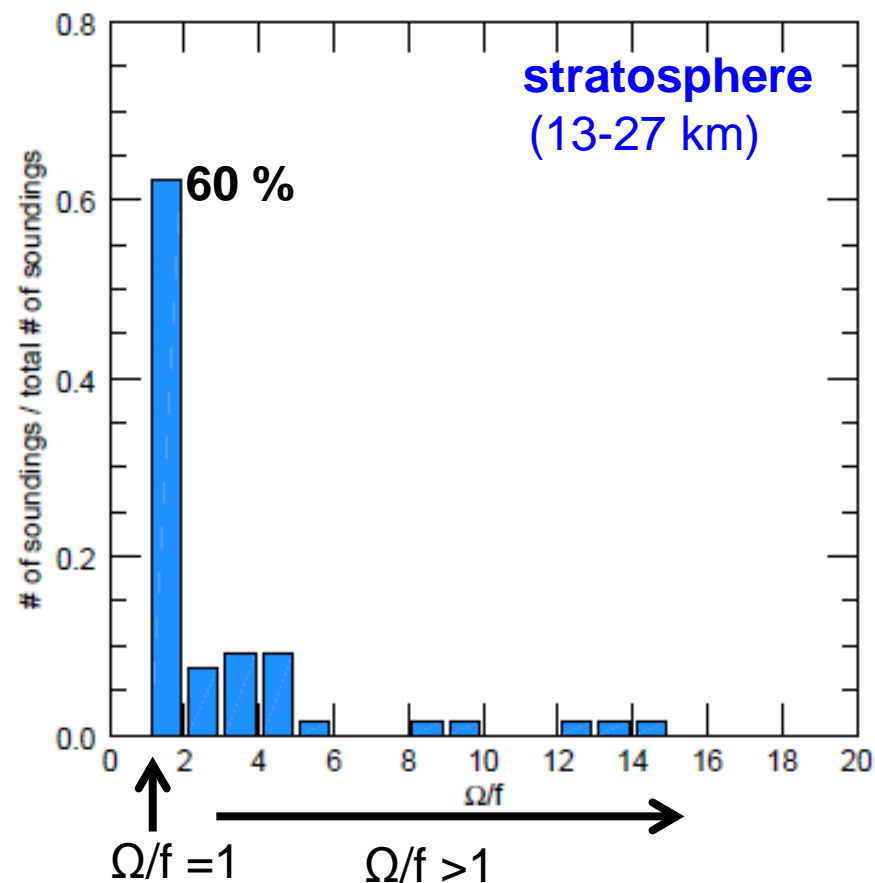
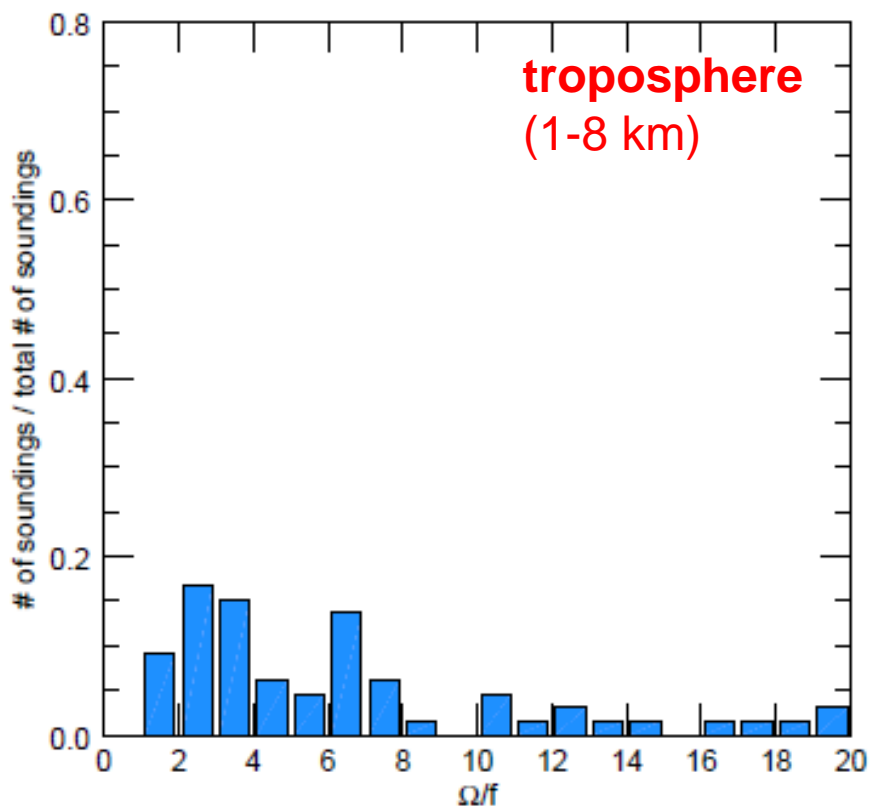
- sense of rotation gives upward/downward propagation
- orientation of major axis gives propagation direction
- axial ratio gives frequency

