

# Gravity Wave and Kelvin Wave Activity in the Tropical Lower Stratosphere

Thomas Birner

with contributions by: Anne (Sasha) Glanville,  
Jeremiah Sjoberg, Richard Johnson

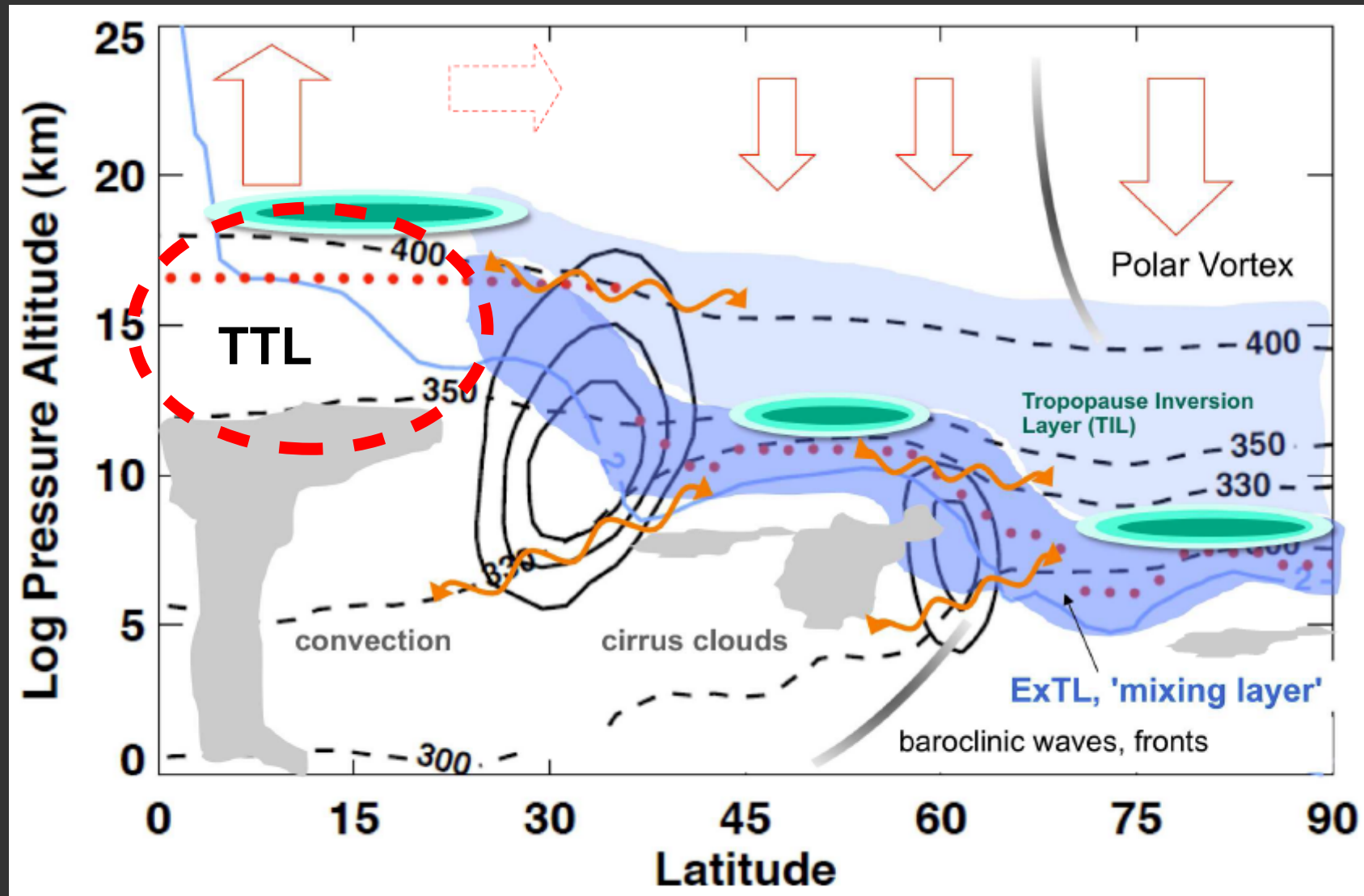
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*2016 SPARC Gravity Wave Symposium*

## Multiscale Dynamics in the TTL

- Planetary-scale circulations (e.g. adiabatic cooling by Brewer-Dobson upwelling)
- Convectively coupled equatorial waves (broad spectrum, incl. **Kelvin waves**)
- Convection (incl. large-scale indirect temperature response)
- Horizontal mixing (due to Rossby wave breaking) with extratropical lowermost stratosphere
- Vertical mixing, e.g. due to overshooting convection, **breaking gravity waves**

# Upper Troposphere / Lower Stratosphere



# Vertical Transport just above the Tropical Tropopause: Residual Circulation Upwelling vs. (vertical) Mixing

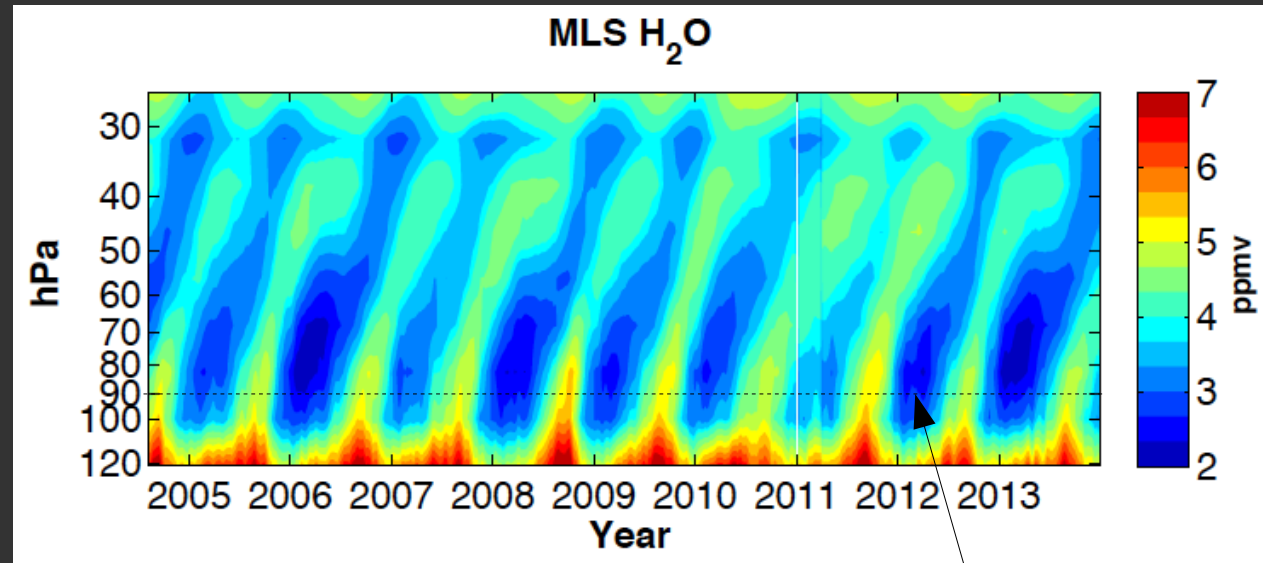
*Glanville & Birner 2016, Atmos. Chem. Phys. Discuss.*

Mote et al., 1996:

## An atmospheric tape recorder: The imprint of tropical tropopause temperatures on stratospheric water vapor

In other words, air is “marked,” on emergence above the highest cloud tops, like a signal recorded on an upward moving magnetic tape.

### Tape Recorder Signal in H<sub>2</sub>O



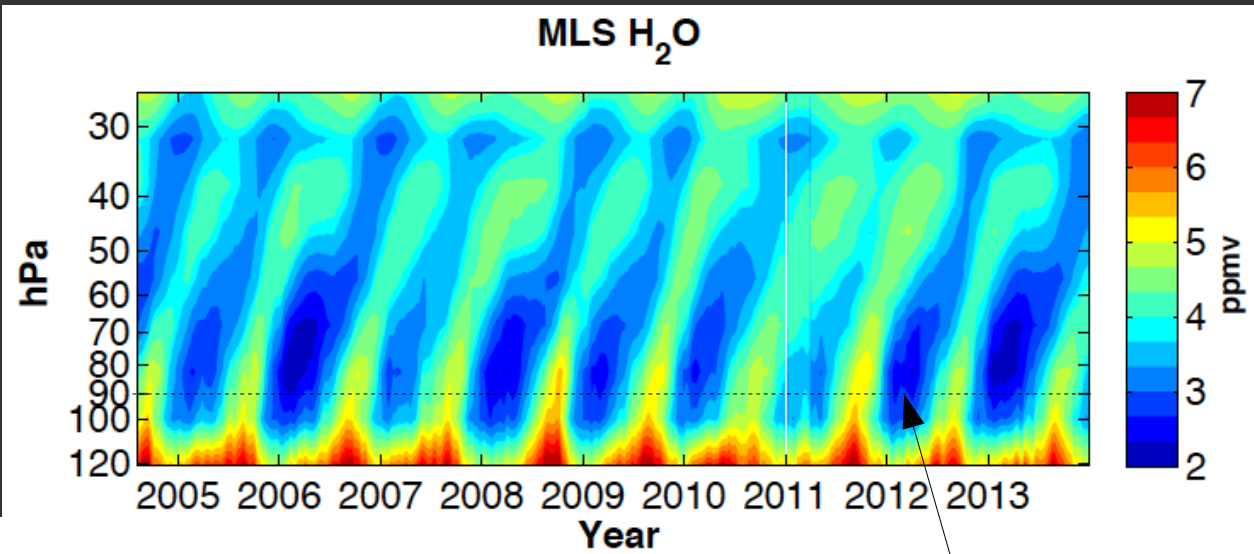
cold point  
tropopause

Mote et al., 1996:

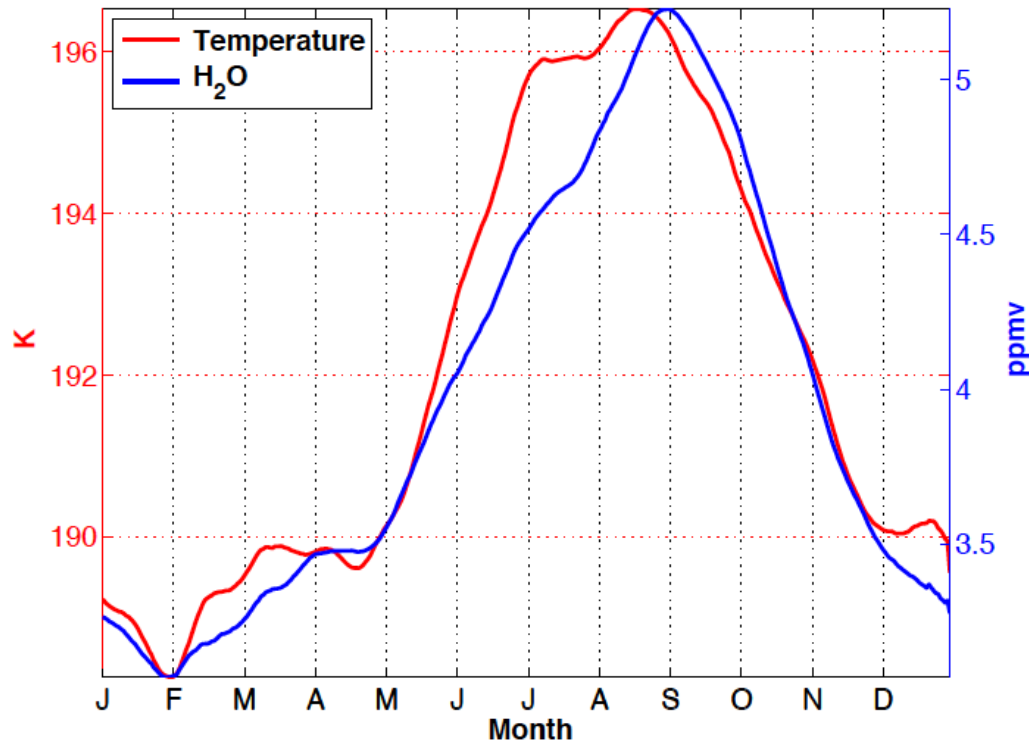
# An atmospheric tape recorder: The imprint of tropical tropopause temperatures on stratospheric water vapor

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## Tape Recorder Signal in H<sub>2</sub>O



Observed Cold Point Climatology



cold point tropopause

*Is the tape recorder signal caused by vertical advection within the stratospheric residual circulation?*

**Synthetic tape recorder** by solving simple 1-d transport Eq., similar to Mote et al. (1998), but with seasonally varying transport coefficients

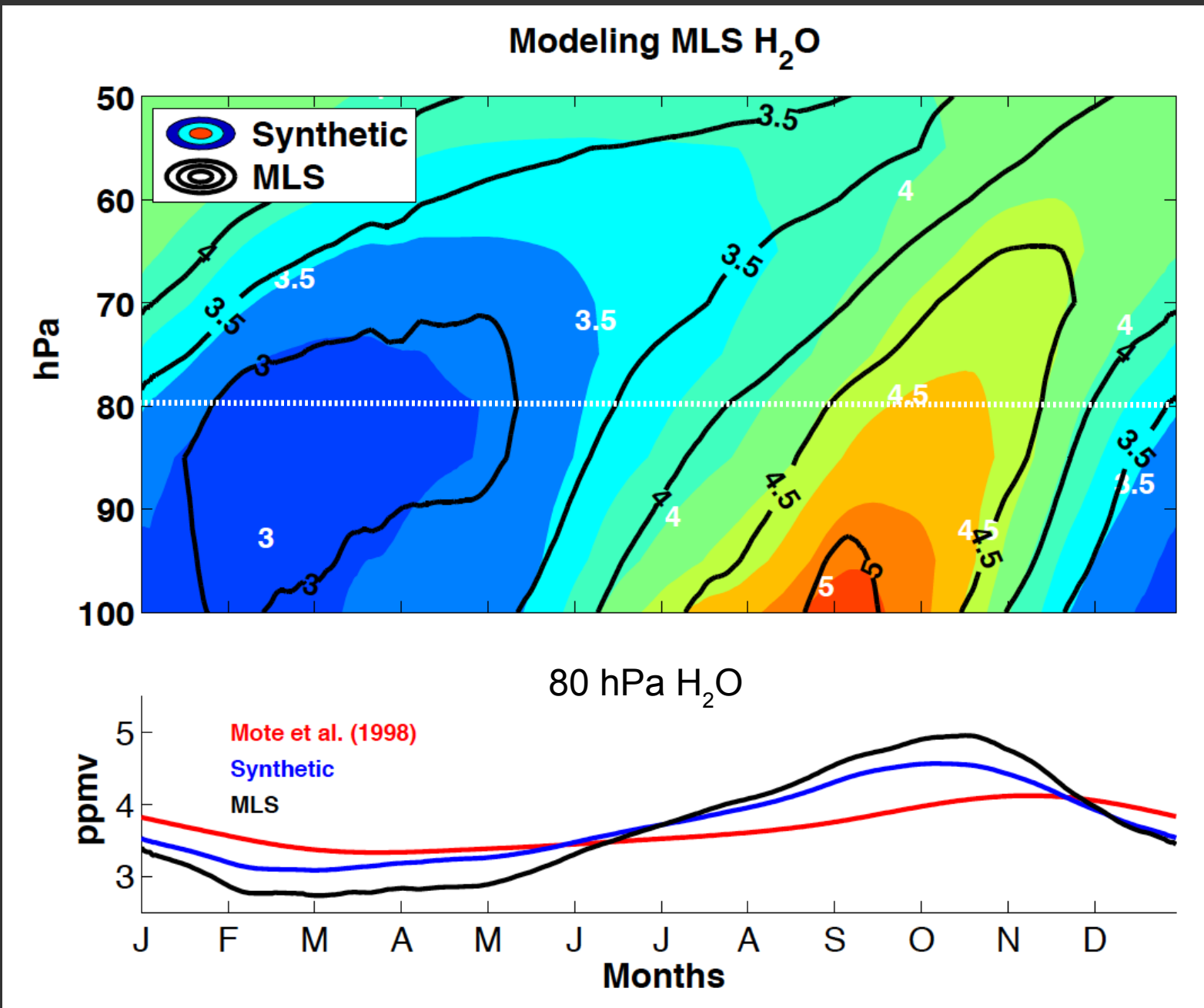
$$\partial_t \bar{\chi} = -\bar{\omega}^* \partial_p \bar{\chi} + \partial_p (K_p \partial_p \bar{\chi}) - \alpha_p (\bar{\chi} - \bar{\chi}_{ML}) + S$$