- contained in methods of **rotary spectra, stokes analysis**



# Inertia-GWs

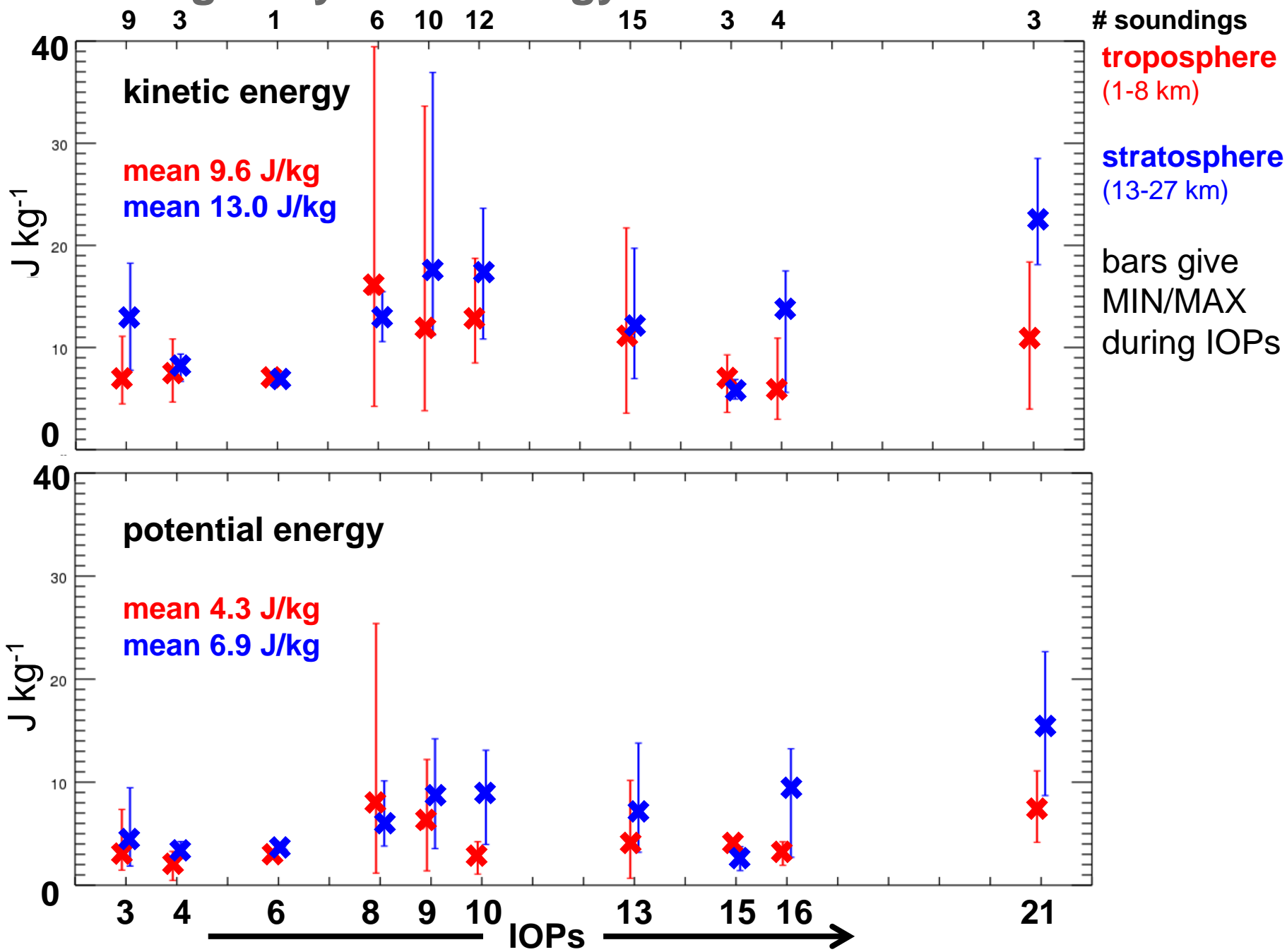
## intrinsic frequency ( $\Omega/f$ ) from Stokes analysis



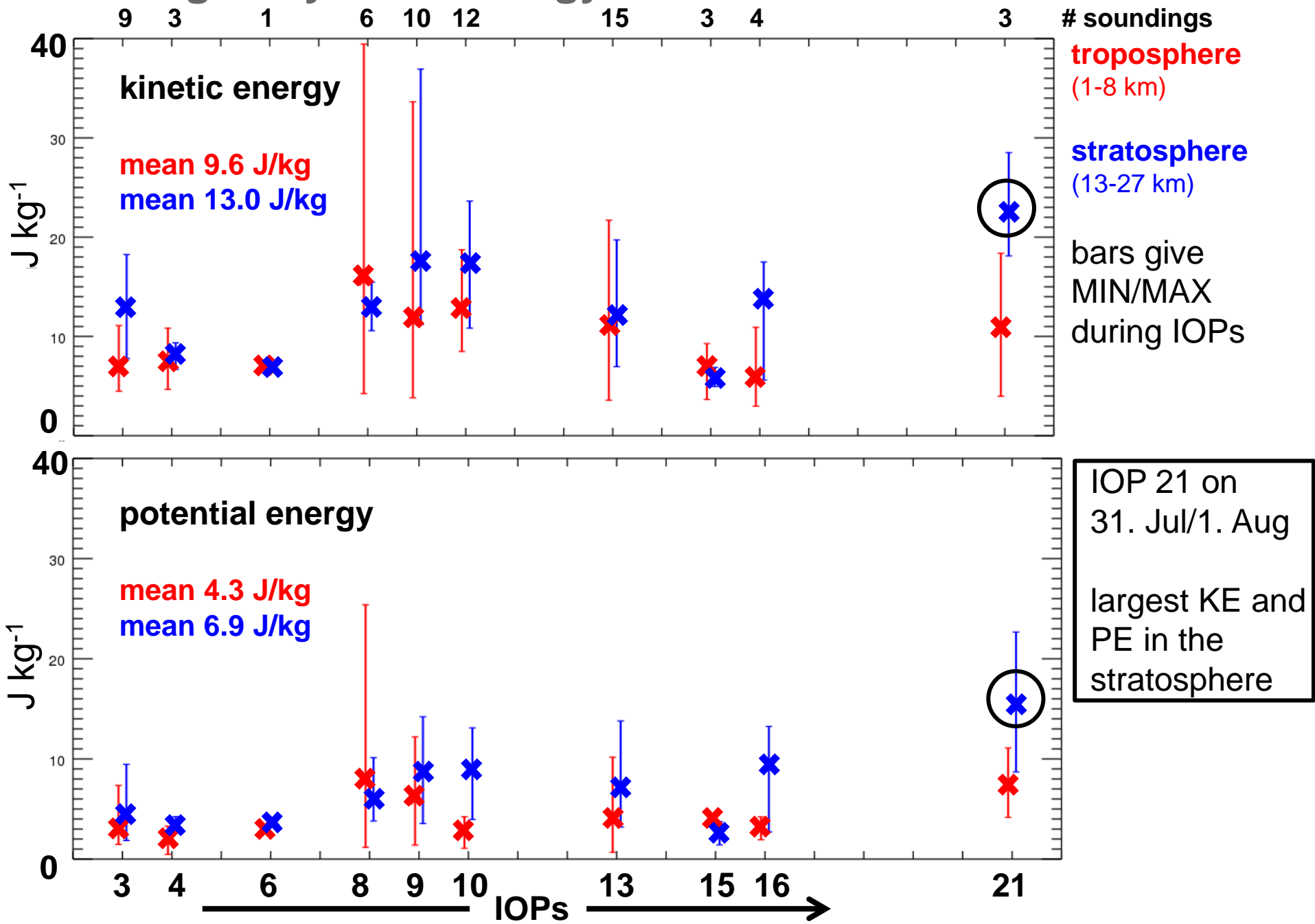
- data ( $u'$ ,  $v'$ ) going into Stokes analysis **mainly contain inertia-GWs**
- determined intrinsic frequencies **more variable in troposphere**



# mean gravity wave energy for all IOPs



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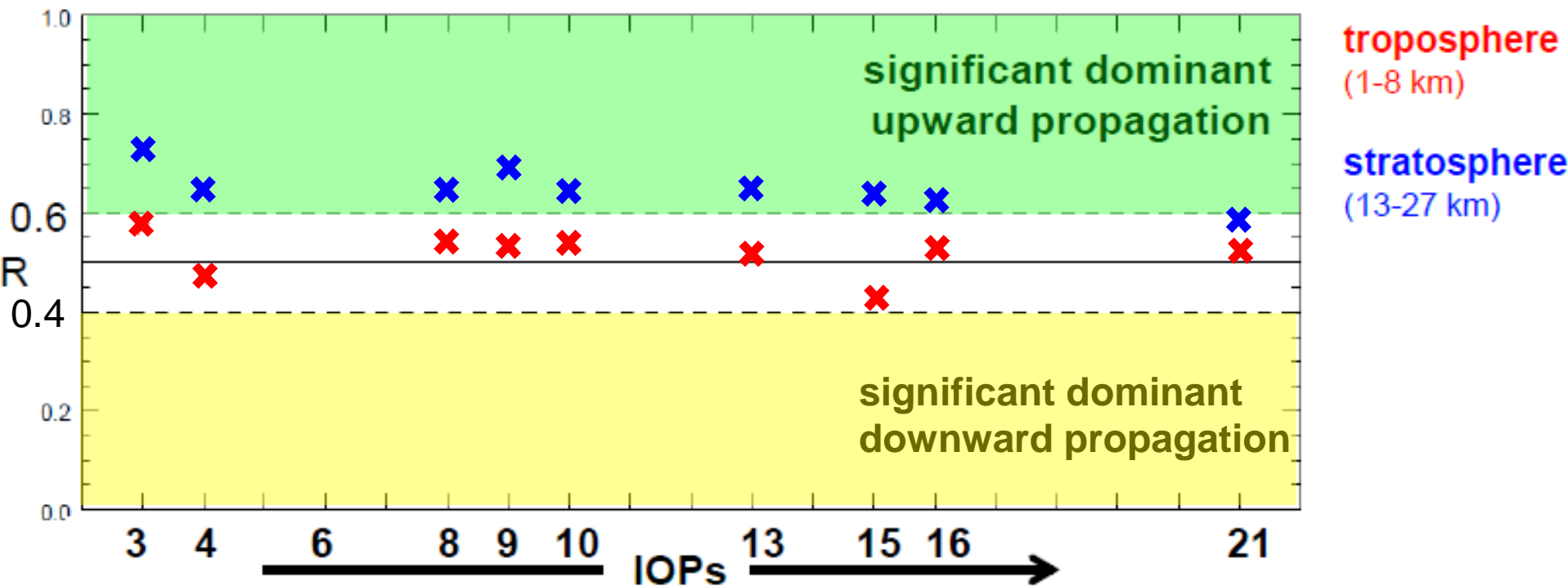
# Inertia-GWs