vertical  
advection

vertical  
mixing/diffusion

horizontal  
mixing/dilution

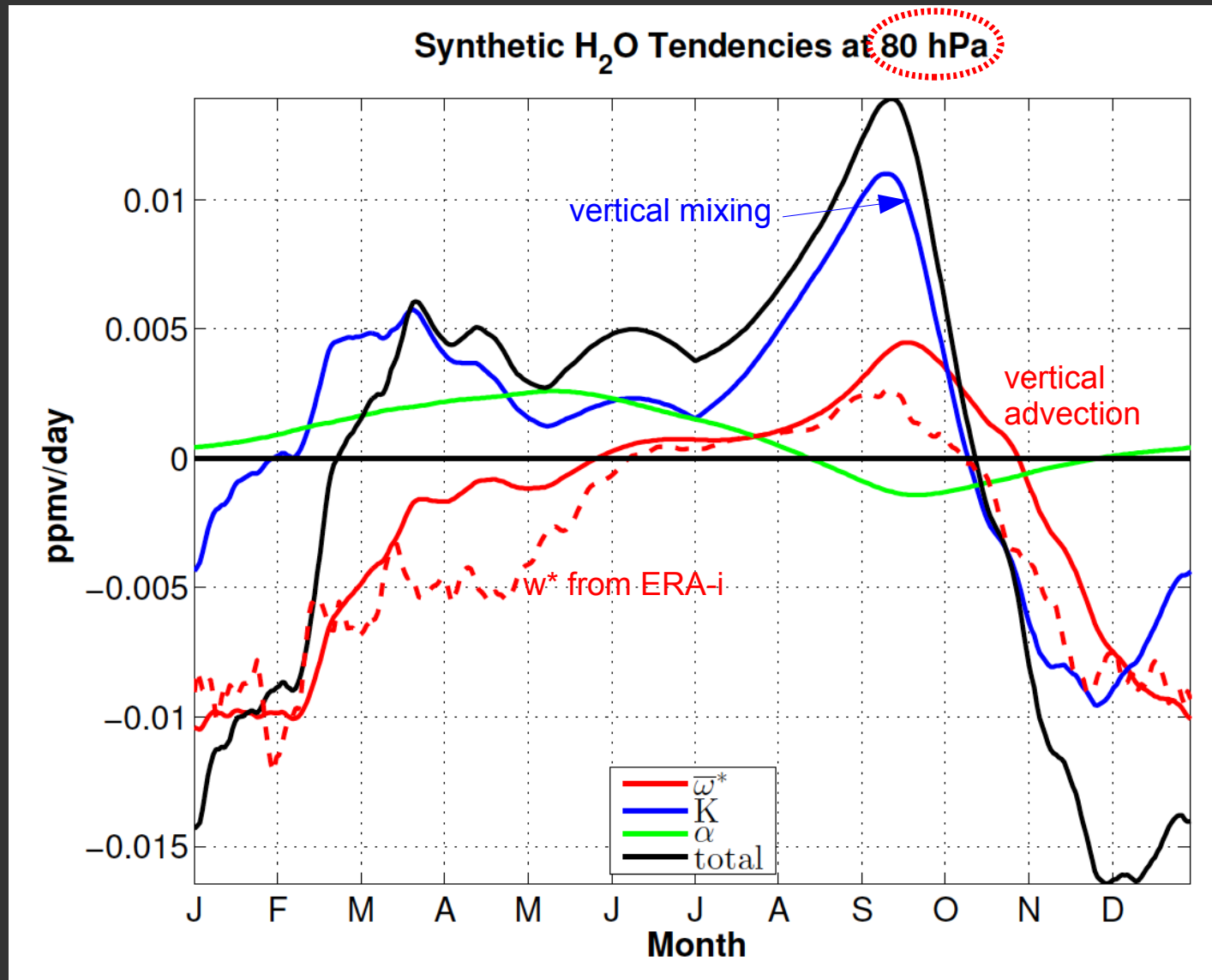
# Modeled vs. Observed Tape Recorder Signal





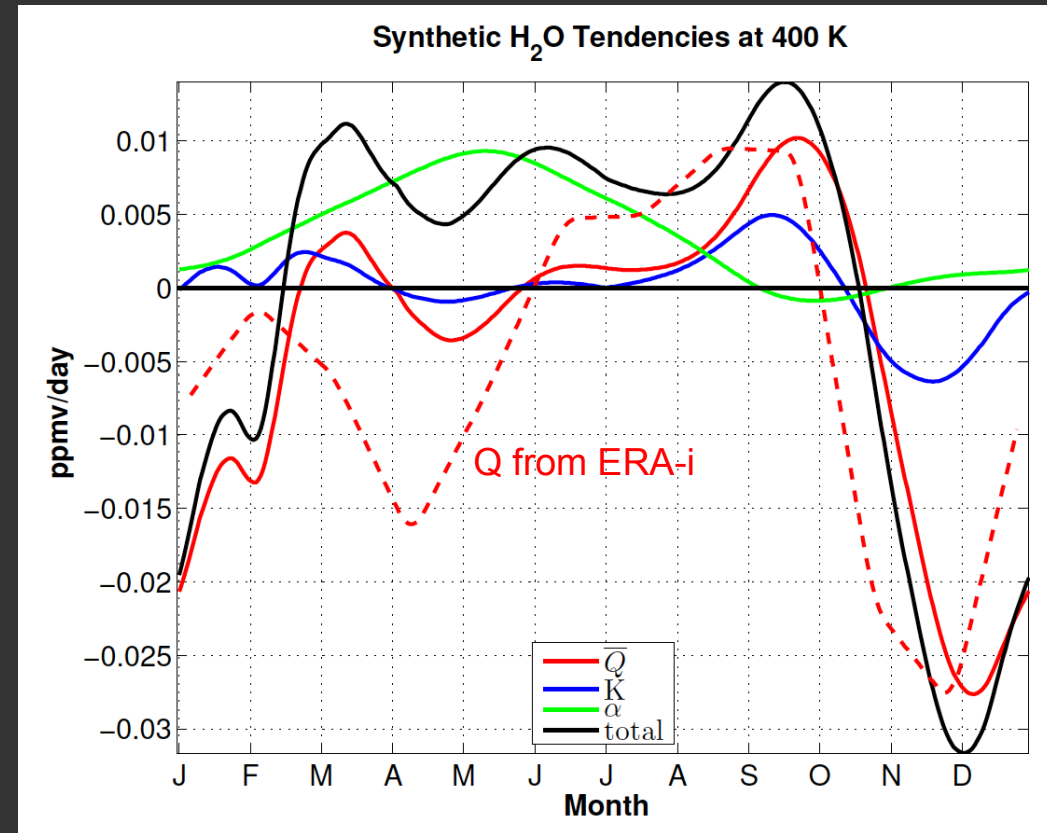
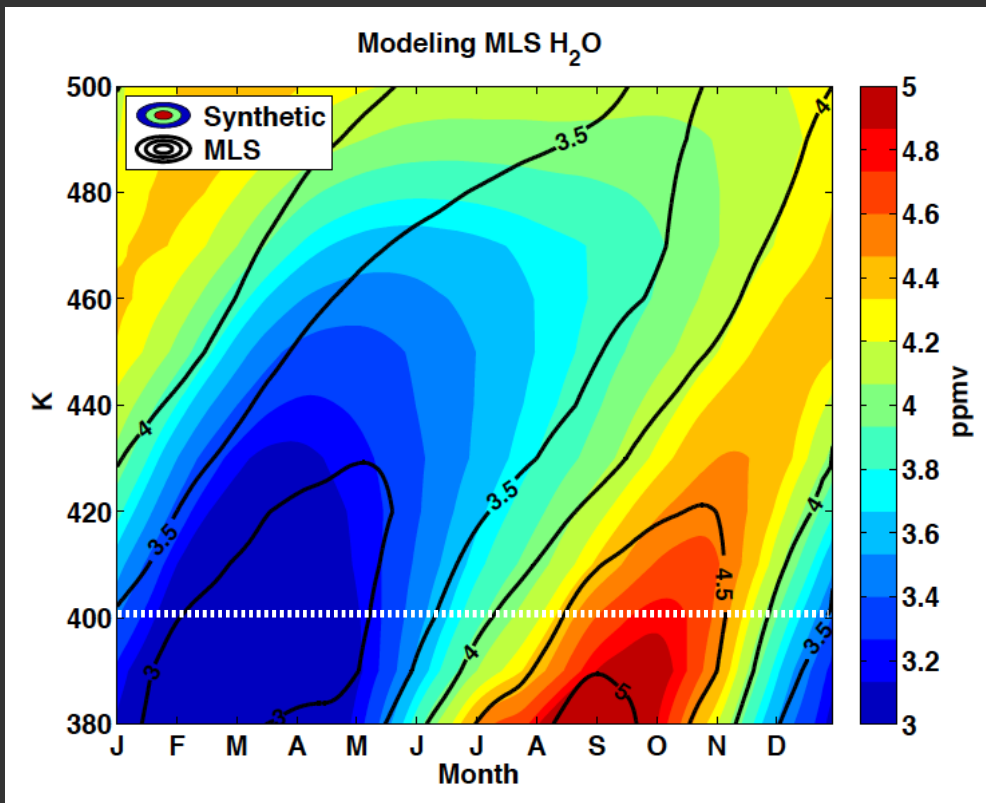
# Vertical mixing as important as vertical advection!

quadrupled(!) vertical mixing compared to Mote et al (but same vertical advection & horizontal mixing)



(for ERAi, optimal solution requires 10 times vertical mixing and 5 times horizontal mixing)

Synthetic tape recorder from 1-d transport model in **isentropic coordinates** → **vertical mixing mostly negligible** (but horizontal mixing important during boreal spring / summer)



→ vertical mixing contribution in p-coordinates largely due to adiabatic processes (e.g. gravity wave breaking)

Effective vertical transport velocity for tracer in p-coordinates:

$$\partial_t \bar{\chi} + \omega_{\text{eff}} \partial_p \bar{\chi} = 0$$

with

$$\omega_{\text{eff}} \approx \bar{\omega}^* + \partial_p \overline{\omega' \chi'} (\partial_p \bar{\chi})^{-1}$$

Effective vertical transport velocity for tracer in p-coordinates:

$$\partial_t \bar{\chi} + \omega_{\text{eff}} \partial_p \bar{\chi} = 0 \quad \text{with} \quad \omega_{\text{eff}} \approx \bar{\omega}^* + \partial_p \overline{\omega' \chi'} (\partial_p \bar{\chi})^{-1}$$