## vertical propagation direction

ratio (R) of upward and downward propagation from rotary spectra ( $u'+iv'$ )

$$R = \frac{\overline{(\text{power} \times m)_{\text{up}}}}{\overline{(\text{power} \times m)_{\text{up}} + (\text{power} \times m)_{\text{down}}}}$$

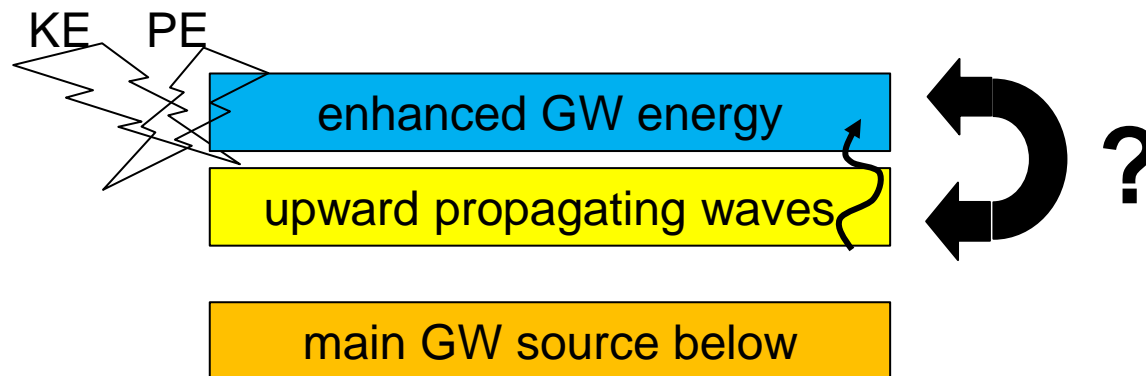
R > 0.6 significant upward energy propagation,  
R < 0.4 significant downward energy propagation



- dominant upward propagation in the **stratosphere** (source lies below → troposphere, tropopause)
- no dominant propagation direction found for troposphere

# Inertia-GWs

## Correlation between vertical propagation direction and GW energy



– **low correlation** between **enhanced KE** and **PE** and **upward propagation** (0.6 or smaller, *in agreement with Guest et al. 2000*)

→ even if **KE** and **PE** are high, **R** would be **close to 0.5...**

... if **upward- and downward-propagating waves** are present

... if **wave frequencies are large** compared to **inertial frequency  $f$**  (medium to high frequency waves)



# Inertia-GWs: summary of properties from soundings

- **GW energy** is variable for different events (values distributed around **10 J/kg**)
- **GW energy** varies during IOPs
- **vertical propagation** direction in troposphere not clear
  - upward and downward propagating waves and/or higher freq. waves
- not necessarily only upward propagating waves if **KE** and **PE** are enhanced
- **dominant upward** propagation in the **stratosphere**
  - source in troposphere/tropopause

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(not shown)

- dominant **vertical wavelength 2-4 km**, **horizontal wavelength 50-800 km**
- ground based **horizontal phase propagation** mainly **eastward** with mean **10 m/s**
  - source west of Lauder



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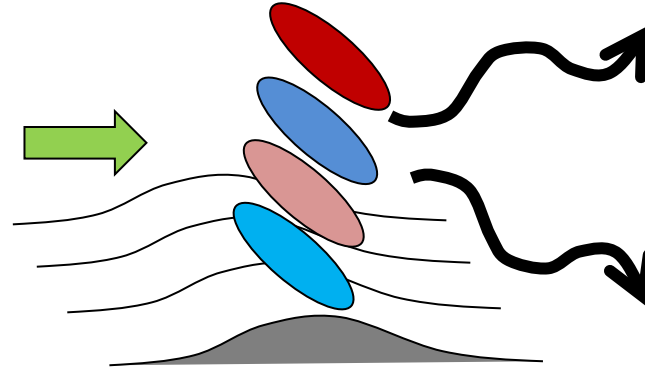
**Possible sources?**



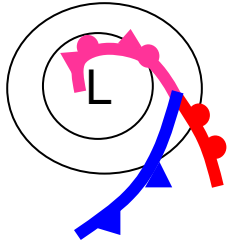


# Known major sources for Inertia-GWs (e.g., Spiga et al. 2008)

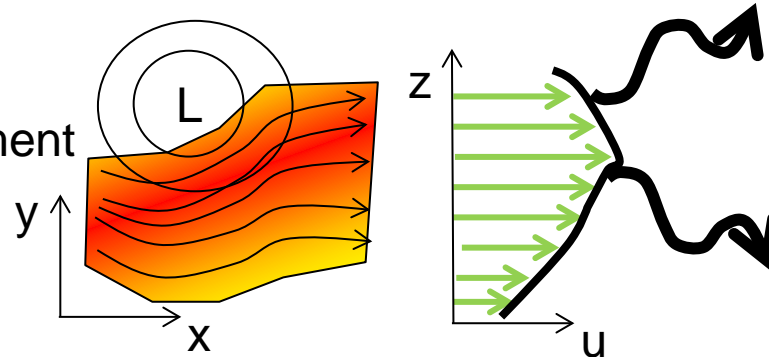
- **large amplitude mountain waves: adjustment of large-scale flow due to high amplitude and eventually breaking of the main mountain wave**



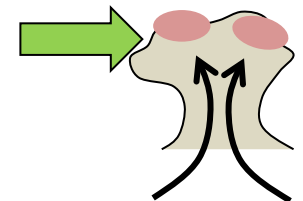
- **fronts**



- **jets: spontaneous adjustment**



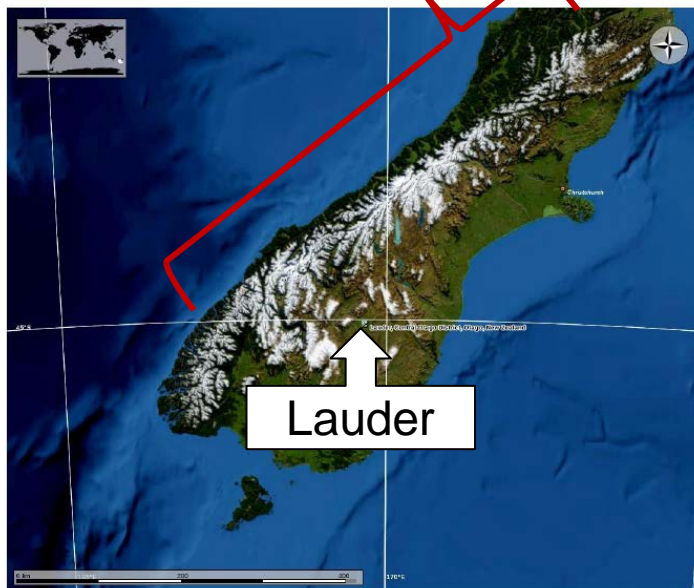
- **deep convection: bulk release of latent heat, “obstacle effect”, mechanical oscillation**



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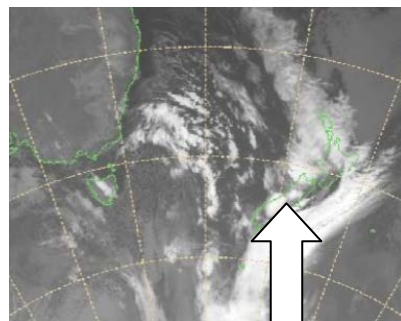


**mountains**  
west of Lauder



Lauder

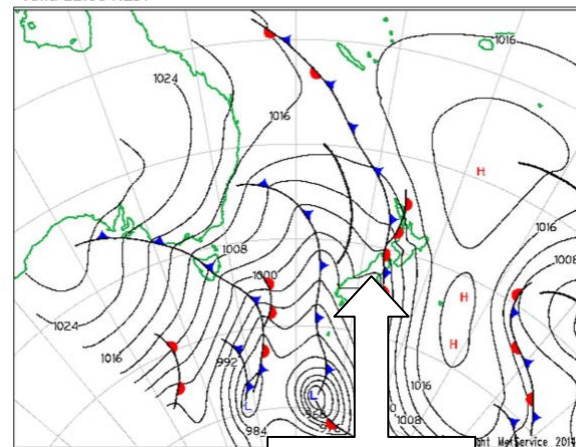
**convection**



Lauder

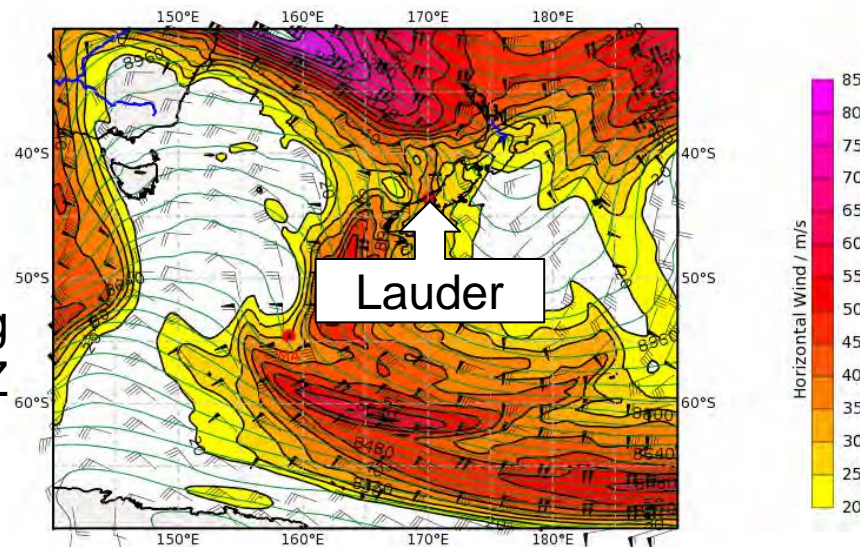
NZ Met Service  
Surface Analysis  
Valid 12:00 NZST