Effective transport velocity for tracer in isentropic coordinates:

$$\partial_t \bar{\chi}^* + Q_{\text{eff}} \partial_{\theta} \bar{\chi}^* = 0$$

Effective vertical transport velocity for tracer in p-coordinates:

$$\partial_t \bar{\chi} + \omega_{\text{eff}} \partial_p \bar{\chi} = 0$$

with

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Effective transport velocity for tracer in isentropic coordinates:

$$\partial_t \bar{\chi}^* + Q_{\text{eff}} \partial_{\theta} \bar{\chi}^* = 0$$

Quasi-adiabatic vertical mixing  
(e.g. due to gravity wave breaking):

$$\overline{\omega' \theta'} \approx \overline{\omega' \chi'} \frac{\partial_p \bar{\theta}}{\partial_p \bar{\chi}}$$

Effective vertical transport velocity for tracer in p-coordinates:

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Diabatic heating in steady state:

$$\bar{Q} \approx \bar{\omega}^* \partial_p \bar{\theta} + \partial_p \overline{\omega' \theta'}$$

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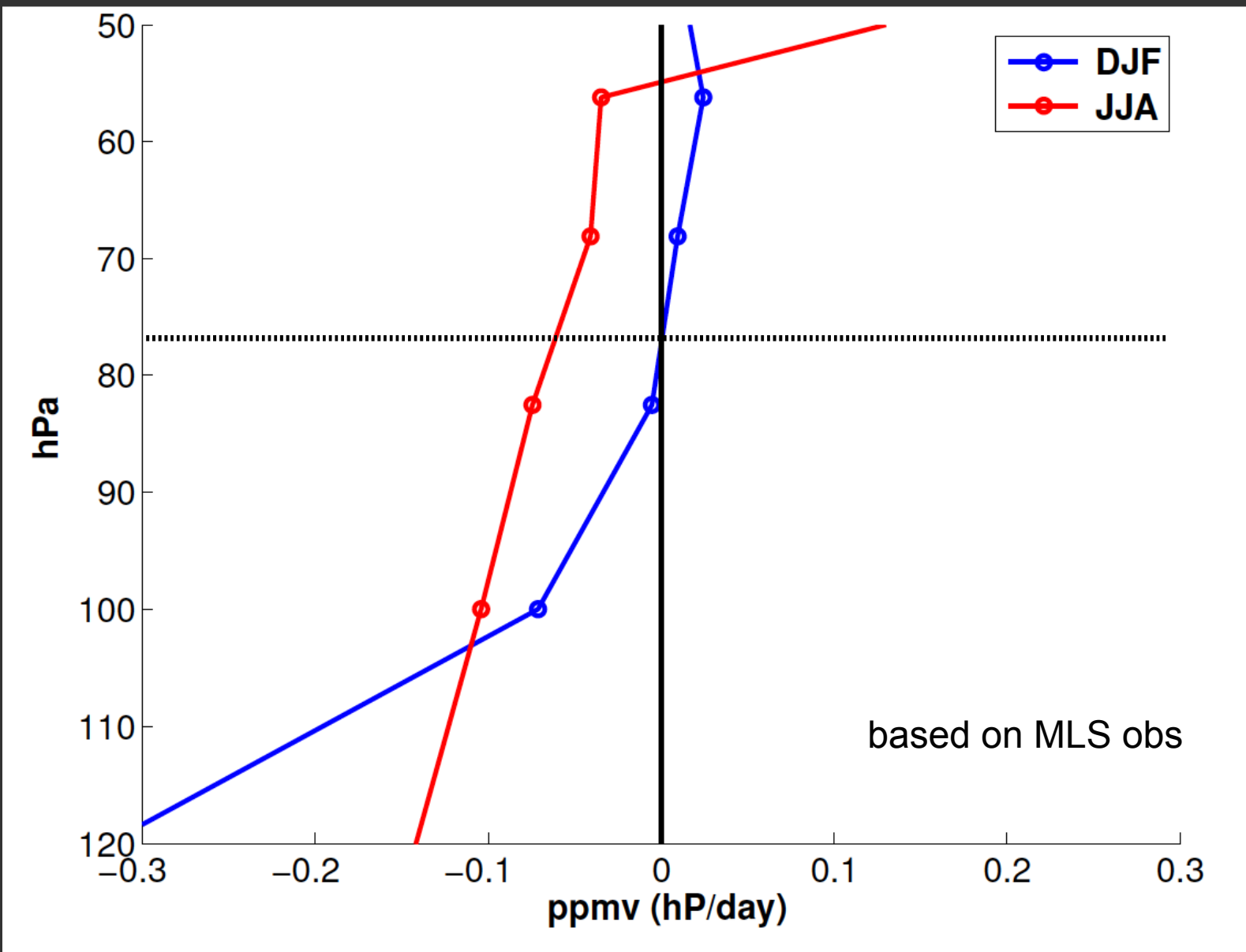
$$\bar{Q} \approx \bar{\omega}^* \partial_p \bar{\theta} + \partial_p \overline{\omega' \theta'}$$

$$\bar{Q} \approx Q_{\text{eff}}$$



$$\overline{\omega' \chi'} \approx \left[ \omega_{\text{eff}} - Q_{\text{eff}} (\partial_p \bar{\theta})^{-1} \right] \frac{(\partial_{\bar{\theta}} \bar{\chi})^2}{\partial_{\bar{\theta} \bar{\theta}} \bar{\chi}}$$

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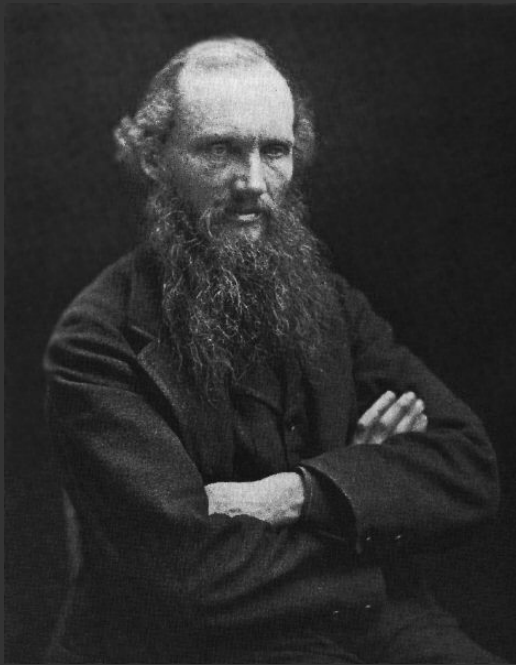


## Conclusions Part I

- Vertical mixing near tropical tropopause has been pointed at (e.g. Flannaghan & Fueglistaler, 2014), but is often neglected
- We find important contribution by quasi-adiabatic vertical mixing (due to gravity wave breaking?) to transport just above the tropical tropopause
- Insights into vertical mixing by comparing effective vertical transport in pressure vs. isentropic coordinates
- Implications for cloud formation & dehydration (e.g. in trajectory simulations as in Jensen & Pfister, 2004+)