**fronts**



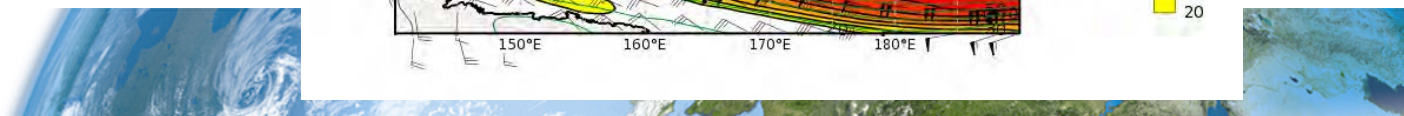
Lauder

**wind @ 300 hPa**



Horizontal Wind / m/s

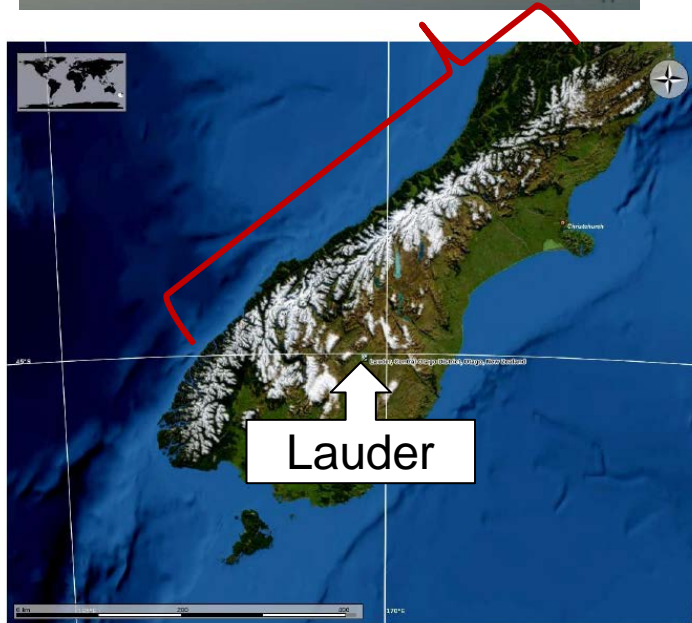
**Jet maximum/Jet-exit region moving over NZ**