# Tropical Lower Stratospheric Kelvin Wave Momentum Flux from Radiosoundings

*Sjoberg, Birner, Johnson, in preparation*



## Thomson (Kelvin) Waves:

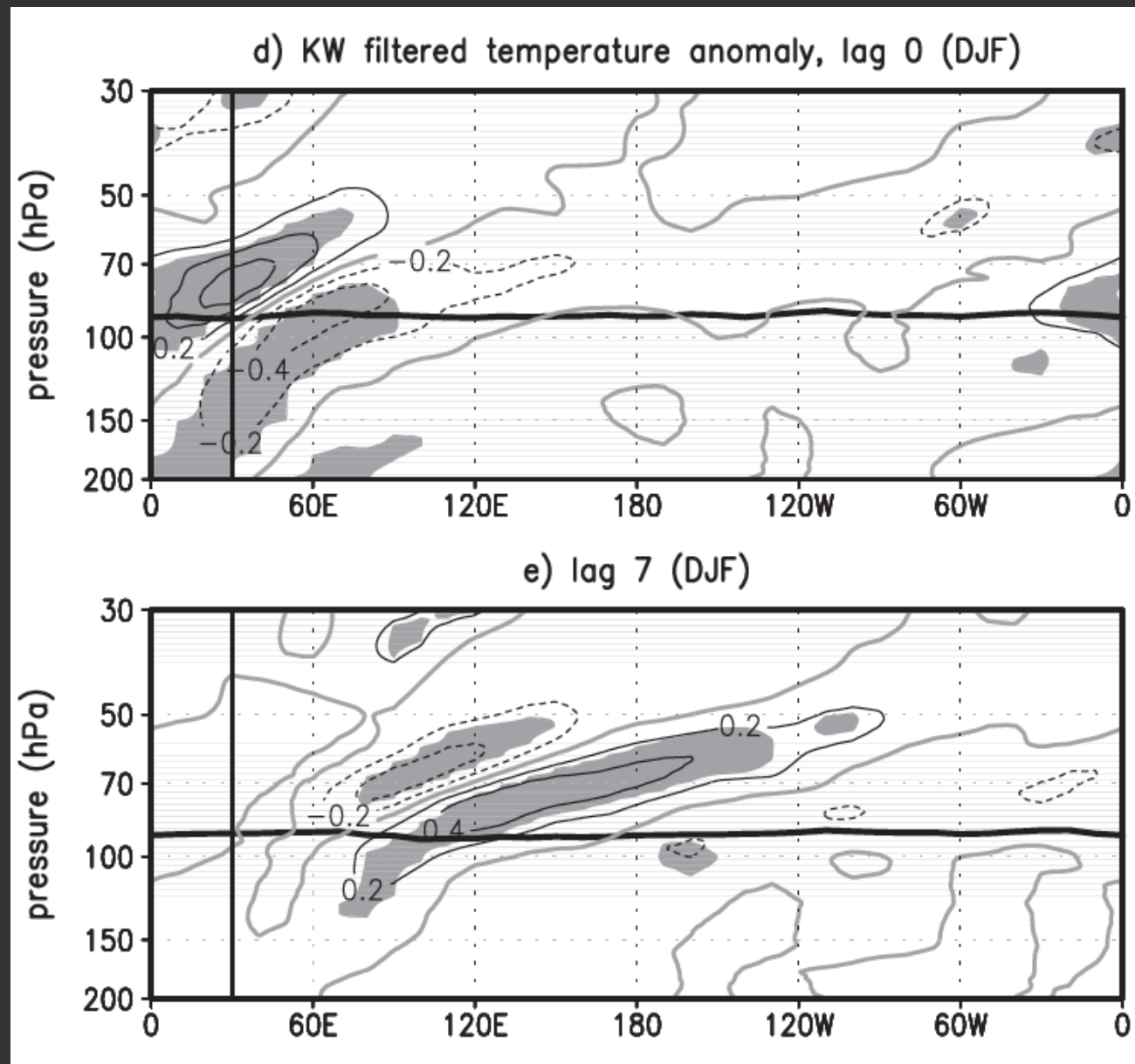
*Monday, 17th March 1879.*

Professor KELLAND, President, in the Chair.

The following Communications were read :—

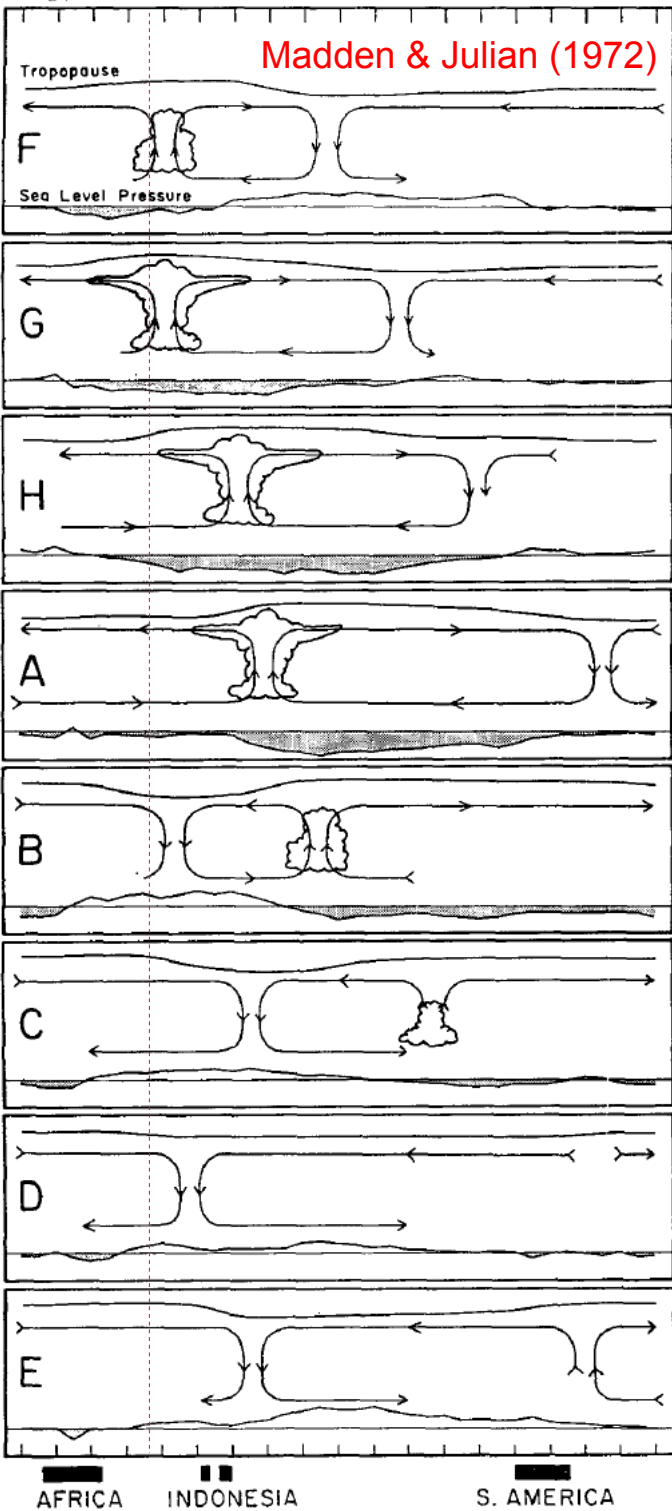
1. On Gravitational Oscillations of Rotating Water.  
By Sir William Thomson.

Kim & Son (2012): Kelvin wave composite from GPS data:

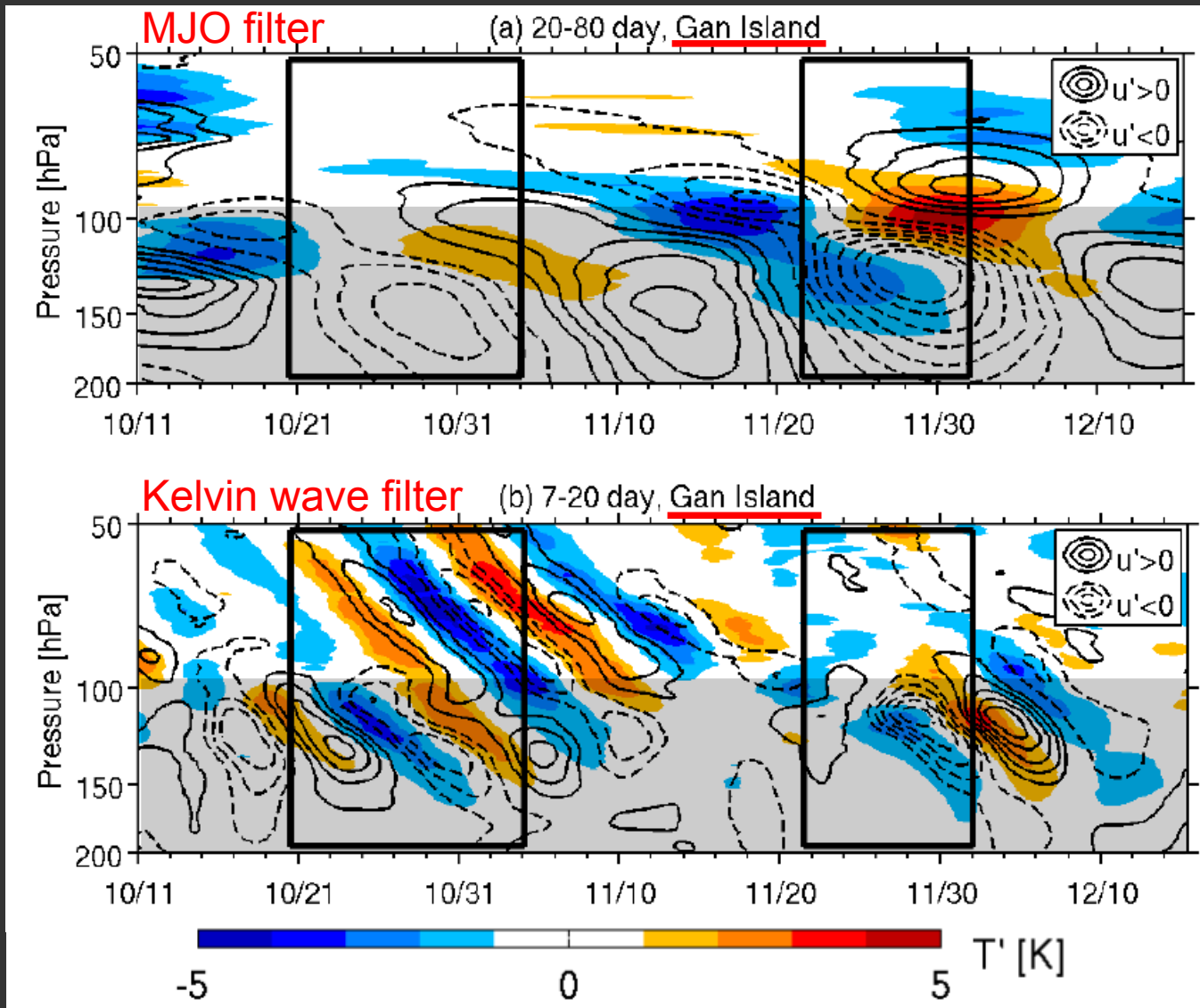


EAST LONGITUDE WEST LONGITUDE  
 20° 60° 100° 140° 180° 140° 100° 60° 20°

Madden & Julian (1972)



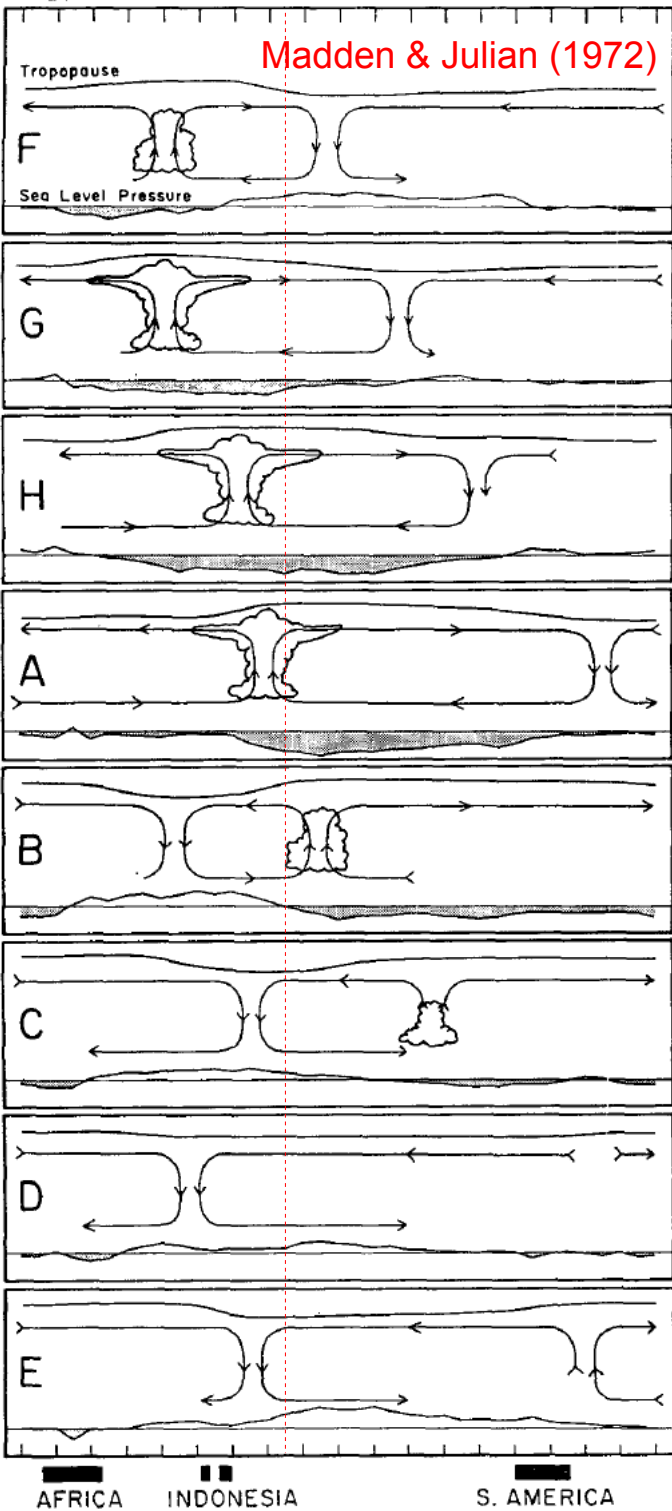
# MJO modulation of TTL dynamics (results from DYNAMO): Gan Island



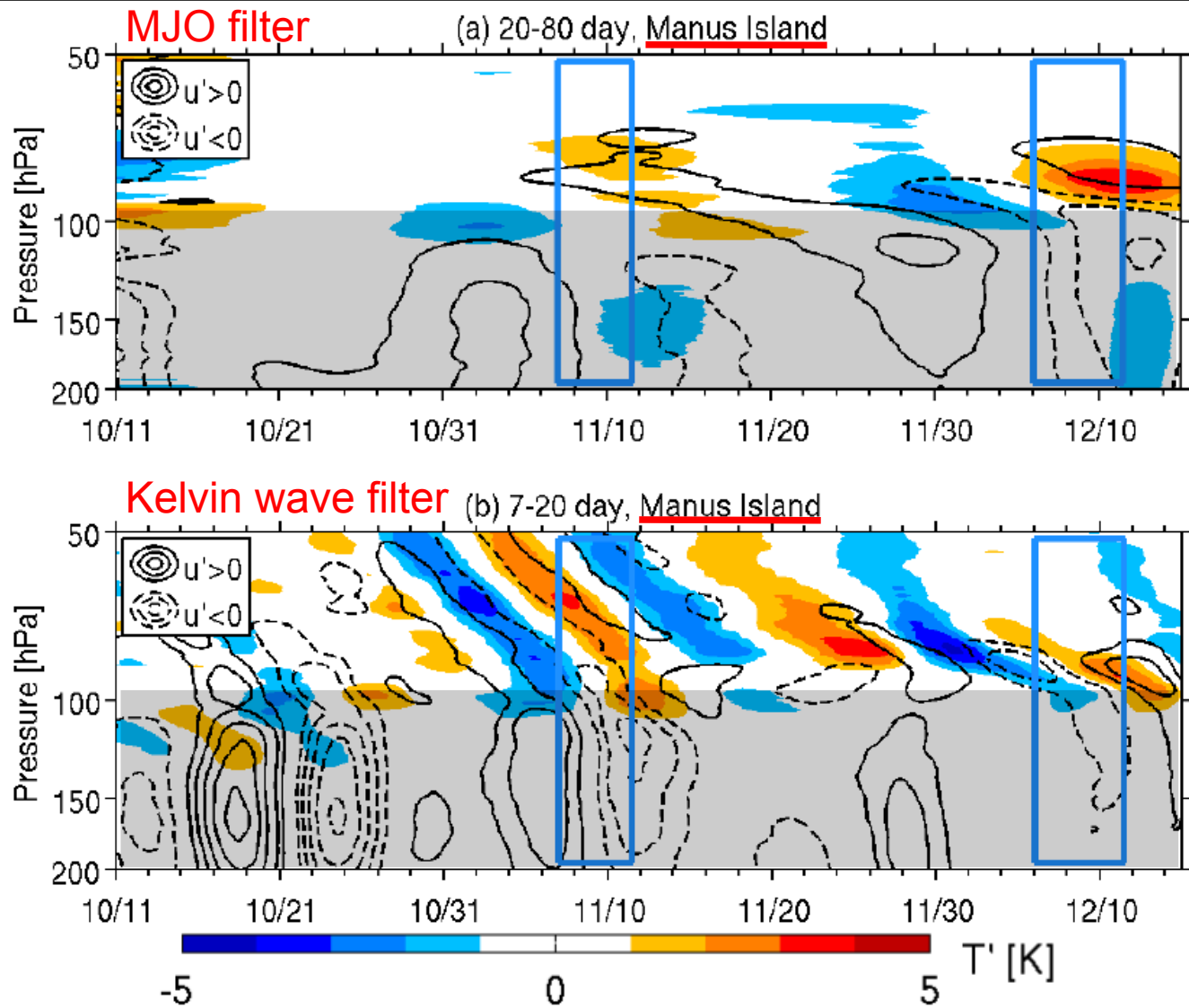
Erin Dagg (MS thesis)

EAST LONGITUDE WEST LONGITUDE  
 20° 60° 100° 140° 180° 140° 100° 60° 20°

Madden & Julian (1972)



# MJO modulation of TTL dynamics (results from DYNAMO): Manus Island



Erin Dagg (MS thesis)

Following Holton et al. 2001 (idea from Kousky & Wallace 1971 and Sato & Dunkerton 1997):

$$\overline{u'w'} = -\frac{R\omega_d}{HN^2} Q_{uT}$$

Intrinsic frequency

Vertical momentum flux

$u'$ - $T'$  Quadrature spectrum

Kelvin/gravity wave dispersion relation:

$$\omega_d = \omega - k\bar{u} = -\frac{kN}{m}$$

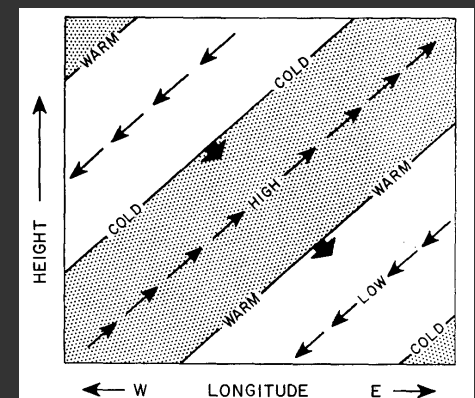


FIG. 7. Idealized cross section along a latitude circle showing phases of the zonal wind, temperature, pressure, and vertical motion oscillations associated with Kelvin waves, as deduced from theoretical considerations.