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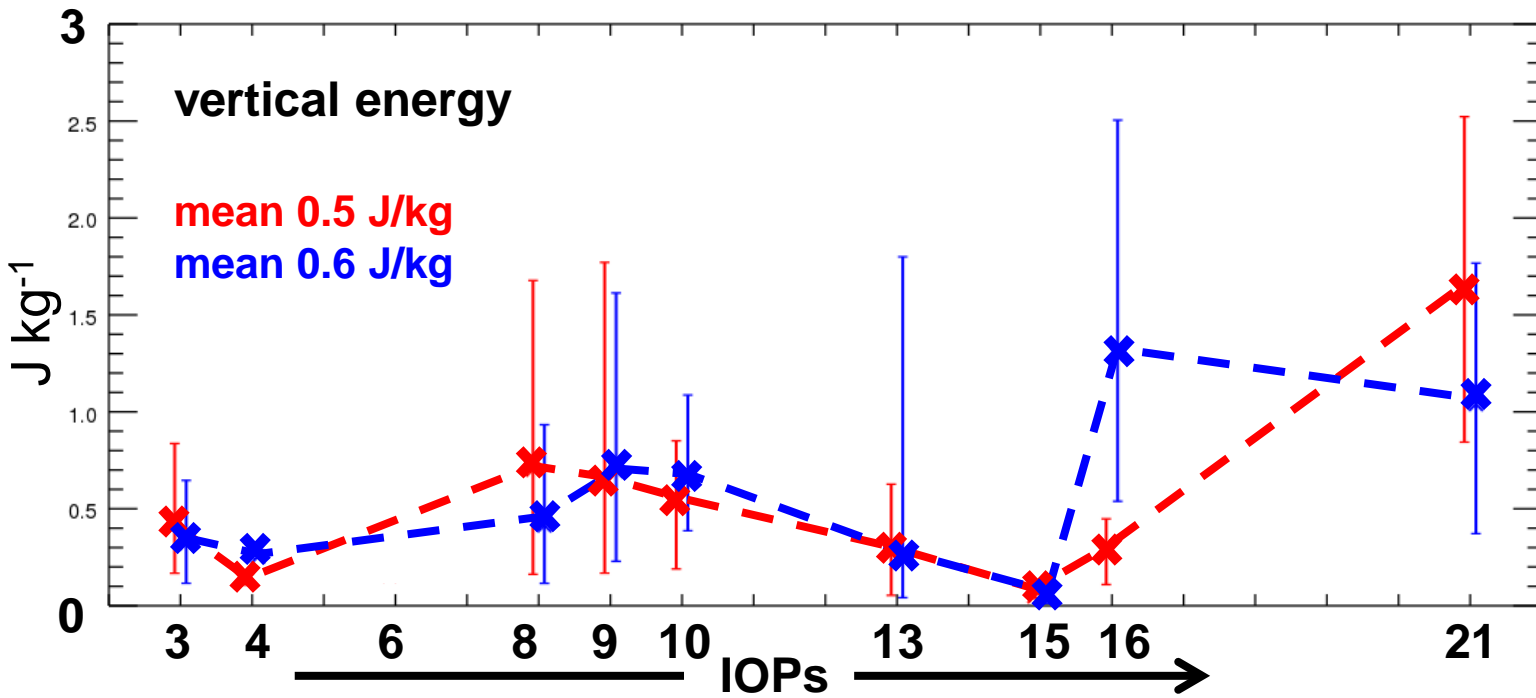
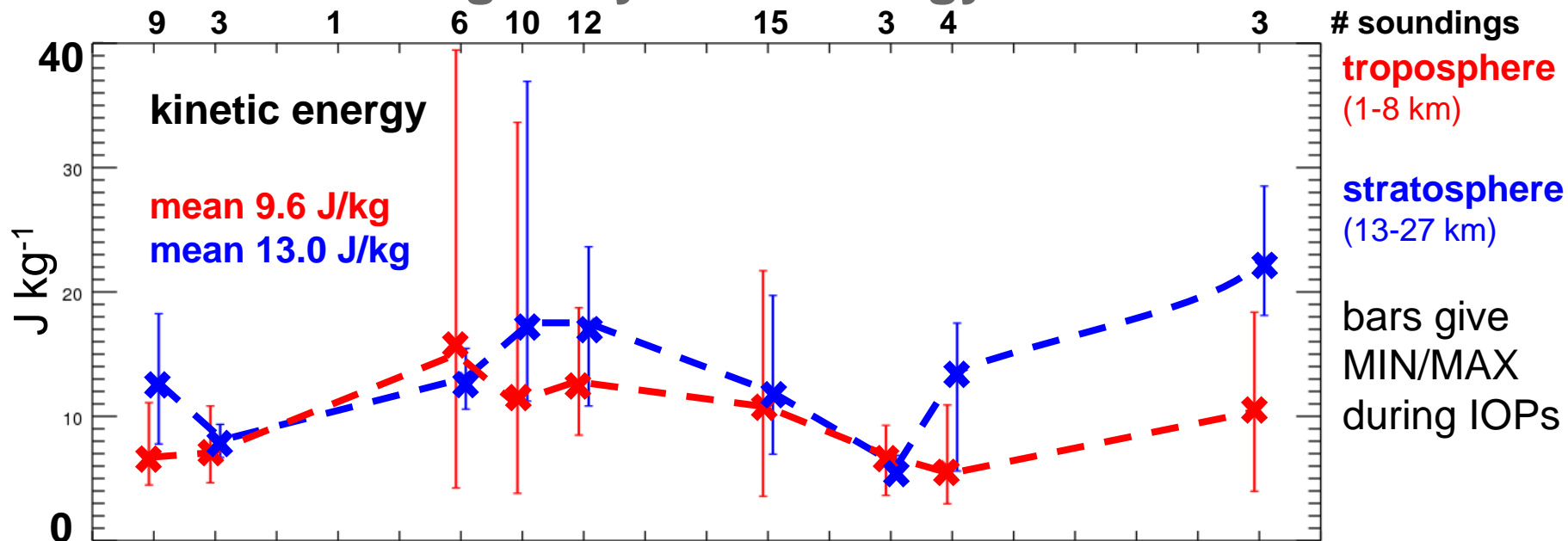
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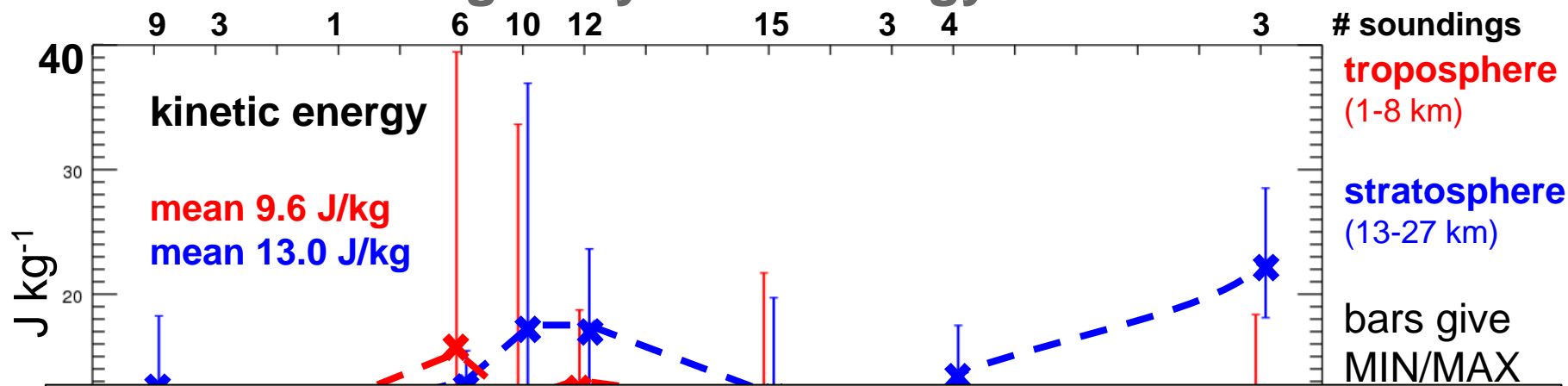
- **radiosondes** were released when **mountain waves** were expected  
→ cross mountain flow
- **vertical energy** based on **balloon ascent rate** to quantify **mountain wave activity**