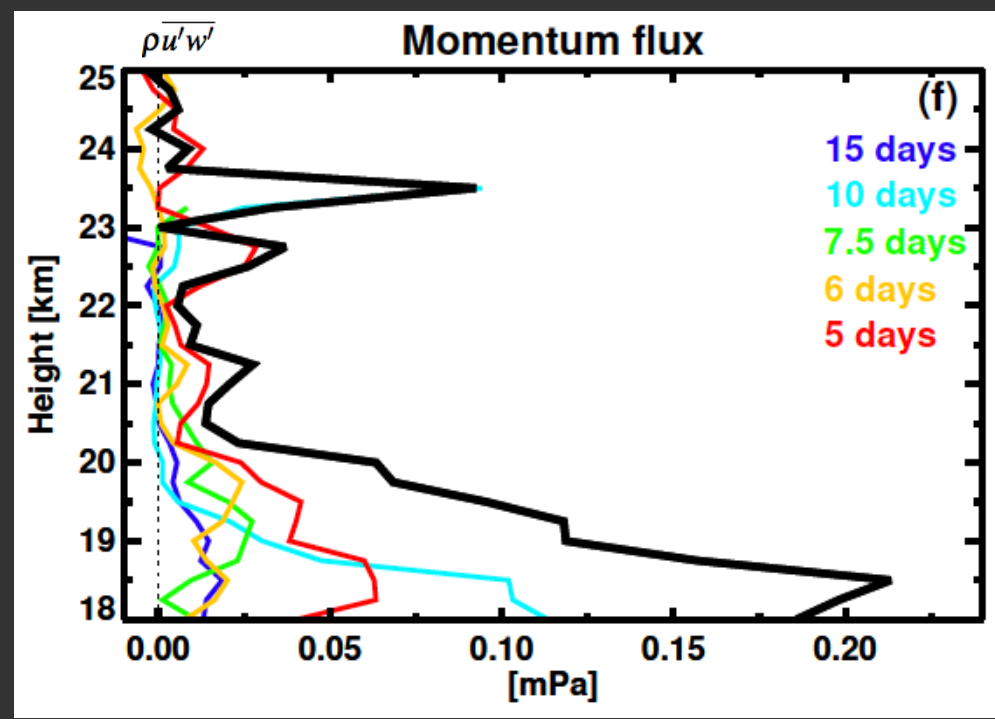
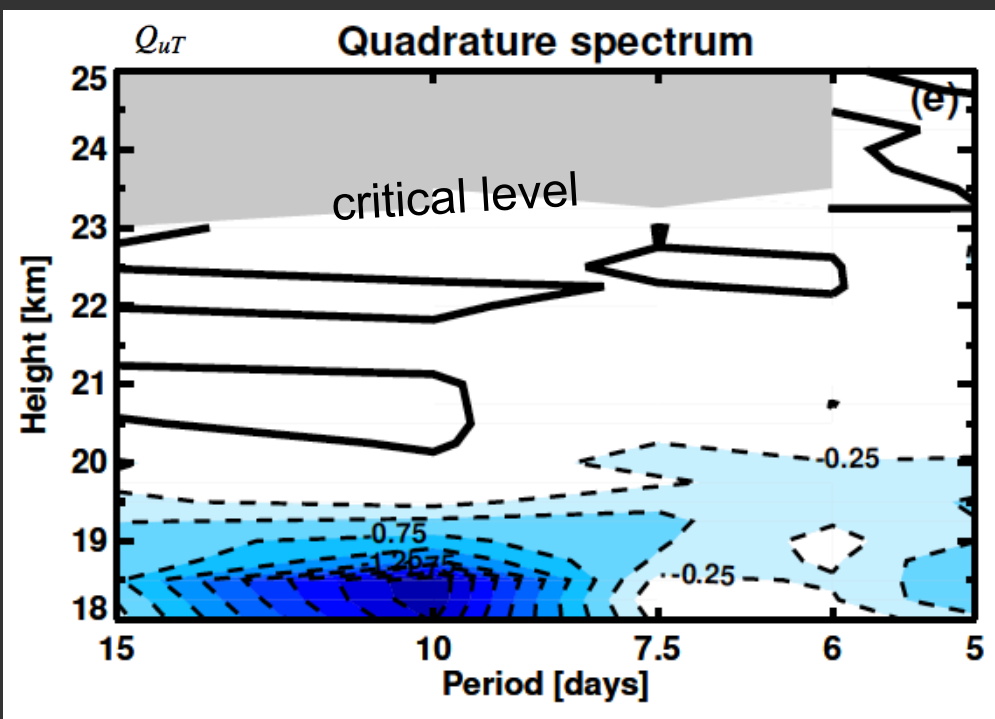
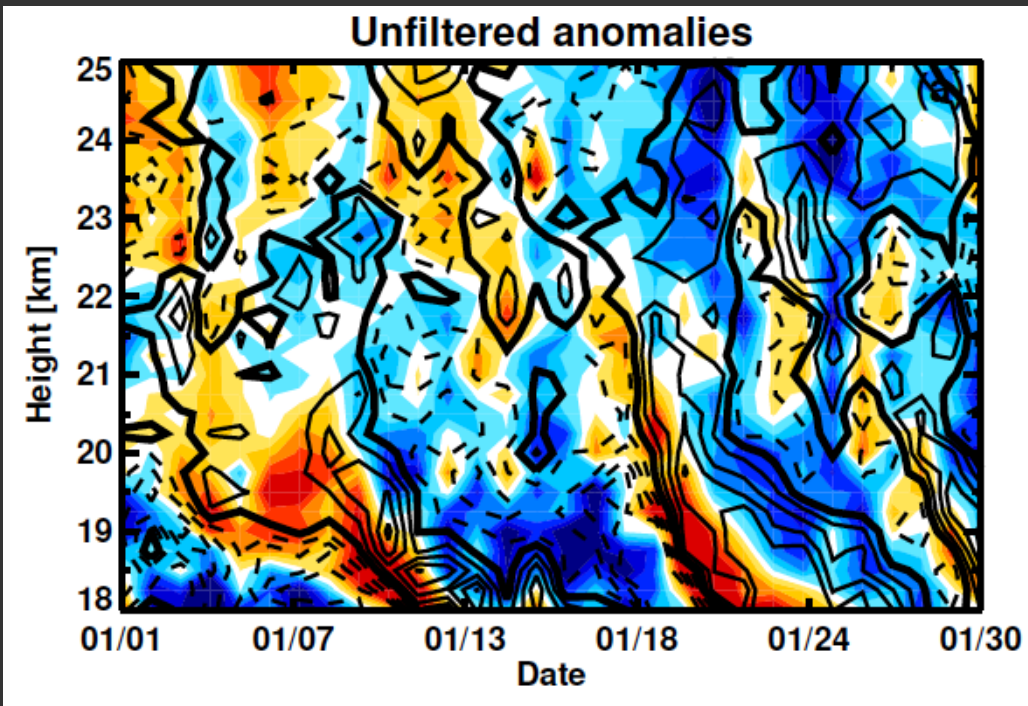
Wallace & Kousky (1968)

# Example:

Gan Island (0.7°S, 73.2°E)  
DYNAMO, January 2012

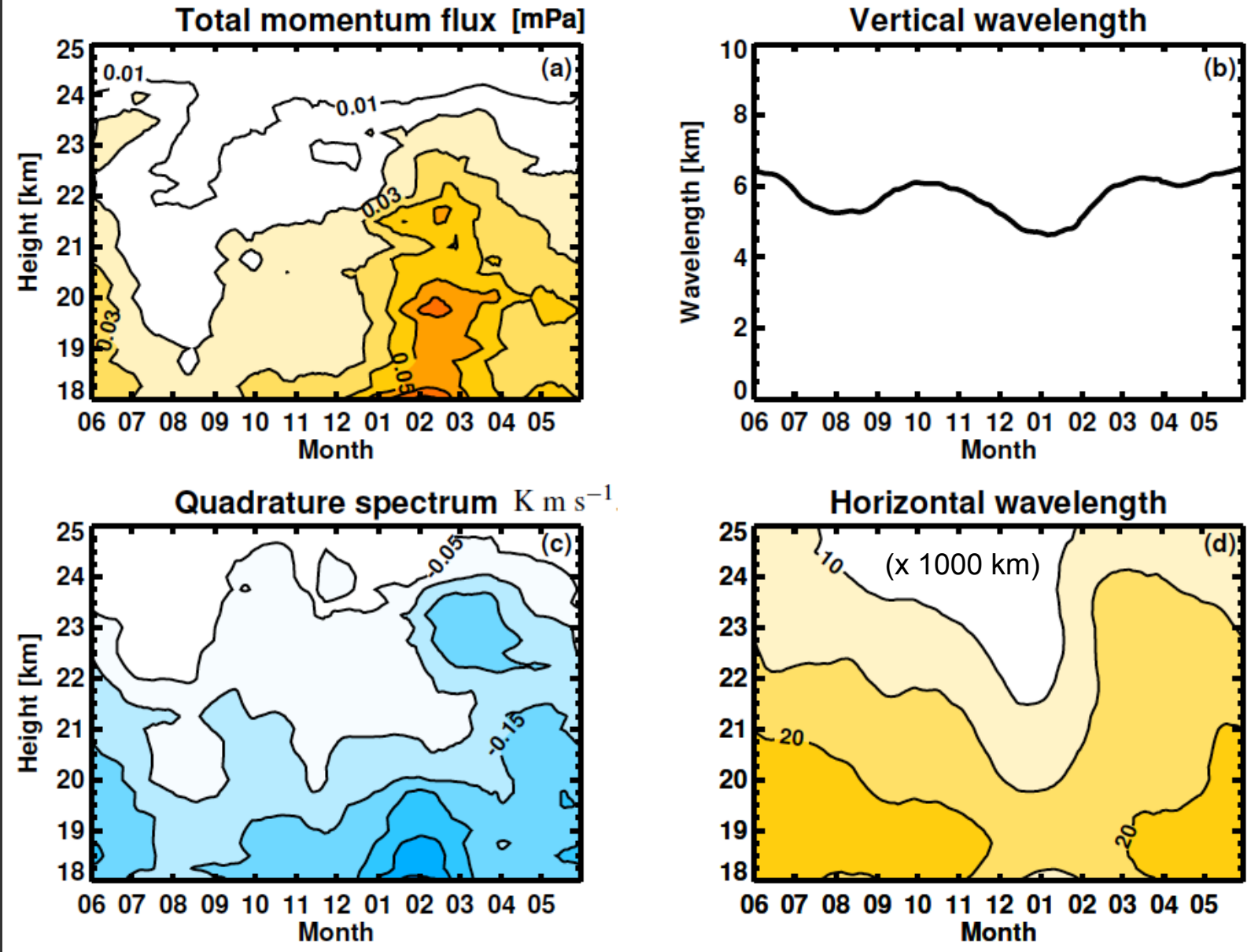
High-vertical resolution  
radiosoundings!

$T'$  (shading, 1 K) &  $u'$  (contours, 3 m/s)

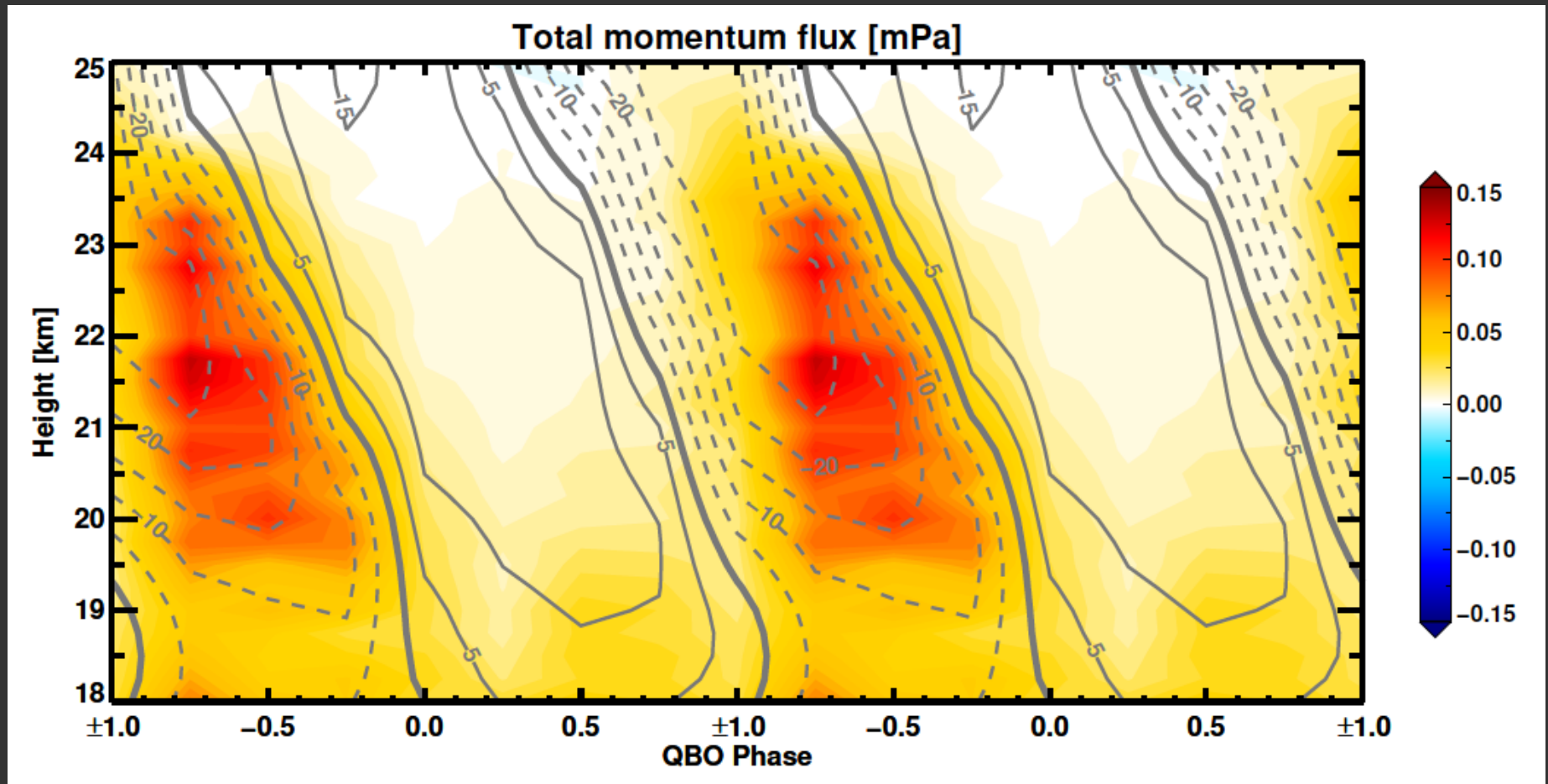




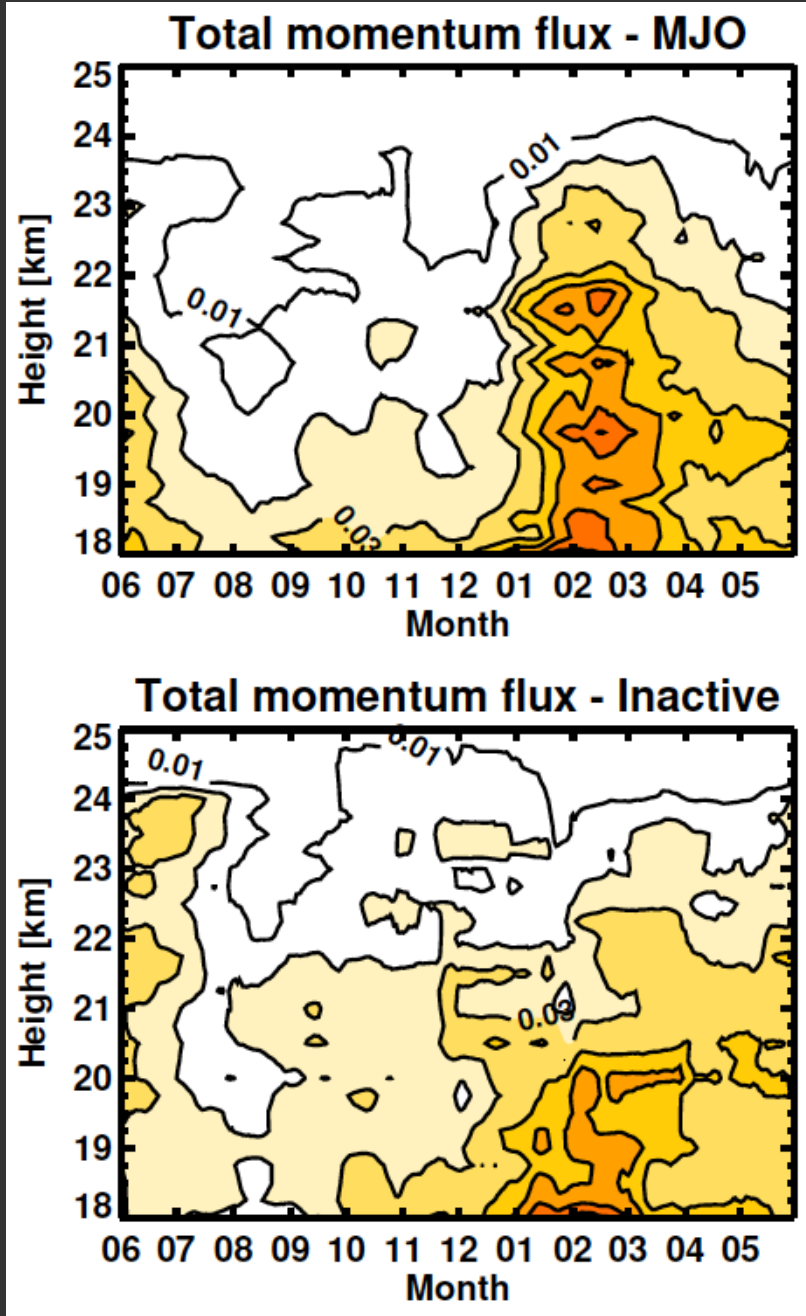
# Climatology (2003–2013) for Manus ARM sounding site (2.0°S, 147.4°E)



# QBO composite (2003–2013) for Manus ARM sounding site (2.0°S, 147.4°E)



→ Kelvin wave momentum flux drives  $E'y \rightarrow W'y$  transition (as expected) and is suppressed in westerly QBO phase



## MJO modulation of lower stratospheric Kelvin wave activity?

→ inconclusive (difference not statistically significant)

Manus ARM sounding site (2.0°S, 147.4°E)

## Conclusions – Part II

- Quadrature  $u'$ - $T'$  spectrum applied to radiosoundings  
→ Kelvin wave momentum flux
- Strongest lower stratospheric wave activity during boreal winter/spring (inferred using Manus site in west pacific)
- Possibly modulation by MJO, but inconclusive
- Kelvin wave driving of QBO easterly→westerly transition confirmed (cf. many previous studies – e.g. Sato & Dunkerton, 1997; Ern & Preusse, 2009)