# Results: mean gravity wave energy for all IOPs



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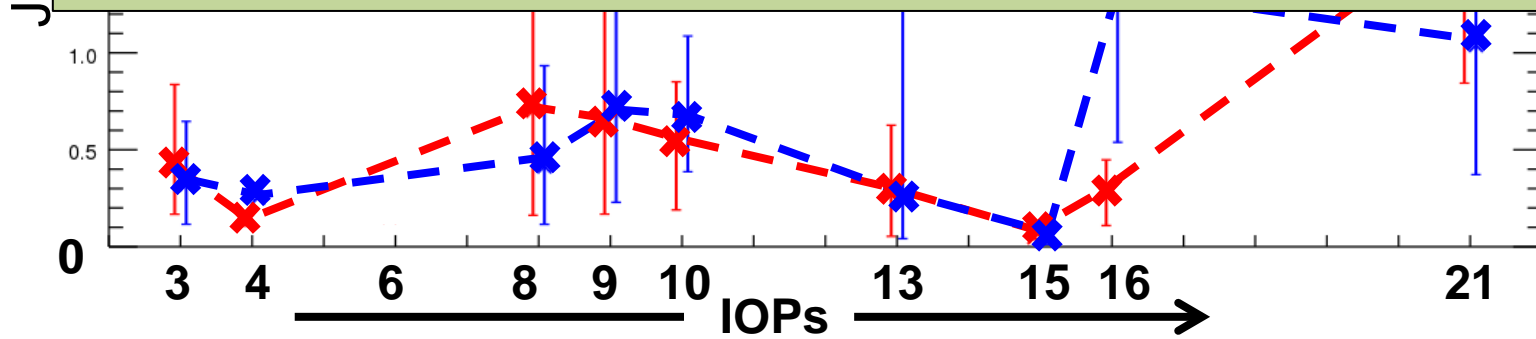
## correlation coefficient of IOP mean values

- KE stratosphere and VE troposphere: 0.87
- KE stratosphere and VE stratosphere: 0.72

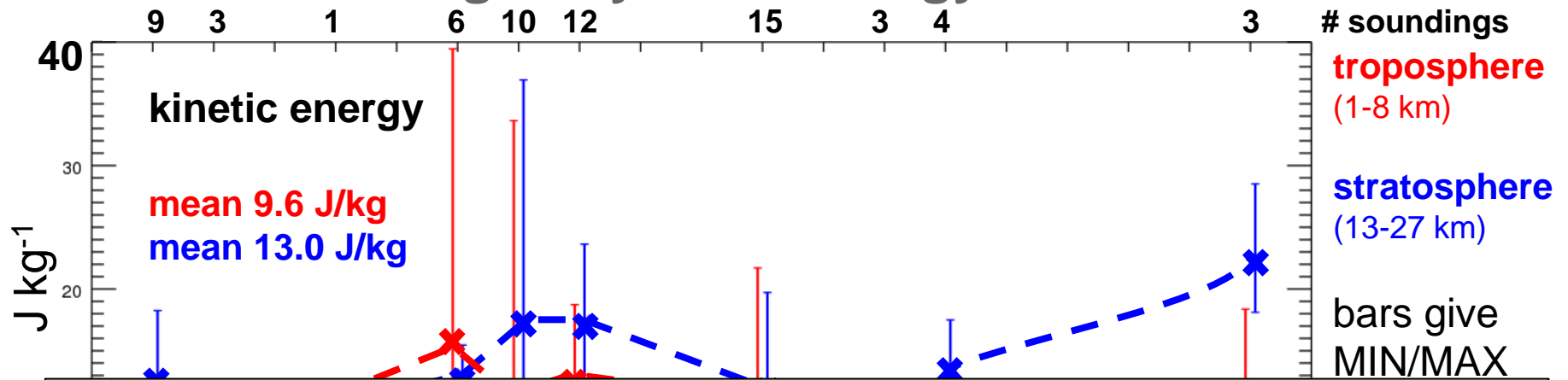
stratospheric inertia-GWs seem to be connected to mountain waves

**BUT** correlation between KE and VE varies during IOPs

→ possible contribution of other sources of inertia-GWs (more detailed analysis the different events necessary)



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# Thank you for your Attention!



*Attendance at the meeting was supported by WMO travel award*